

*Particle acceleration in Galaxy Clusters  
&  
connection with cluster mergers*

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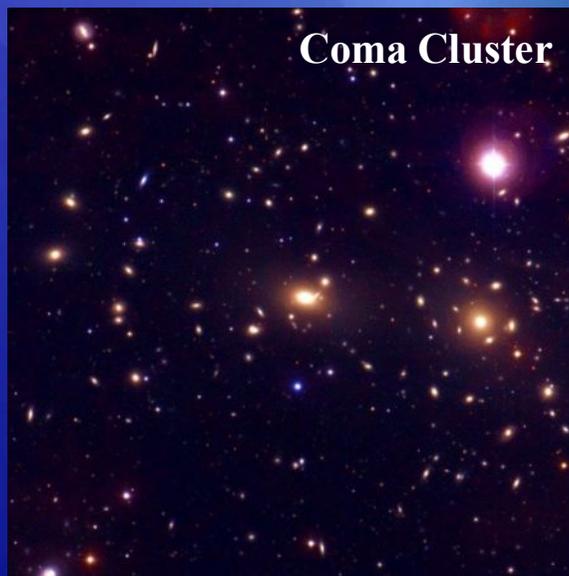
# Outline

- Galaxy Clusters & non thermal phenomena
- Physics & dynamics of CR in galaxy clusters
- CR protons (limits)
- CR electrons : Radio Halos (turbulence?)
- General Picture of non-thermal clusters  
(calculations of broad band non thermal emission)
- Expectations : ... steep spectrum diffuse radio emission & LOFAR+LWA

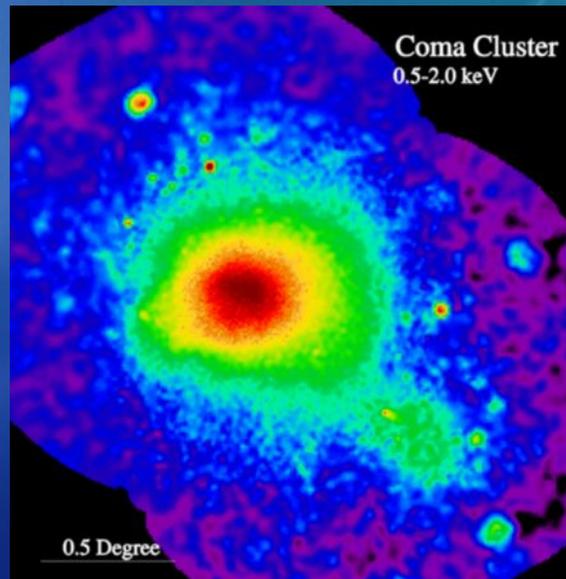
# Clusters of galaxies:

- Galaxy Clusters are the largest concentrations of matter in our Universe.
- They form by accretion & mergers between sub-units
- They extend over **2-4 Mpc** and have a total mass of  $\sim 10^{14}-10^{15} M_{\text{sol}}$
- They contain thousands of galaxies, hot diffuse gas and especially dark matter

Optical



X- ray



Galaxy cluster mass:

**Barions** 10% of stars in galaxies

15-20% of hot diffuse gas

**Dark Matter** 70%

stars + dark matter

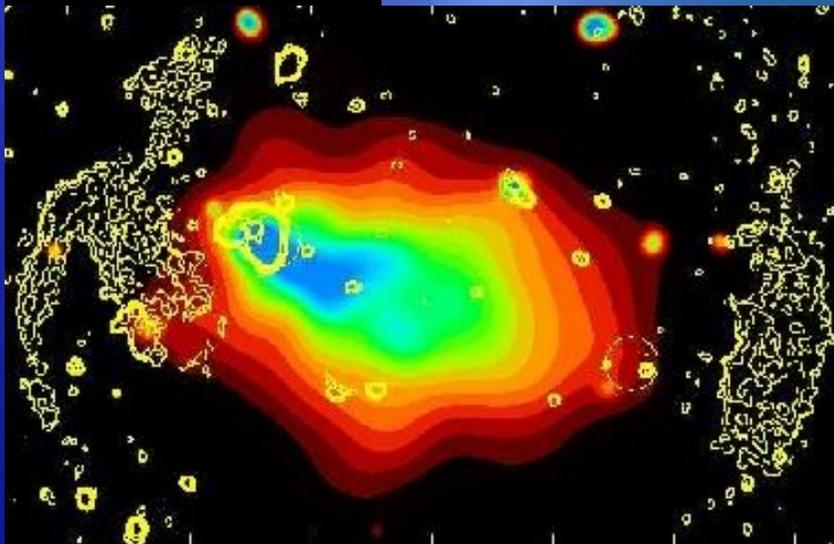
hot diffuse gas

# *Non-thermal components* & cluster mergers

**Radio Halos** and **Radio Relics** are only found in **non-relaxed** clusters with **recent /ongoing cluster mergers** (e.g. Buote 2001)

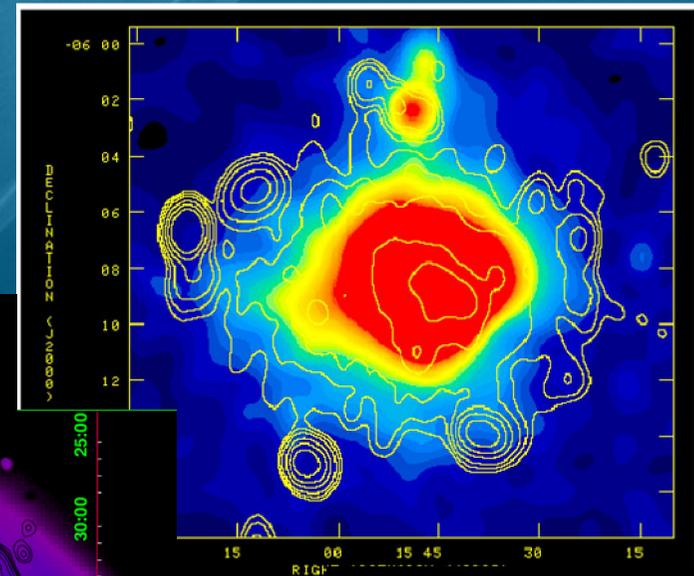
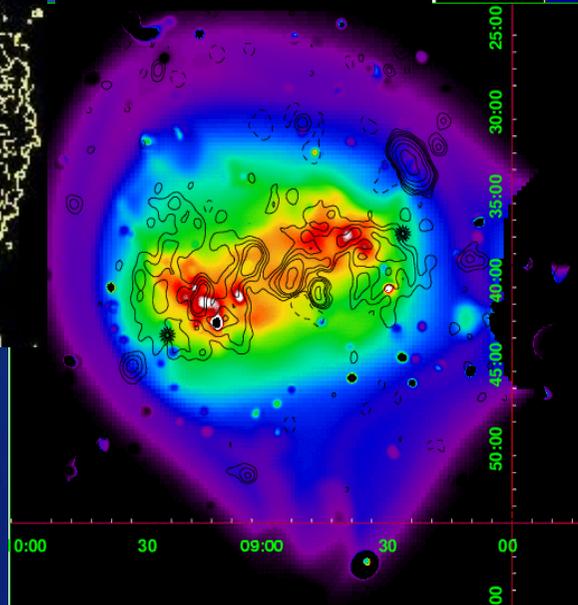
Mergings are the most energetic events in the Universe  $\approx$  **few  $10^{63}$  ergs** in a crossing time!

