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# Dark Energy in the Local Universe

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## GLOBAL DARK ENERGY

**Einstein (1917): Cosmological constant  $\Lambda \equiv$  Global antigravity, if  $\Lambda > 0$**

**Static universe  $\rightarrow$  Gravity + Antigravity = 0**

**Friedmann (1922-24): Exact GR solutions with  $\Lambda$**

**Expanding universe  $\rightarrow$  Gravity + Antigravity = f (t)**

**Riess et al. (1998), Perlmutter et al. (1999): Global acceleration**

$$\Lambda > 0$$

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## $\Lambda$ CDM

**Standard  $\Lambda$ CDM Model: DE  $\equiv$  Einstein's  $\Lambda$**

**Observations (WMAP-2006, etc.):**

**DE contributes 70-75% to the present total mass/energy of the universe**

$$\rho_{\Lambda} = (c^2/8\pi G) \Lambda = (0.72 \pm 0.03) \cdot 10^{-29} \text{ g/cm}^3$$

**DE antigravity dominates at**

$$z < z_{\Lambda} \approx 0.7; \quad t > t_{\Lambda} \approx 7 \text{ Gyr}$$

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## VACUUM

### MACROSCOPIC DESCRIPTION: Einstein-Gliner vacuum

**Gliner (1965):**

- \* Equation of state  $p_{\Lambda} = -\rho_{\Lambda}$
- \* Perfectly uniform
- \* Density  $\rho_{\Lambda}$  is constant in any reference frame

**WMAP (2006):**  $p_{\Lambda}/\rho_{\Lambda} = -1 \pm 0.1$

**Planck (launched 14 apr 2009):**  $\pm 0.03-0.02$

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## ANTIGRAVITY

**GR: effective gravitating density**

$$\rho_{\text{eff}} = \rho + 3 p$$

**DE:  $\rho_{\text{eff}} = -2 \rho_{\Lambda} < 0 \rightarrow$  antigravity**

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## PHYSICAL NATURE???

### MICROSCOPIC STRUCTURE:

Severe challenge to fundamental physics

Zeldovich (1967):  $\Lambda \equiv \text{Quantum Vacuum}$

Arkani-Hamed et al. (2001):  $\rho_\Lambda \sim (M_{EW}/M_P)^8 \rho_P$

$M_{EW} \sim 1 \text{ TeV}, M_P \sim 10^{15} \text{ TeV}$

$\rho_P \sim M_P^4$

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## LOCAL DARK ENERGY

DE is discovered at near-horizon distances of  $\sim 1\,000$  Mpc

*Does DE act on relatively small local scales?*

In principle, yes -- if  $DE = \Lambda$

Specifically:

- \* *How strong may local DE antigravity be?*
- \* *May DE antigravity dominate locally?*

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# LOCAL GRAVITY-ANTIGRAVITY

**Schwarzschild-de Sitter static spacetime:**

**point-like mass on DE background**

$$ds^2 = A(R) dt^2 - R^2 d\Omega^2 - A^{-1} dR^2$$

$$A(R) = 1 - 2GM/R - (8\pi G/3) \rho_\Lambda R^2$$

**Newtonian limit:**

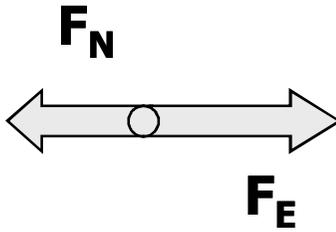
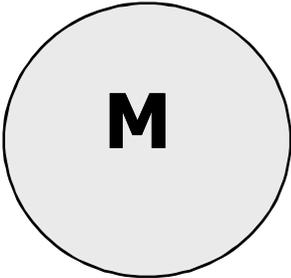
$$1 + U \approx A^{1/2} \approx 1 - GM/R - (4\pi G/3) \rho_\Lambda R^2$$

$$F(R) = - \text{grad } U = - GM/R^2 + (8\pi G/3) \rho_\Lambda R$$



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# LOCAL DYNAMICS



**Newton Law**      $F_N = - G M / R^2$

**Einstein Law**      $F_E = - G M_{\text{eff}} / R^2$

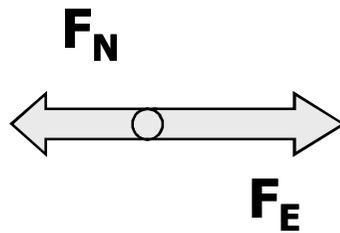
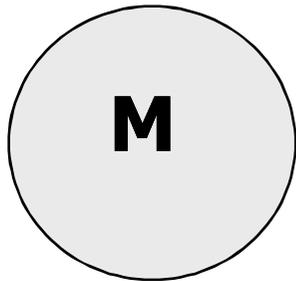
$$M_{\text{eff}} = (4\pi/3) \rho_{\text{eff}} R^3 = (4\pi/3) (\rho + 3p) R^3 = - (8\pi/3) G \rho_{\Lambda} R^3$$

$$F_E = + (8\pi/3) G \rho_{\Lambda} R$$

(per unit mass)