Abell 3376  
Bagchi et al. 2005



*Radio Relics*

Abell 754  
Henry et al. 2004



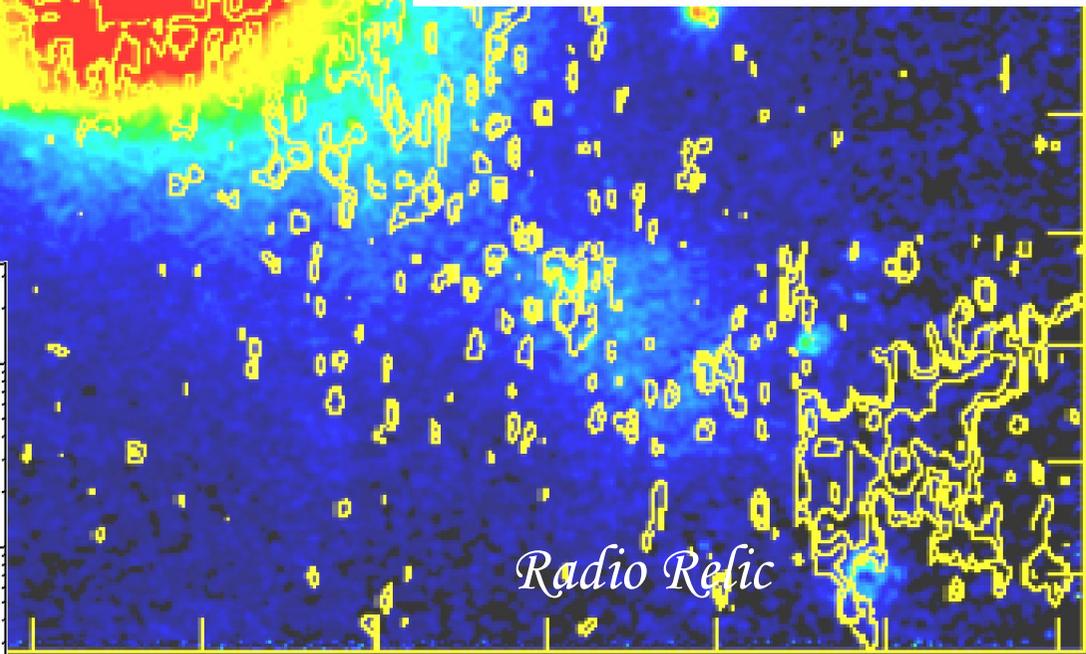
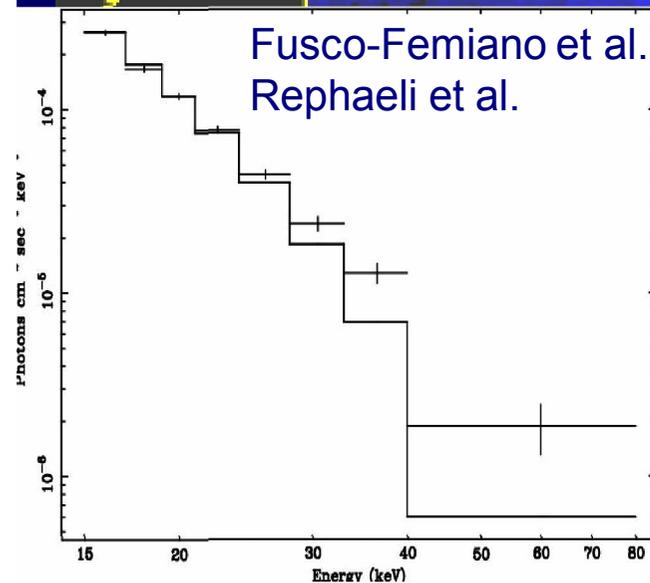
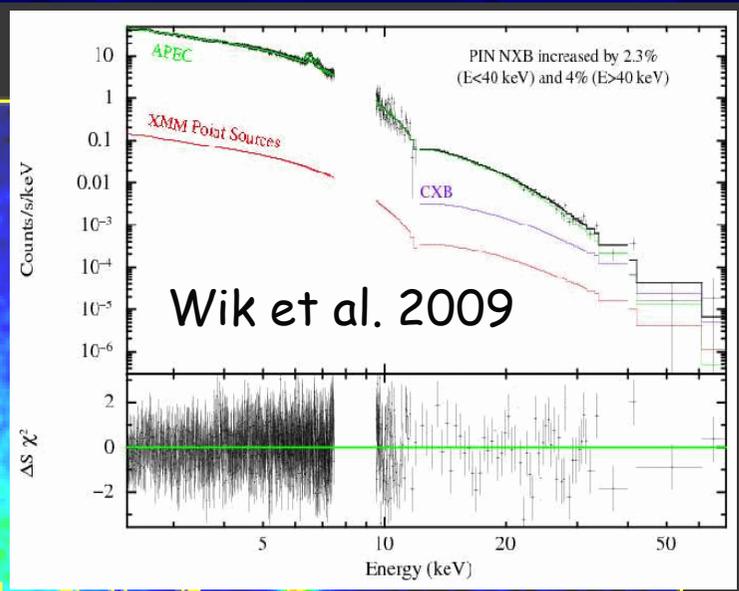
Abell 2163  
Feretti et al. 2001

*Radio Halos*

# Coma Cluster

28 50  
40  
30  
20  
10  
00  
27 50

*Radio Halo*



58 57 56 55 54 53 52

RIGHT ASCENSION (E1950)

Ajello et al. 2008, Fujita et al. 2009  
Eckert et al. 2008, Perez-Torres et al. 2009

# Injection & Dynamics of Cosmic Rays in GC

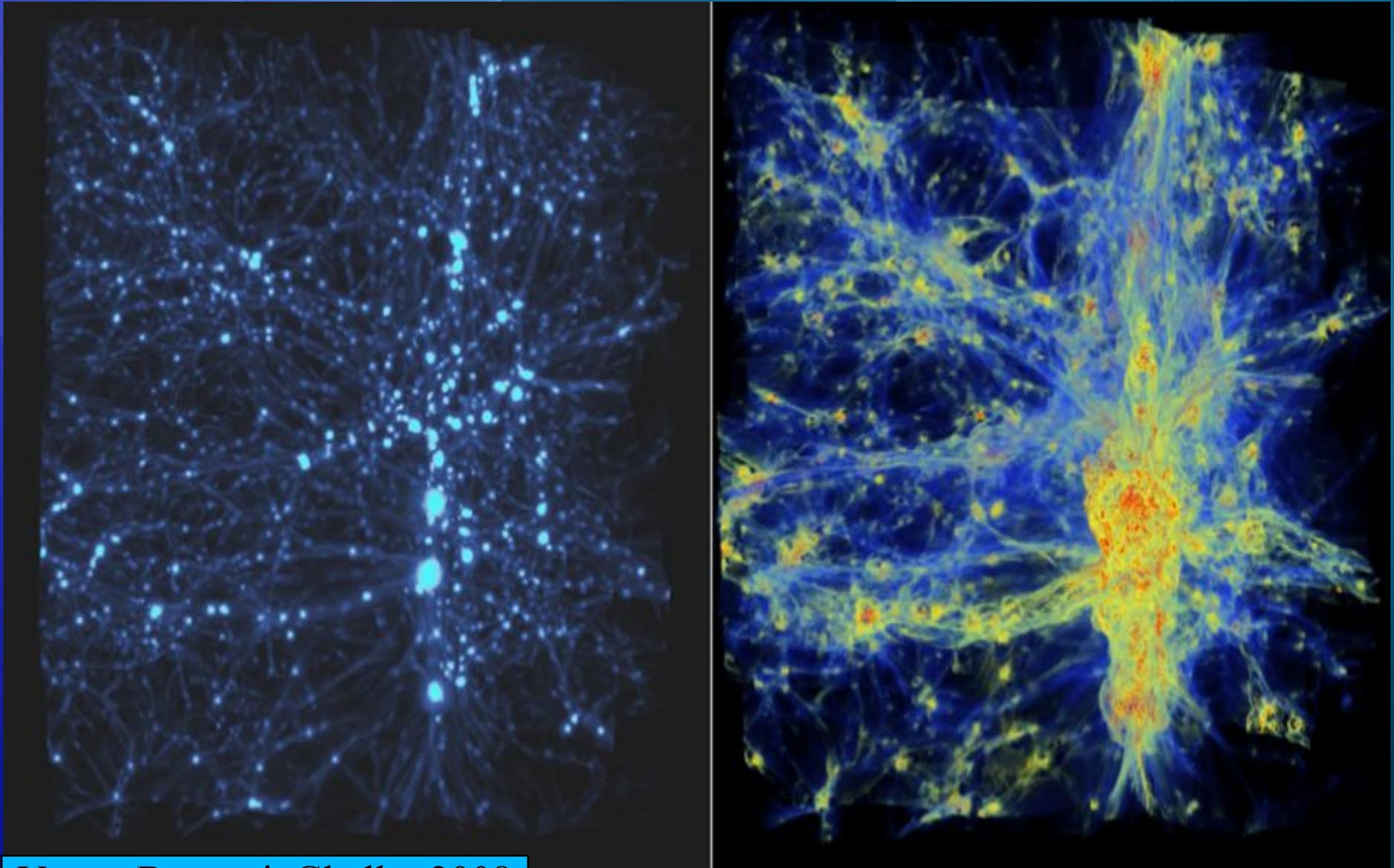
## Cosmological Shocks

(e.g. Sarazin 1999, Miniati et al. 2001, Blasi 2001, Gabici & Blasi 2003, Ryu et al. 2003, Pfrommer et al. 2006, 2008, Vazza, Brunetti, Gheller 2008)

## AGN, Galactic Winds

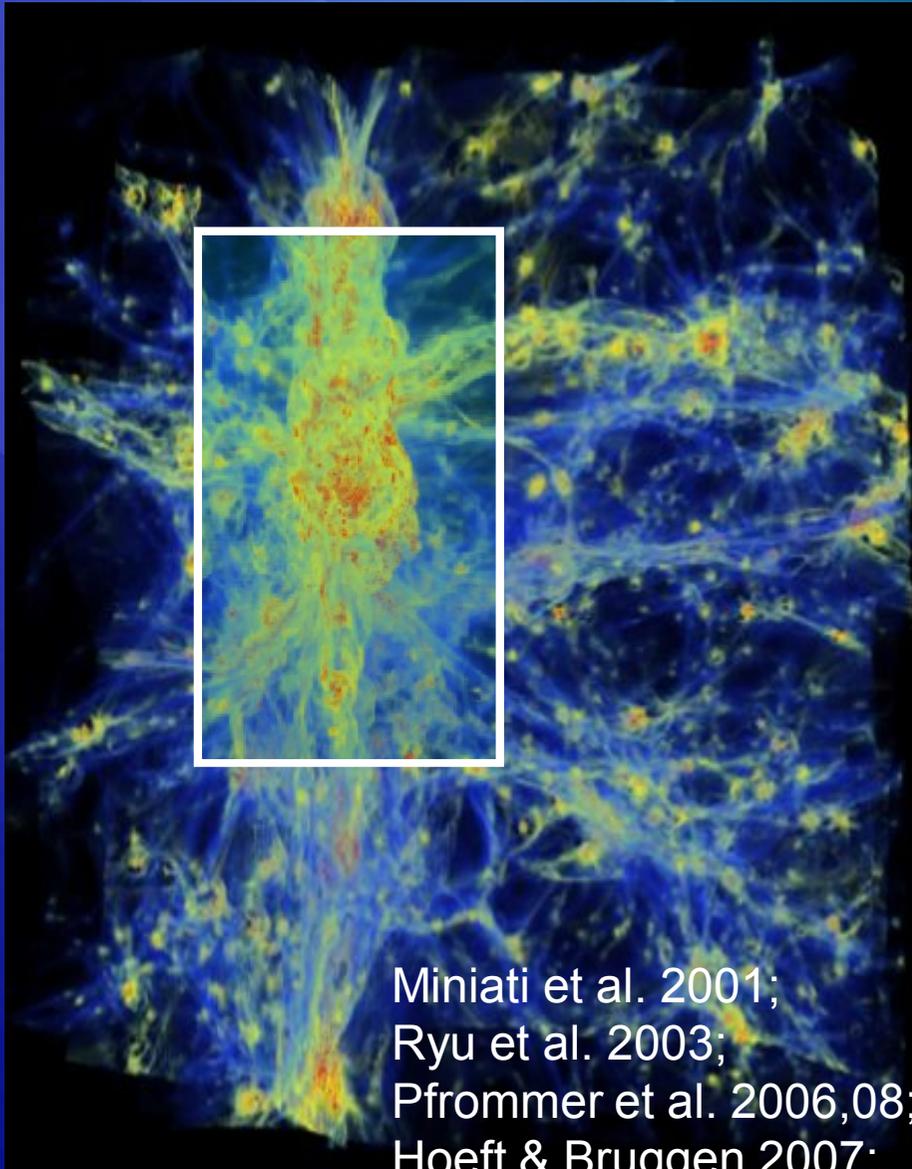
(e.g. Ensslin et al. 1998; Voelk & Atoyan 1999)

# Simulations : Shocks in Galaxy Clusters

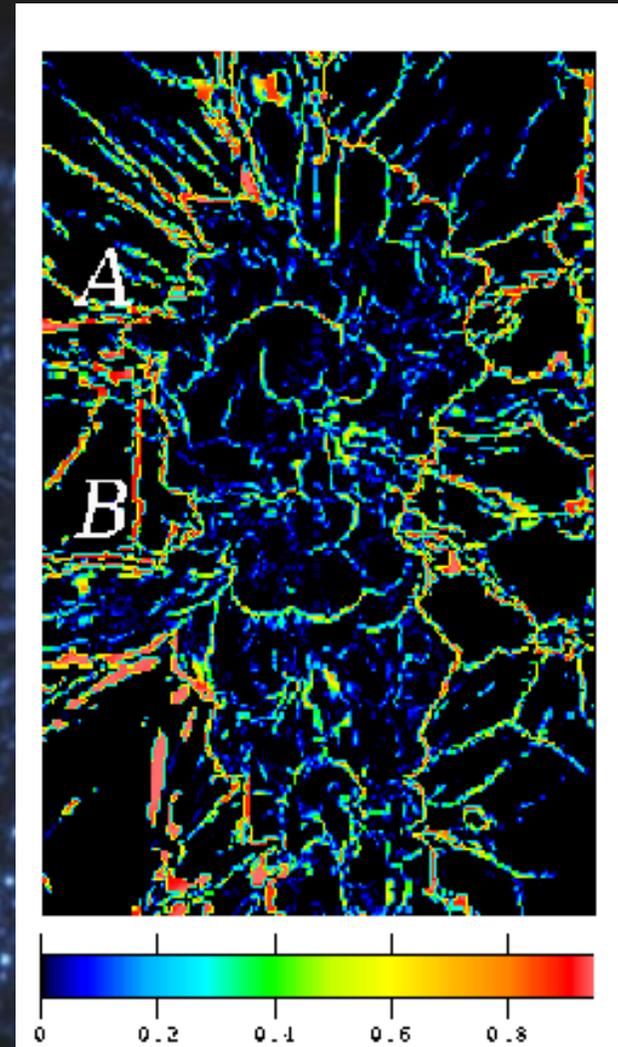


Vazza, Brunetti, Gheller 2008

# Shocks in Galaxy Clusters



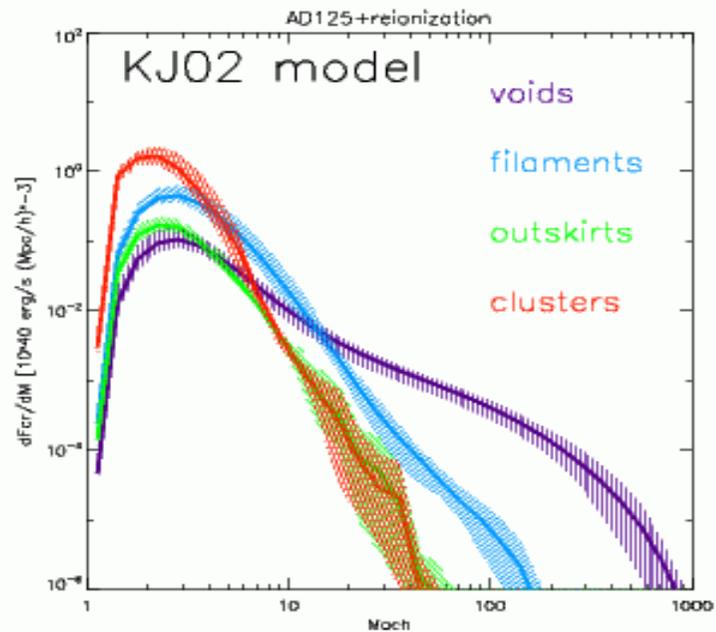
Miniati et al. 2001;  
Ryu et al. 2003;  
Pfrommer et al. 2006,08;  
Hoeft & Bruggen 2007;  
Skillman et al. 2008



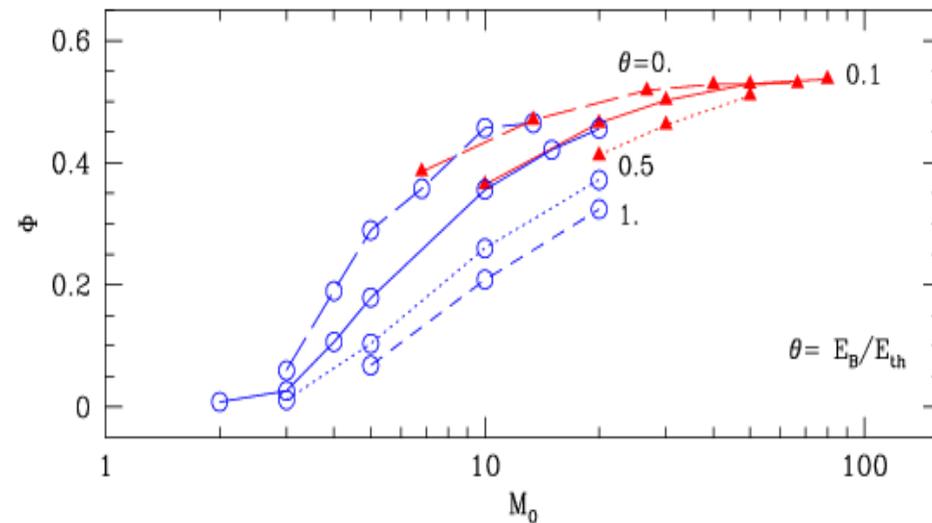
Vazza, Brunetti, Gheller 2008

# Uncertainties in CR acceleration

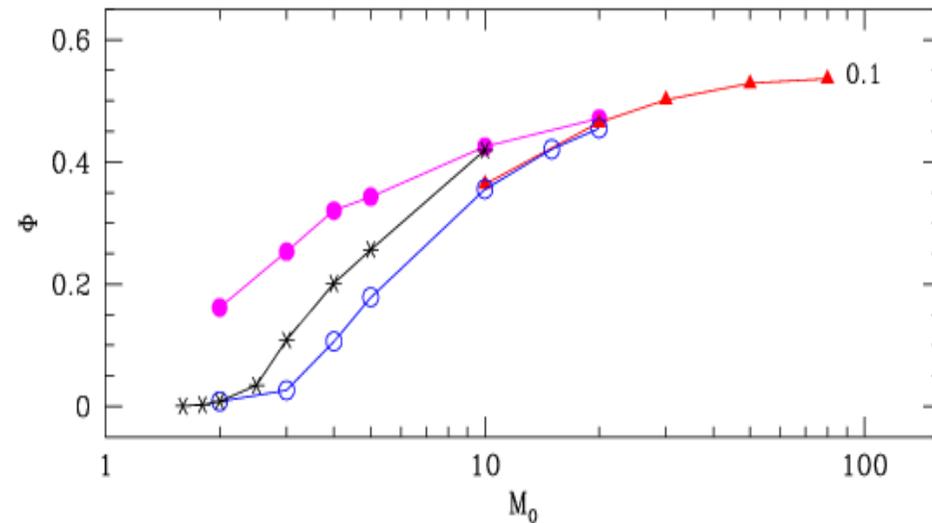
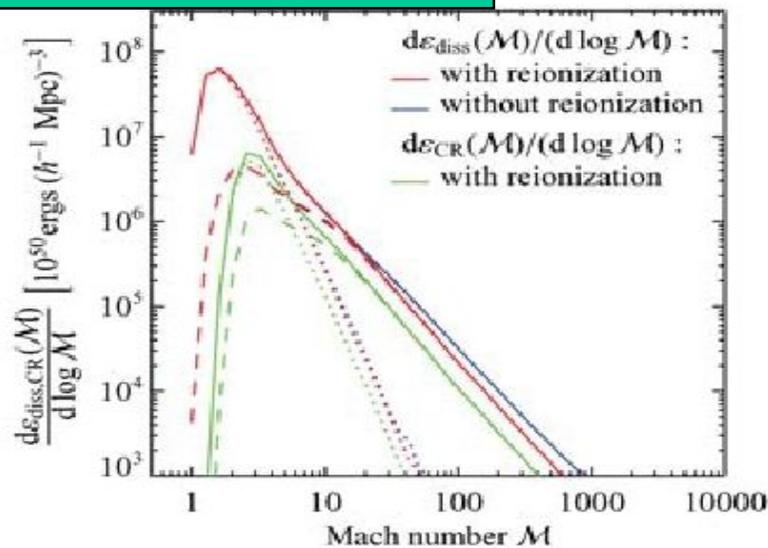
Vazza, Brunetti, Gheller 2008