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## ZERO-GRAVITY RADIUS



$$F(R=R_\Lambda) = F_N + F_E = 0:$$

$$R_\Lambda = [ 3 M / (8\pi \rho_\Lambda) ]^{1/3}$$

$$\approx 1 [ M / 10^{12} M_{\text{sun}} ]^{1/3} \text{ Mpc} \quad (\text{Chernin et al. 2000})$$

**Groups of galaxies:**  $M = (1-10) 10^{12} M_{\text{sun}} \rightarrow R_\Lambda = 1-2 \text{ Mpc}$

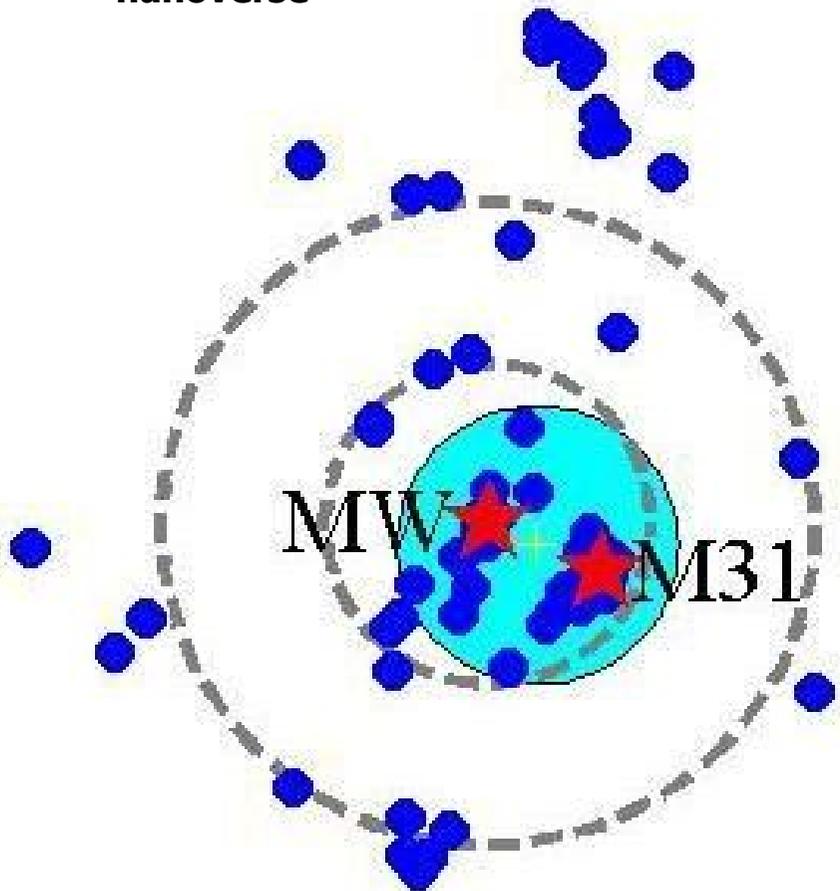
**Clusters of galaxies:**  $M = (1-10) 10^{14} M_{\text{sun}} \rightarrow R_\Lambda = 5-10 \text{ Mpc}$

$R_\Lambda$  is local counterpart of global redshift  $z_\Lambda \approx 0.7$

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# LOCAL HUBBLE CELL (LHC)

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**LHC = Local Group +  
local expansion outflow**

**LHC IS NATURAL SETUP  
TO DETECT AND MEASURE  
LOCAL DARK ENERGY**

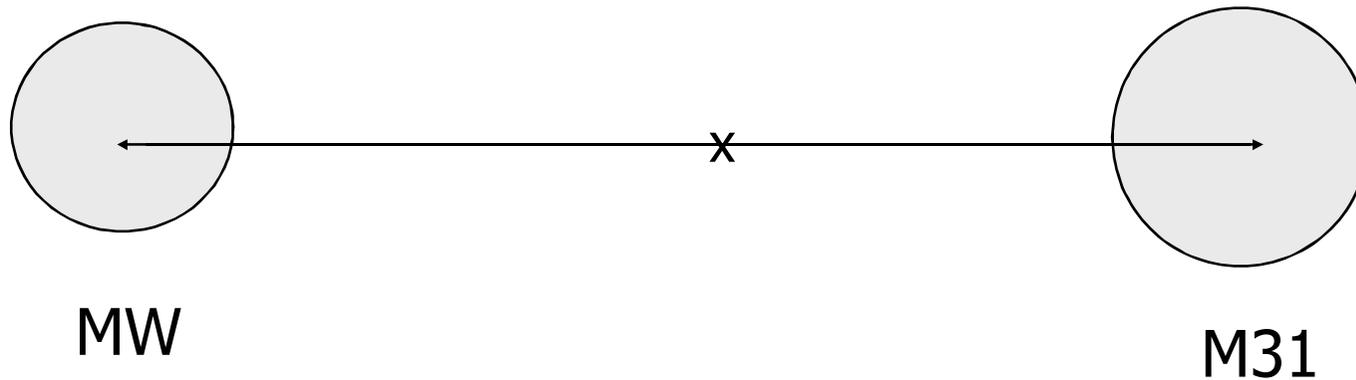
**Hubble cells are typical population  
of the Local Universe (Hubble 1936)**