Kang & Jones 2007

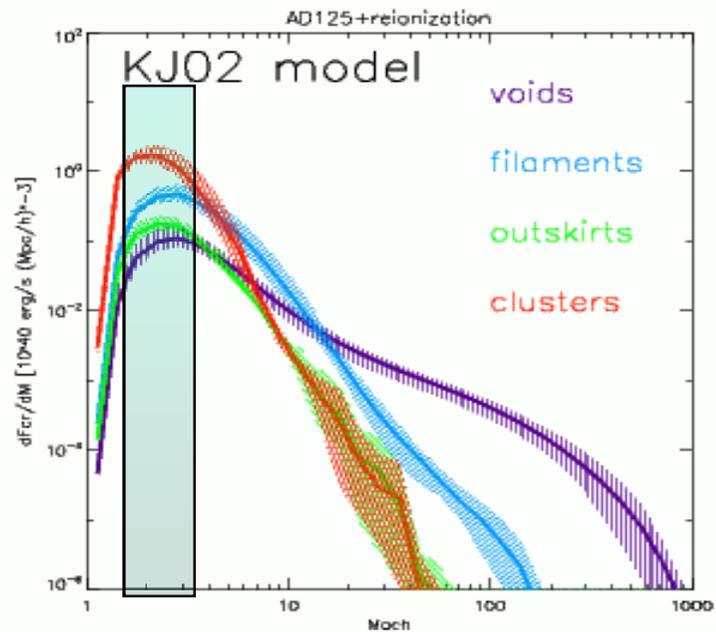


Pfrommer et al. 2008

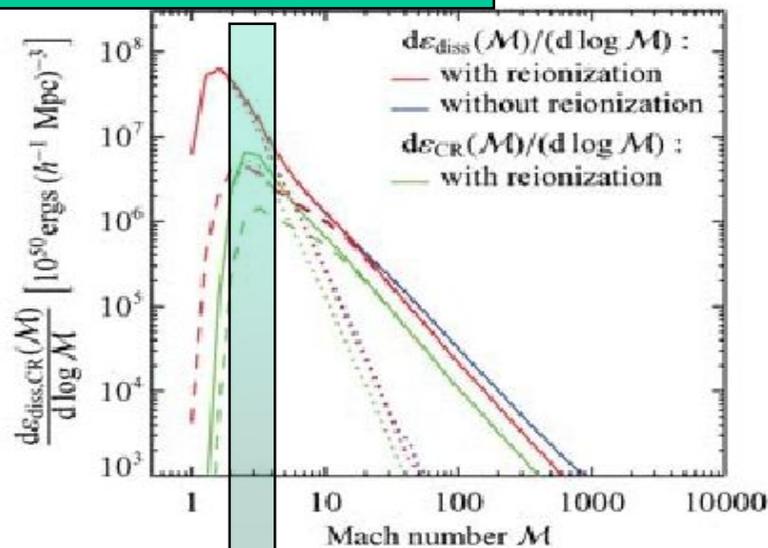


# Uncertainties in CR acceleration

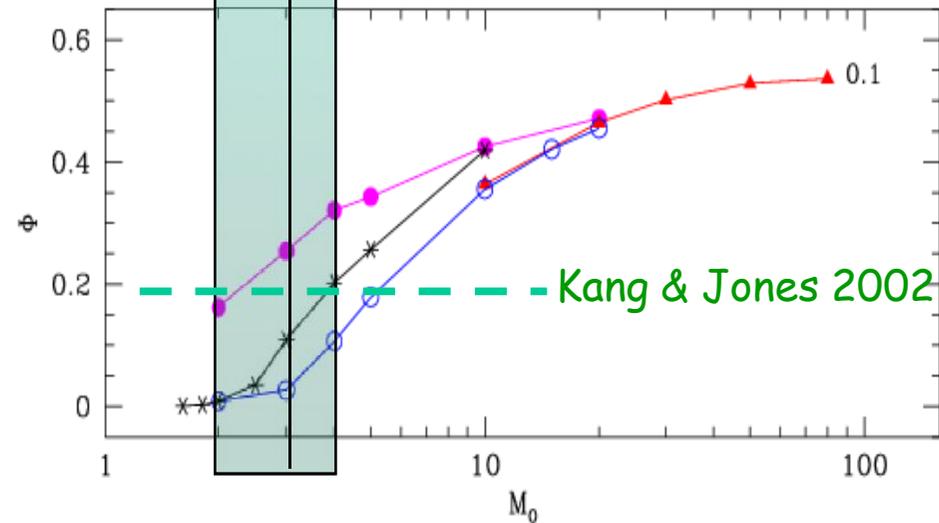
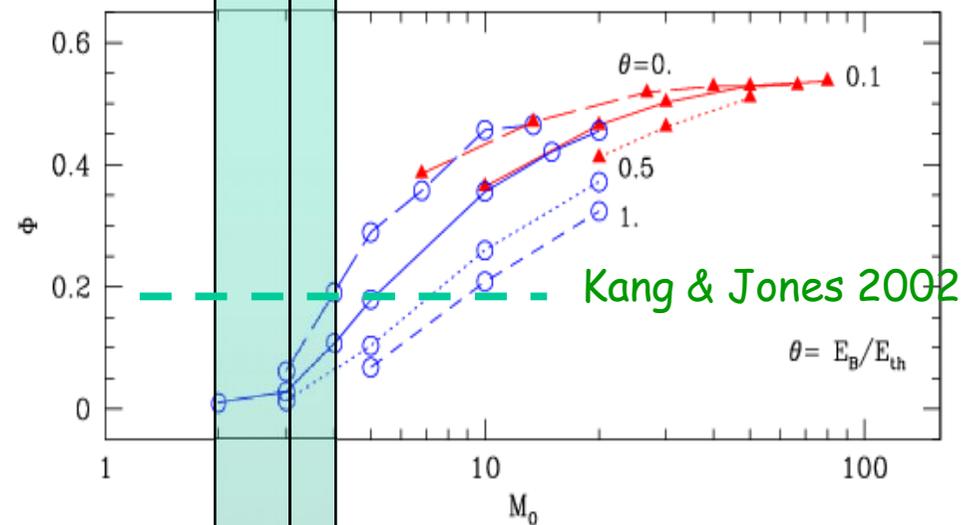
Vazza, Brunetti, Gheller 2008



Pfrommer et al. 2008

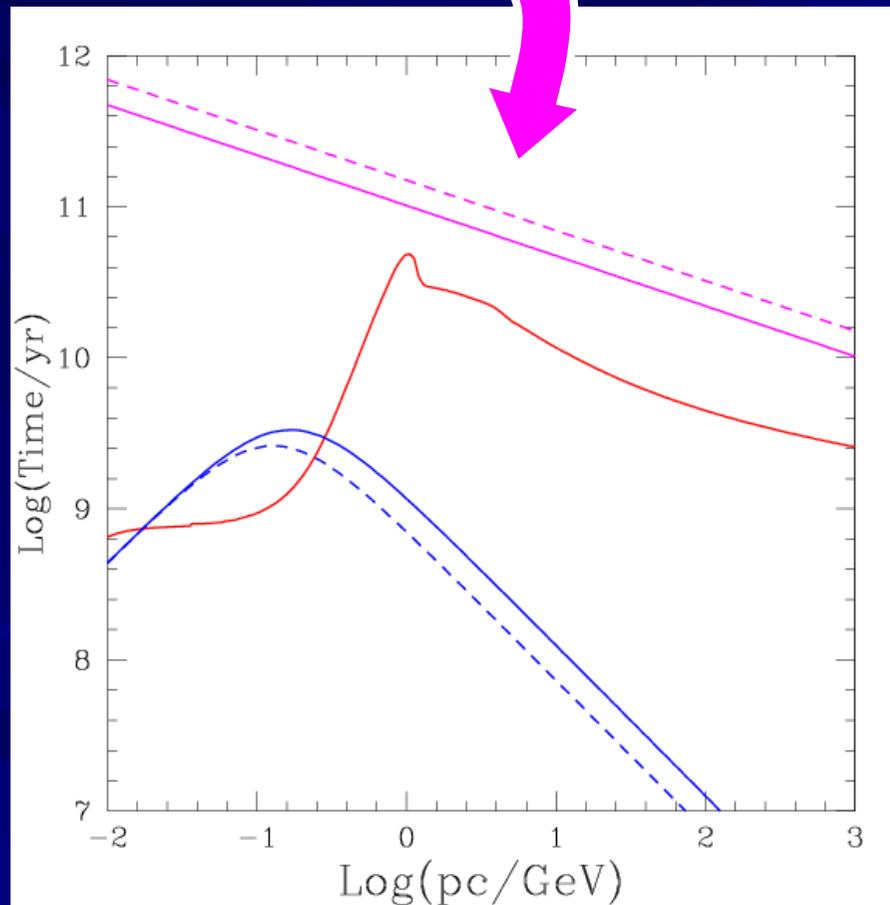
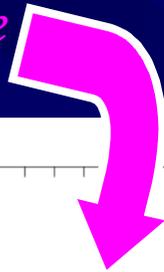


Kang & Jones 2007



# Cosmic Ray Physics & Confinement

*Diffusion time*

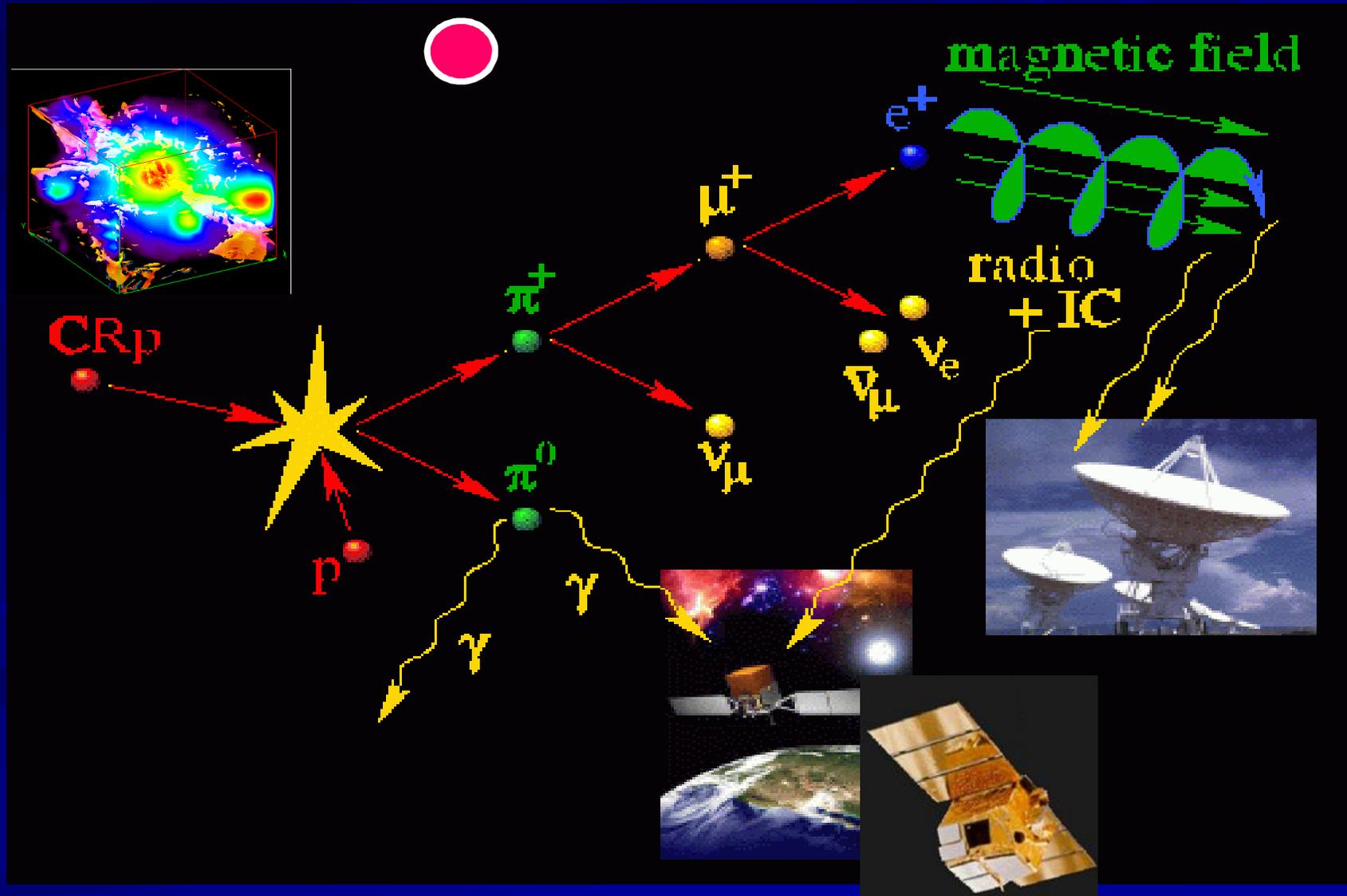


- CR protons are long living particles and are confined (Voelk et al 1996; Berezhinsky, Blasi, Ptuskin 1997)
- CR electrons are short living particles and accumulated at  $\gamma \approx 100-300$  (e.g., Sarazin 1999)

Blasi, Gabici, Brunetti 2007

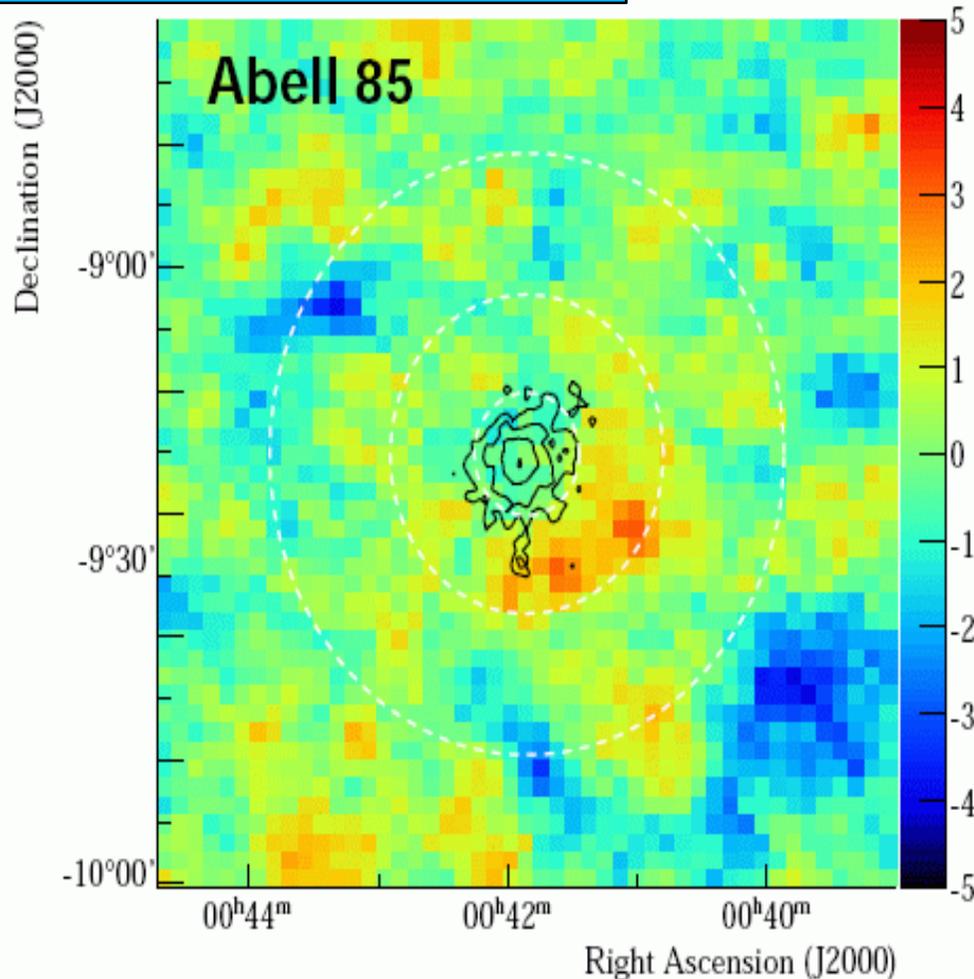
# Secondary Particles in the IGM

Dennison 1980; Blasi & Colafrancesco 1999; Pfrommer & Ensslin 2004;  
Brunetti & Blasi 2005; Wolfe & Melia 2007; Brunetti 2008

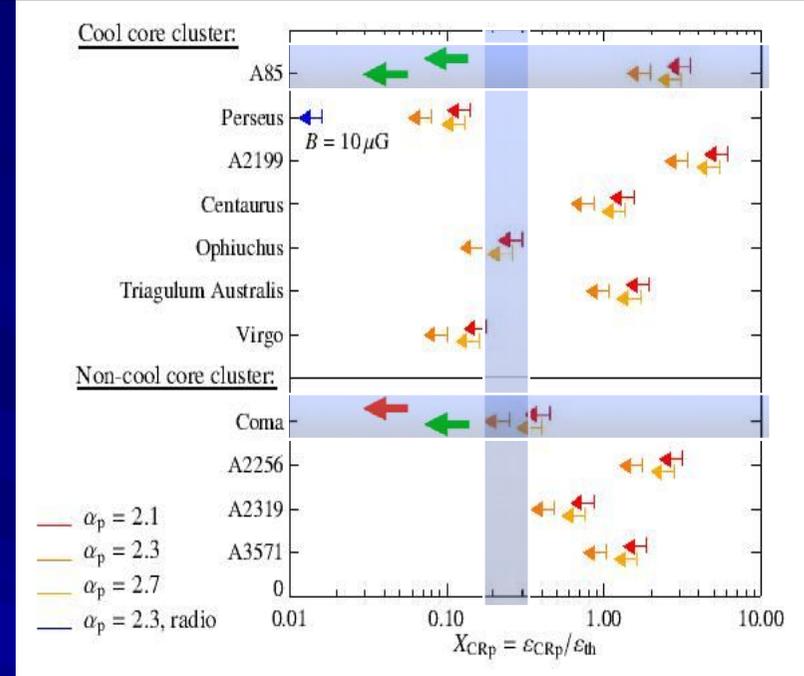


# CRp: Limits from gamma rays

Aharonian + al. 2008



Reimer +al. 2003; Pfrommer & Ensslin 2004



H.E.S.S.