6 Mpc

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Karachentsev et al. 2006

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## LOCAL GROUP

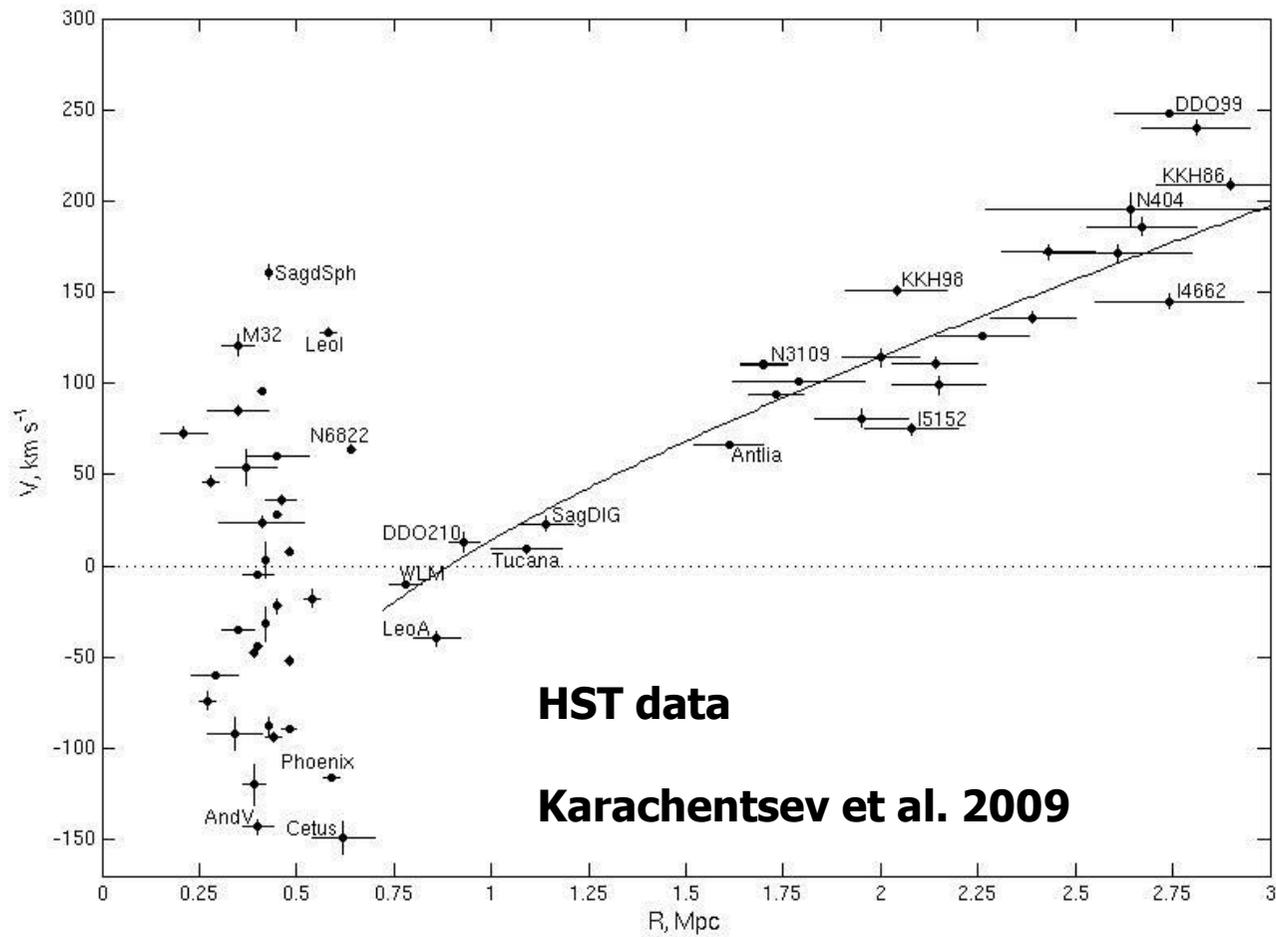


**Giant MW-M31 binary and  $\approx$  50 dwarf galaxies**

**MW and M31 are separated by distance of 0.7 Mpc  
and move toward each other with  
relative velocity – 120 km/s now**

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# LHC PHASE PORTAIT



**Group:**  
**R < 1.2 Mpc**

**Outflow:**  
**R > 1.6 Mpc**

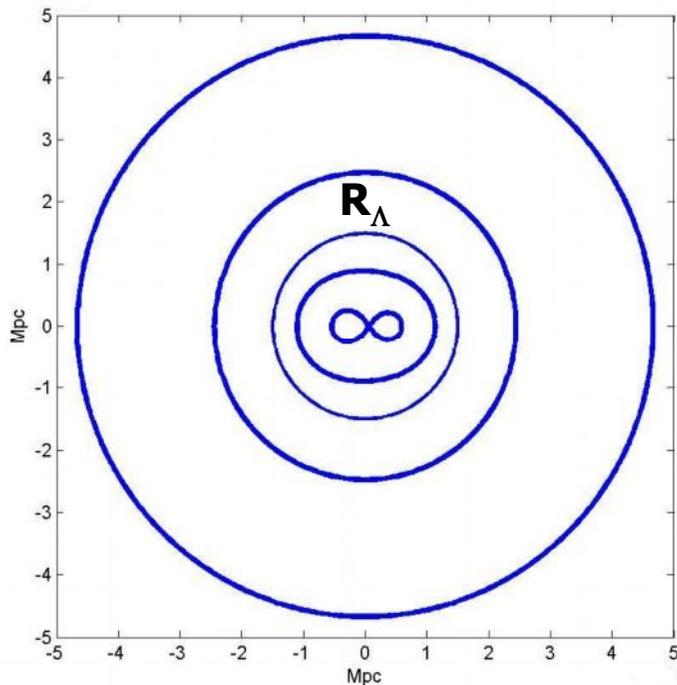


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# LHC ZERO-GRAVITY RADIUS

## LHC gravity-antigravity potential



### Gravitationally bound group

$R < R_{\Lambda}$ : **gravity dominates**

### Expansion outflow

$R > R_{\Lambda}$ : **antigravity dominates**

**Antigravity makes outflow cool:  
linear velocity-distance relation with  
low dispersion**

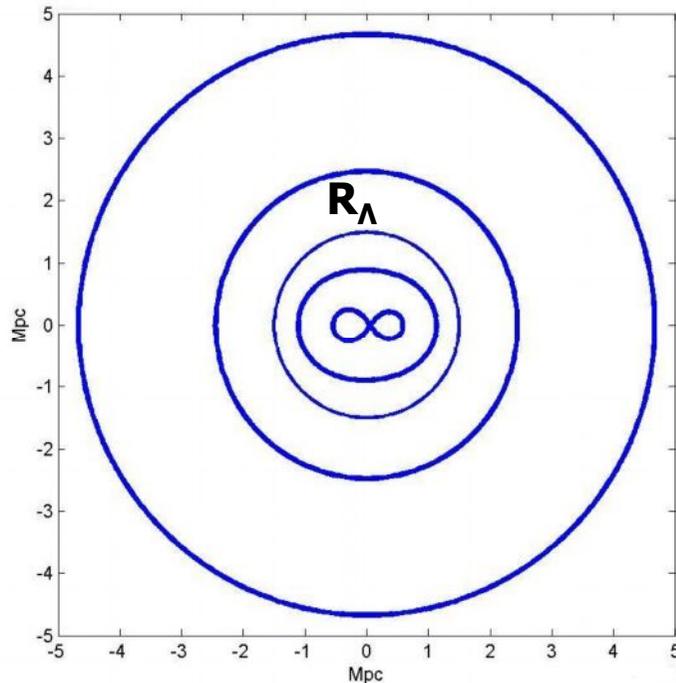
**(Chernin et al. 2000-04,  
Maccio' et al. 2005, Sandage et al. 2006)**

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# LHC MODEL

## LHC gravity-antigravity potential



## Group:

**MW\_M31 binary  
as bound linear  
two-body system**

## Expansion outflow:

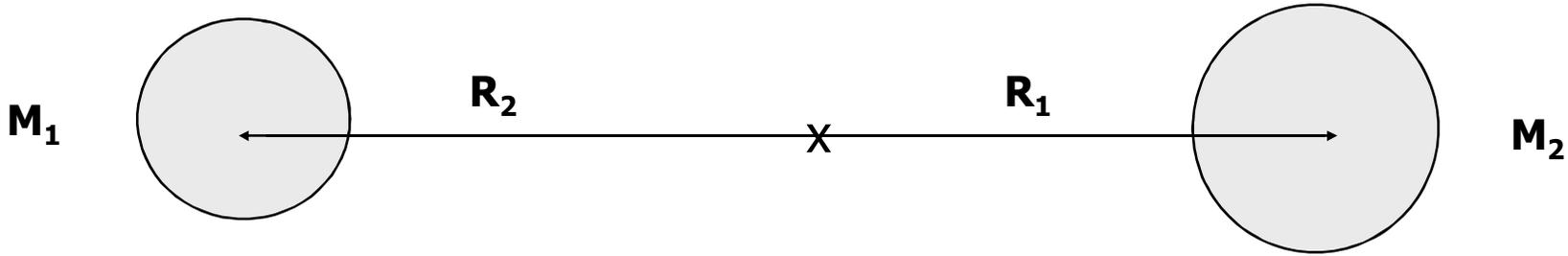
**dwarf galaxies as  
test particles  
moving in a spherical  
gravity-antigravity  
static potential**