A 85 :  $E_{cr}/E_{th} < 6-15\%$  (hard spectra)

Coma :  $E_{cr}/E_{th} < 12\%$

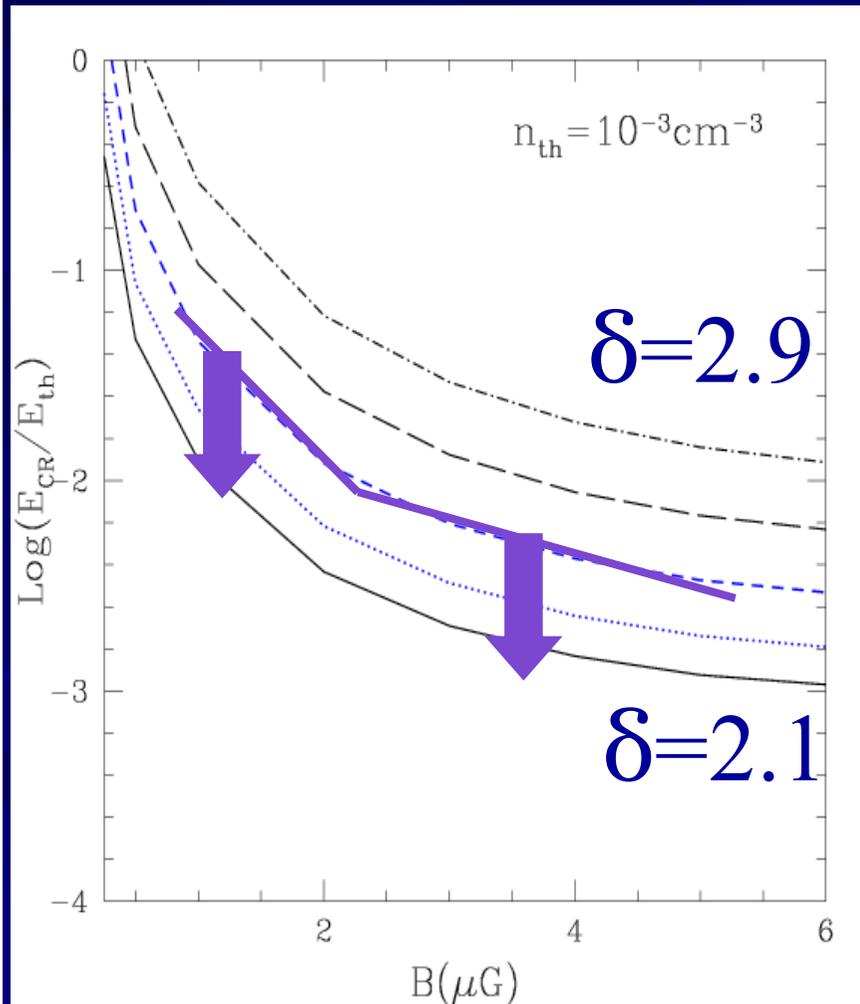
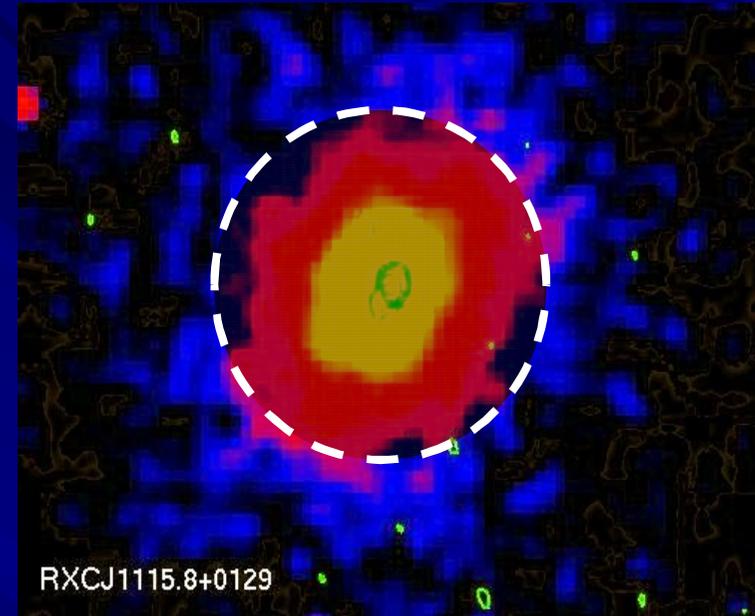
VERITAS (Perkins +al. 2008)

Coma :  $E_{cr}/E_{th} < 5\%$  (hard spectra)

# CRp: limits from Radio

Brunetti +al. 2007

Making use of clusters in the GMRT survey



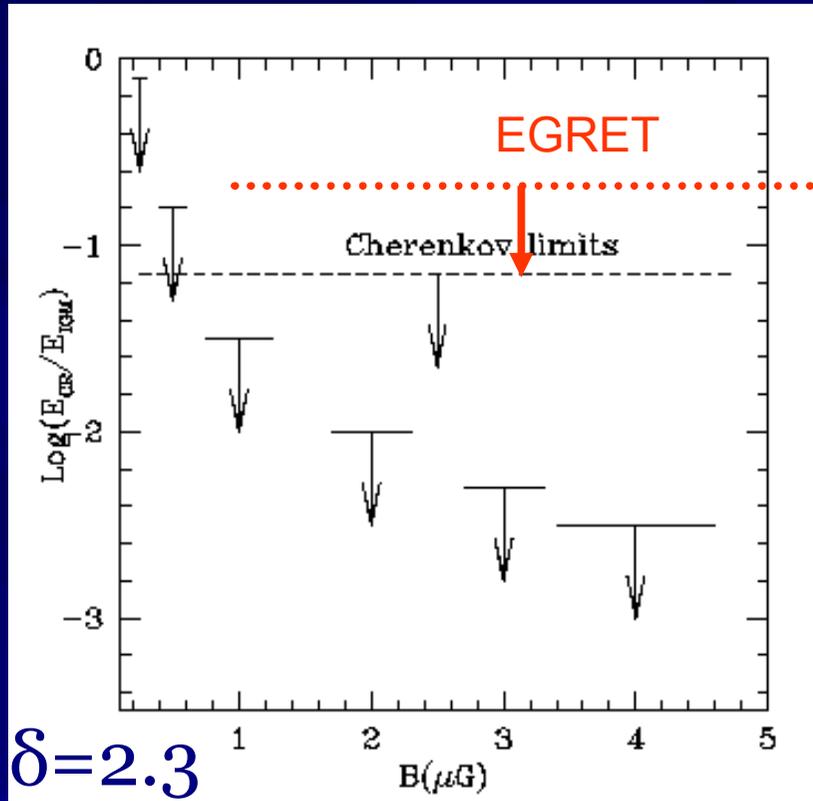
Assuming that secondary particles are injected in the IGM, their synchrotron emission should be smaller than upper limits to the diffuse radio emission.

limit on :  $B$  ,  $E_{CRp}$  ,  $\delta$

$$N(p) = K p^{-\delta}$$

# Limits for CR protons

Brunetti, Blasi, Cassano, Gabici 2008



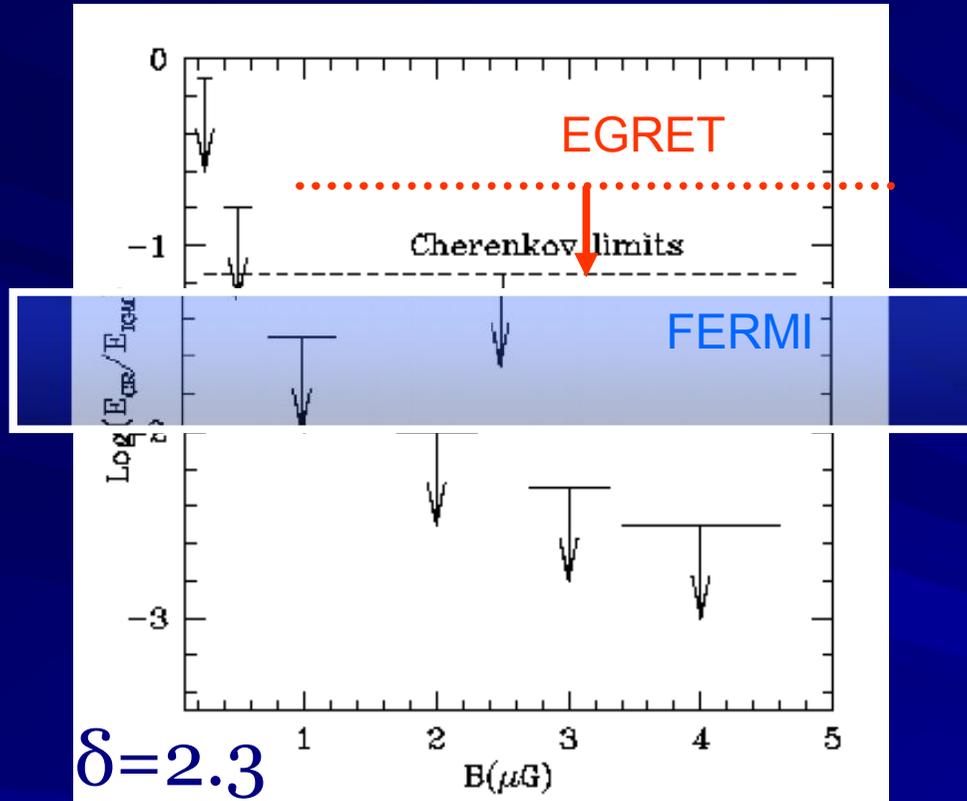
Reimer et al. 2003  
Reimer et al. 2004  
Pfrommer & Ensslin 2004  
Perkins et al. 2006  
Brunetti et al. 2007  
Brunetti et al. 2008  
Perkins et al. 2008  
Aharonian et al. 2008