**The cell is embedded in the uniform DE background**

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# MW-M31 BINARY



$D = R_1 + R_2 = 0.7 \text{ Mpc}; \quad V = -120 \text{ km/s}$

**Linear two-body problem on DE background: equations of motion**

$$d^2R_1/dt^2 = - G M_2/D^2 + G (8\pi/3)\rho_\Lambda R_1$$

$$- d^2R_2/dt^2 = G M_1/D^2 - G (8\pi/3)\rho_\Lambda R_2$$

(barycenter reference frame)



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## GRAVITY-ANTIGRAVITY POTENTIAL

$$d^2D/dt^2 = -GM/D^2 + G(8\pi/3)\rho_\Lambda D$$

$$(M = M_1 + M_2, D = R_1 + R_2)$$

The first integral

$$(1/2) V^2 = GM/D + G(4\pi/3)\rho_\Lambda D^2 + E,$$

$$(E = \text{Const})$$

Effective potential :  $U = -GM/D - G(4\pi/3)\rho_\Lambda D^2$

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# BINDING CONDITION

Binary is gravitationally bound, if

$$E < U_{\max} = - (3/2) GM^{2/3} [(8\pi/3) \rho_{\Lambda}]^{1/3}$$

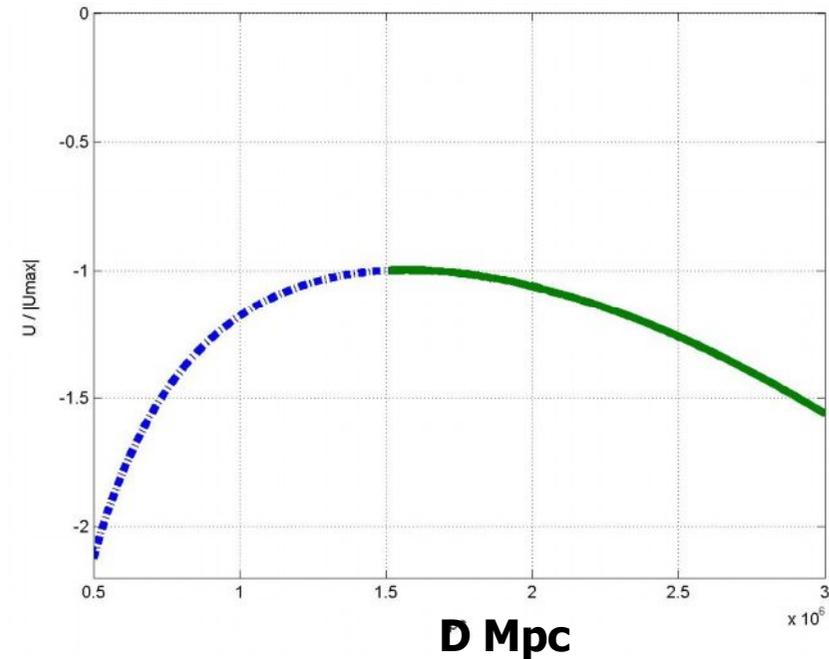
Binding condition + first integral

$$(1/2) V^2 = GM/D + G (4\pi/3) \rho_{\Lambda} D^2 + E$$

lead to lower limit to mass

$$M > M_1 = 3.3 \cdot 10^{12} M_{\text{sun}}$$

(KW:  $M_1 = 1.1$ )



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# TIMING ARGUMENT

Gravitational instability in  $\Lambda$ CDM model is terminated when antigravity becomes stronger than gravity at  $t = t_\Lambda = 7 \text{ Gyr}$  (e.g. Chernin et al. 2003)