In case of flat proton spectrum present limits constrain  $E_{\text{CR}} < \text{few \% } E_{\text{thermal}}$

Additional limits from cluster dynamics (e.g. Churazov et al. 2008) constrain  $E_{\text{CR}} + E_{\text{B}} + E_{\text{turb}}$  below 10%  $E_{\text{thermal}}$ .

# Limits for CR protons

Brunetti, Blasi, Cassano, Gabici 2008

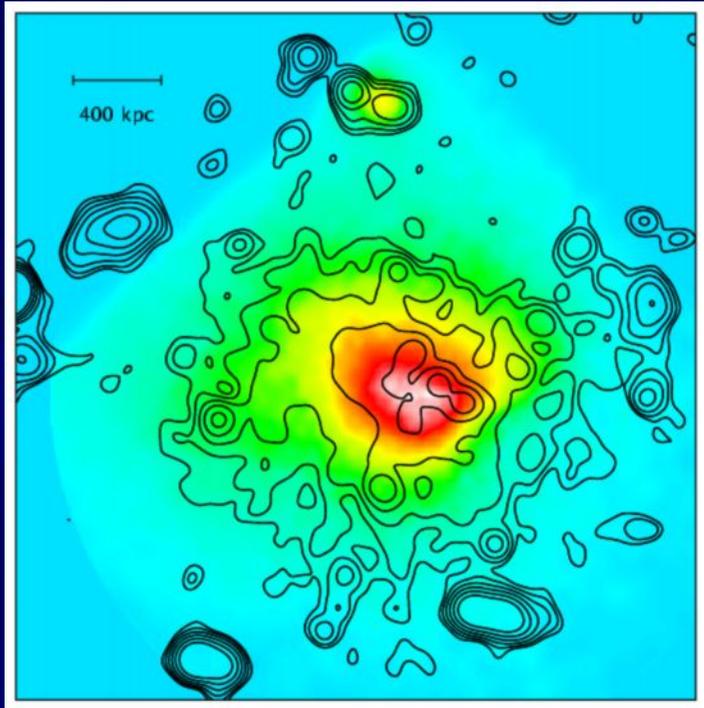


Reimer et al. 2003  
Reimer et al. 2004  
Pfrommer & Ensslin 2004  
Perkins et al. 2006  
Brunetti et al. 2007  
Brunetti et al. 2008  
Perkins et al. 2008  
Aharonian et al. 2008

In case of flat proton spectrum present limits constrain  $E_{\text{CR}} < \text{few \% } E_{\text{thermal}}$ .  
In case of flat spectra FERMI is expected to step into the region of the Radio limits, providing better constraints in case of steeper spectra.

Additional limits from cluster dynamics (e.g. Churazov et al. 2008) constrain  $E_{\text{CR}} + E_{\text{B}} + E_{\text{turb}}$  below 10%  $E_{\text{thermal}}$ .

# *Radio Halos as LABs for particle acceleration*



● **GeV electrons on Mpc scales**

●  **$\mu\text{G}$  magnetic fields on Mpc scales**

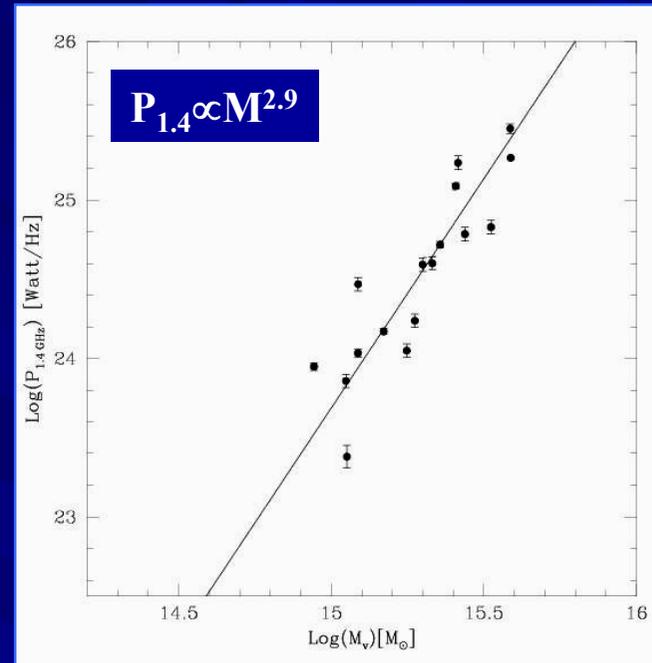
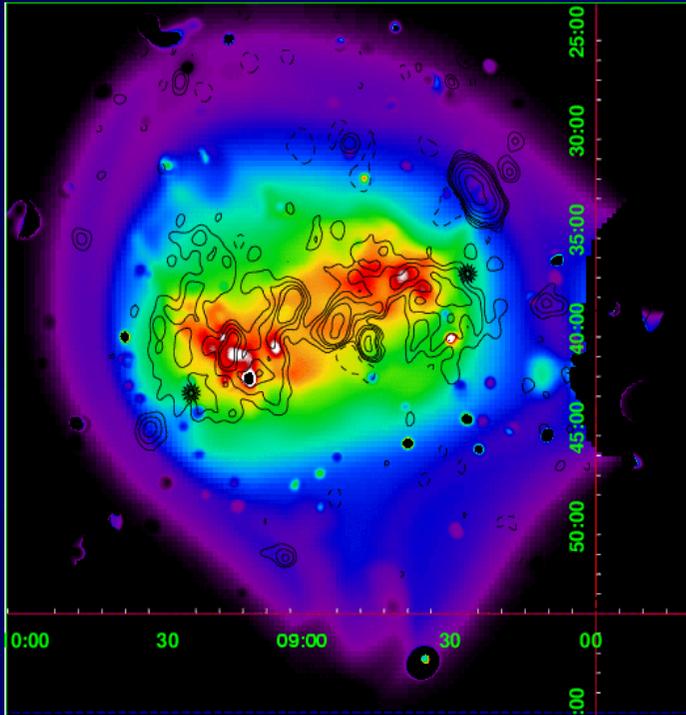
●  $T_{\text{diff}} (\sim 10^{10} \text{ yr}) \gg T_{\text{cool}} (\sim 10^8 \text{ yr})$

(Jaffe 1977)



*Looking at new physical processes  
Labs to study GC as particle accelerators*

# Radio Halos and cluster-cluster mergers



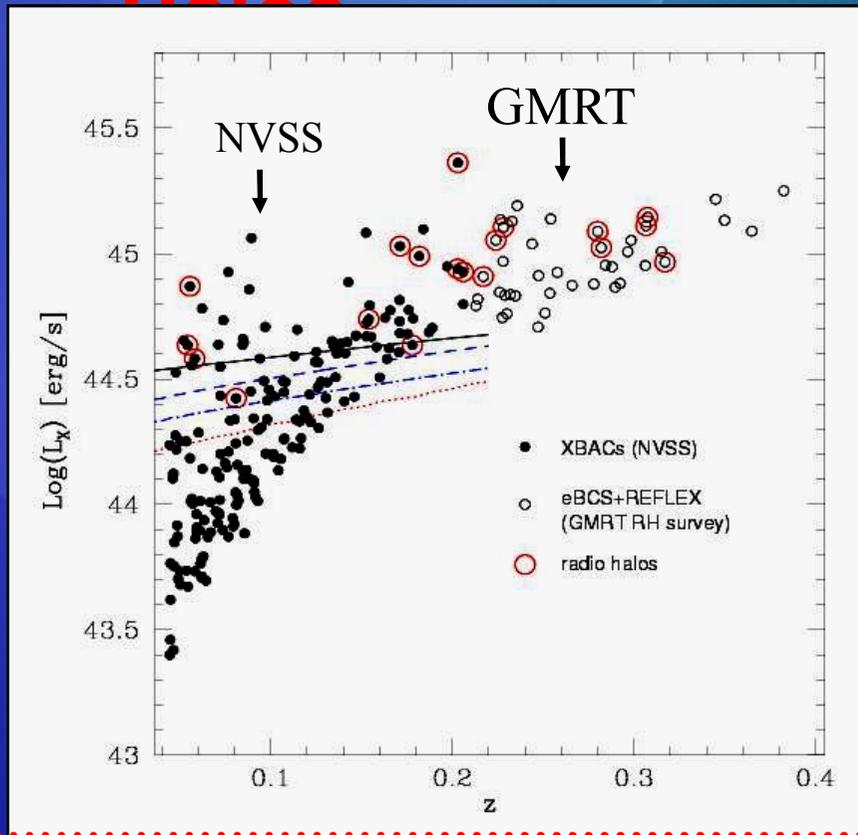
Connection with cluster mergers (e.g. Buote 2001, Schuecher et al. 2001, Markevitch et al. 2002, Boschini et al. 2003 Govoni et al. 2004)