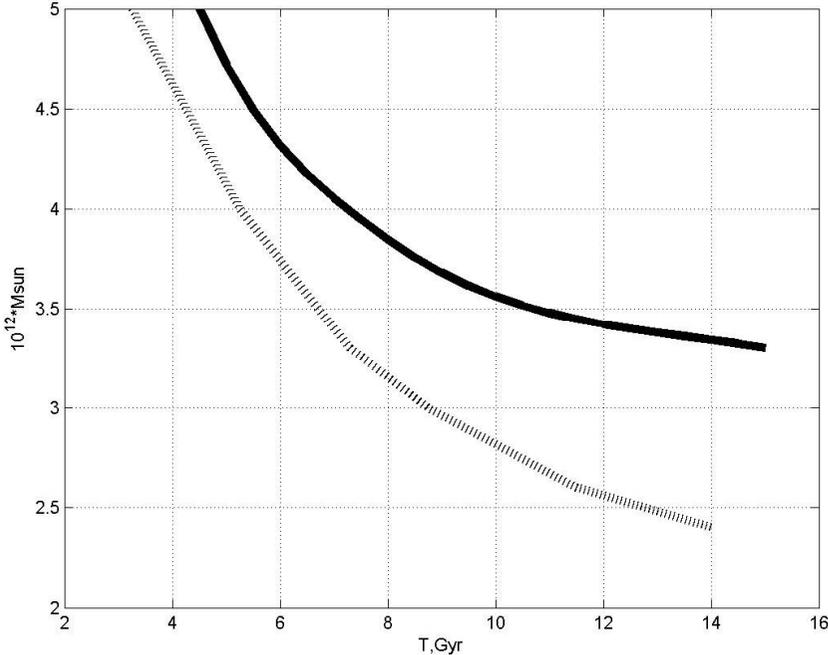
Therefore binary collapse time

$$T > t_0 - t_\Lambda \approx 7 \text{ Gyr}$$

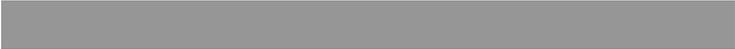
M-T relation leads to upper limit to mass:

$$M < M_2 = 4.1 \cdot 10^{12} M_{\text{sun}}$$

(KW:  $M_2 = 3.2$ )



M-T relation comes from second integration of equation of motion



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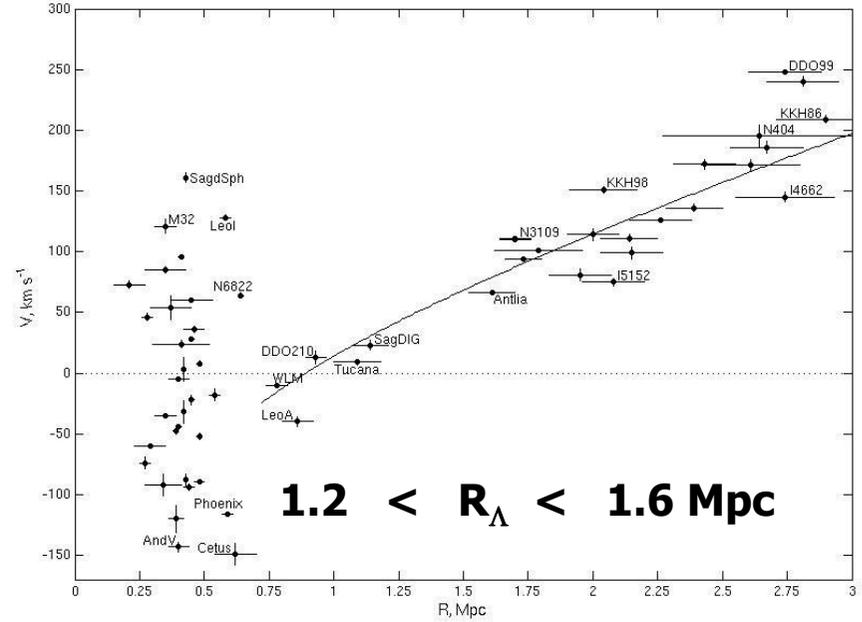
# LIMITS TO ZERO-GRAVITY RADIUS

$$R_{\Lambda} = [ 3 M / (8\pi \rho_{\Lambda}) ]^{1/3} \rightarrow M = (8\pi/3) \rho_{\Lambda} R_{\Lambda}^3$$

$$M_3 < M < M_4$$

$$M_3 = 1.7 \cdot 10^{12} M_{\text{sun}}$$

$$M_4 = 3.9 \cdot 10^{12} M_{\text{sun}}$$



HST data: Karachentsev et al. 2009



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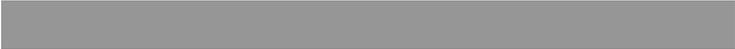
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# LOCAL GROUP MASS

**Four limits to group mass in combination**

$$3.3 < M < 3.9 \cdot 10^{12} M_{\text{sun}}$$

**If local DE density = global value  $\rho_{\Lambda}$**



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## LOCAL DE DENSITY

**If local DE density is unknown  $\rho_x$ ,  
four mass limits are functions of  
local DE density, or  $x = \rho_x / \rho_\Lambda$**

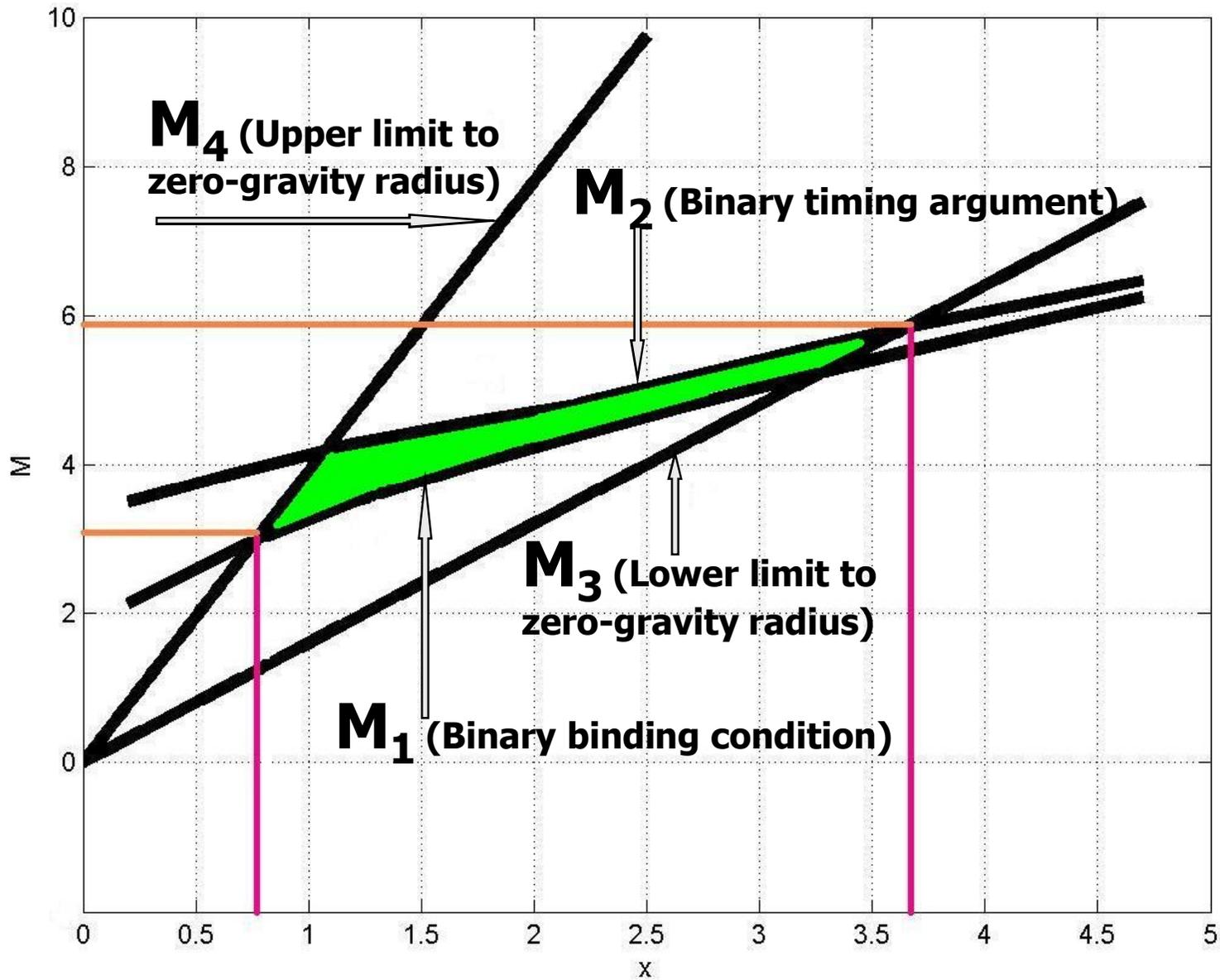
$$M > M_1(x), \quad M < M_2(x),$$

$$M < M_3(x), \quad M_4 > M_4(x)$$

**Observational data:  $D = 0.7$  Mpc,  $V = -120$  km/s**

$$1.2 < R_\Lambda < 1.6 \text{ Mpc}$$

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$$x = \rho_x / \rho_\Lambda$$

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# CONCLUSIONS

**LHC is natural setup for measuring Local Group mass and local DE density at  $\sim 1$  Mpc in self-consistent way**

**Total (dark matter + baryons) mass of Local Group**

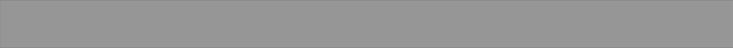
$$3.1 < M < 5.9 \cdot 10^{12} M_{\text{sun}}$$



**(20-30% accuracy)**

**If  $\rho_x = \rho_\Lambda$ :  $3.3 < M < 3.9 \cdot 10^{12} M_{\text{sun}}$**

**$\Lambda$ CDM Millennium Simulations (2008):  $1.7 < M < 5.1 \cdot 10^{12} M_{\text{sun}}$**



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# CONCLUSIONS

**DARK ENERGY EXISTS ON SCALE  $\sim 1$  Mpc**

**ANTIGRAVITY IS STRONG ON THIS SCALE**

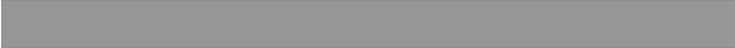
**Local density of dark energy**

$$0.8 < \rho_x < 3.7 \rho_\Lambda$$

===== (20-30% accuracy)

**Local DE density at  $R \sim 1$  Mpc is close, if not exactly equal,  
to global DE density at  $R \sim 1\ 000$  Mpc**

**NEW INDEPENDENT EVIDENCE FOR  
EINSTEIN'S IDEA OF UNIVERSAL ANTIGRAVITY**



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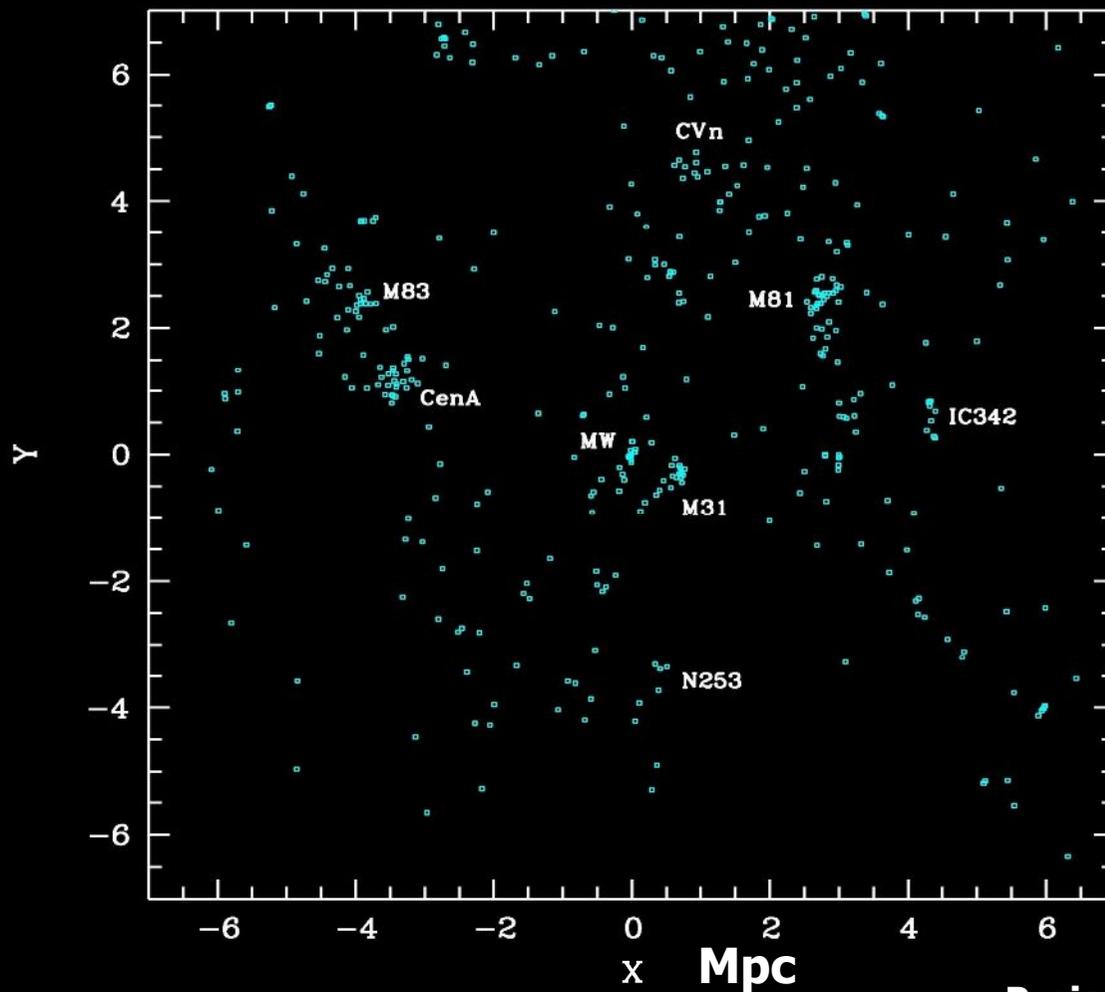
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# LOCAL UNIVERSE



**Karachentsev et al.  
(2006):**

**HST map  
of the local volume  
of 14 Mpc across**

**Projection on the Supergalactic plane**

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## LOCAL UNIVERSE

**The Local Universe is a network of receding partly overlapping “Hubble cells”**

**The Hubble cell is a gravitationally bound galaxy system (group or cluster) + an expansion flow of galaxies around it**

**The network (100-300 Mpc across) is embedded in the uniform dark energy background**



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## KAHN-WOLTJER MODEL

$$d^2D/dt^2 = -G M/D^2 \quad \rightarrow \quad \frac{1}{2} V^2 = GM/D + E$$

$$(dD/dt = V; \quad D = R_1 + R_2; \quad M = M_1 + M_2)$$

The first integral and the bound condition  $E < 0$  imply:

$$M > M_{\min} = \frac{1}{2} V^2 D/G = 10^{12} M_{\text{sun}}$$

$$M_{\min} \sim 10 M_L$$

First evidence for dark matter in MW and M31

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