The 1.4 GHz synchrotron radio power of GRH increases with the cluster mass ( $L_x, T$ ) (e.g. Liang 1999, Bacchi et al. 2003, Cassano et al. 2006)



*Gravitational - driven processes ?*

# The complex statistics of Radio Halos

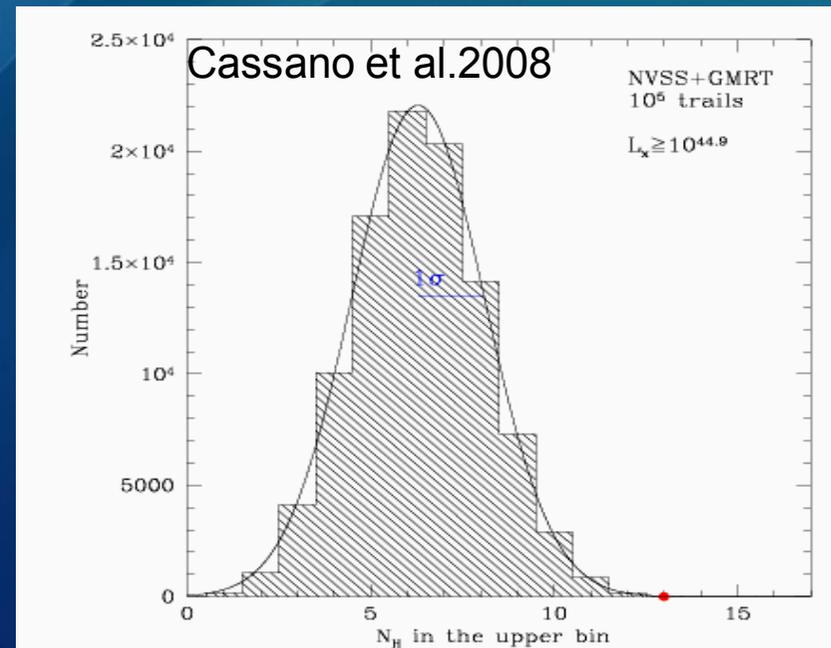
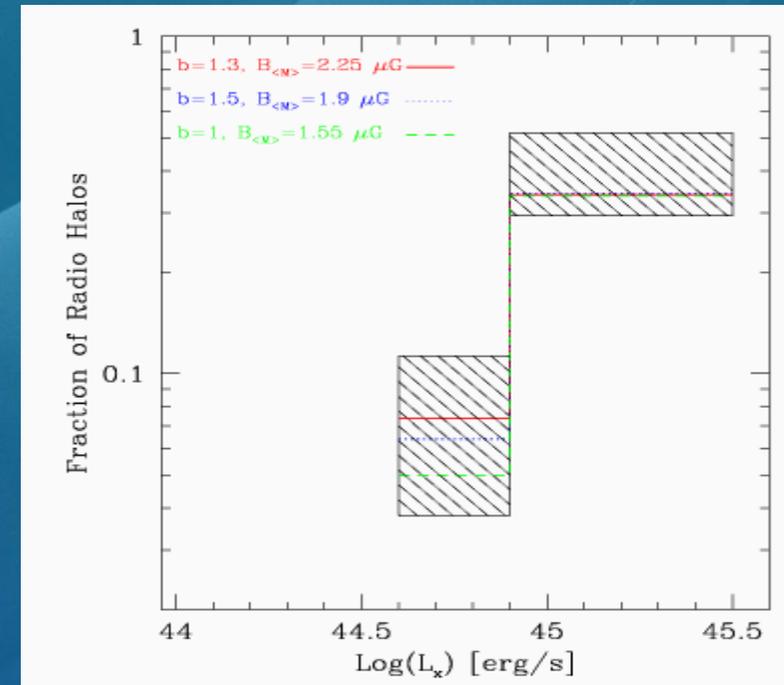


NVSS data (from *Giovannini et al. 1999*) and deep GMRT observations.

$0.41 \pm 0.11$  for  $L_x > 10^{44.9}$  erg/s

$0.08 \pm 0.04$  for  $L_x < 10^{44.9}$  erg/s

(*Venturi et al. 2007, 2008; Cassano et al. 2008*)



# The complex statistics of Radio Halos

## Halos

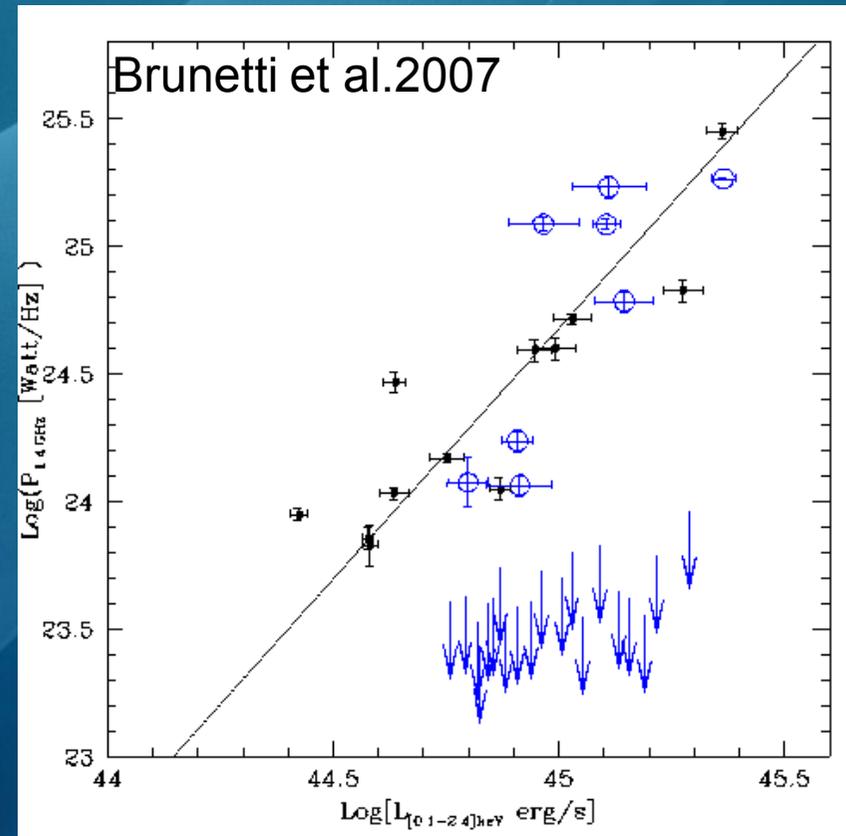
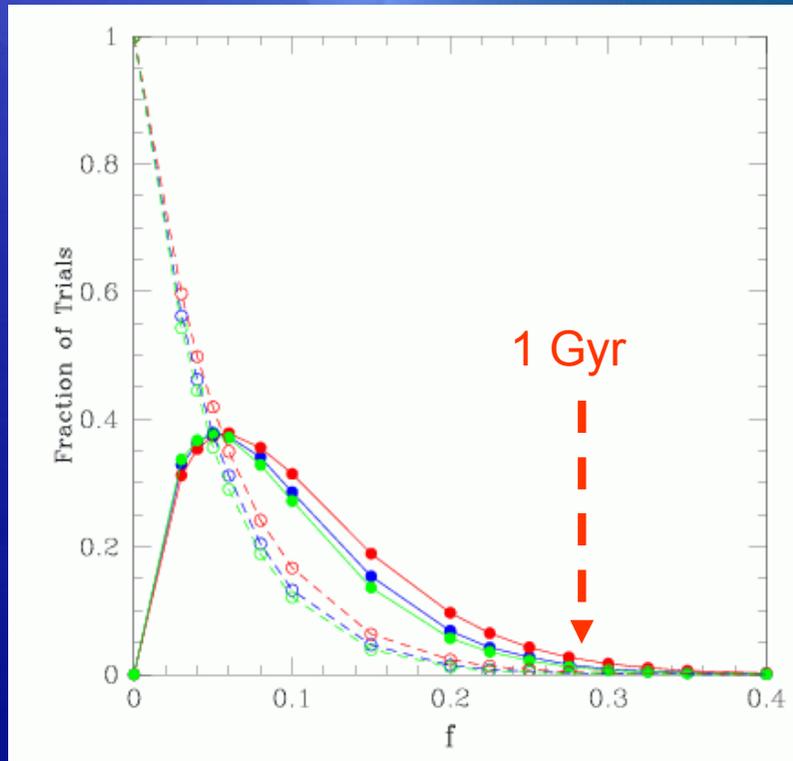
Connection with cluster mergers

(e.g. *Schuecher et al. 2001*, *Markevitch et al. 2002*, *Boschin et al. 2003* *Govoni et al. 2004*)

Which is the difference between RH-clusters and ULimits ?

Does non thermal emission evolve ?

Which time-scale ?



Magnetic field dissipation ?

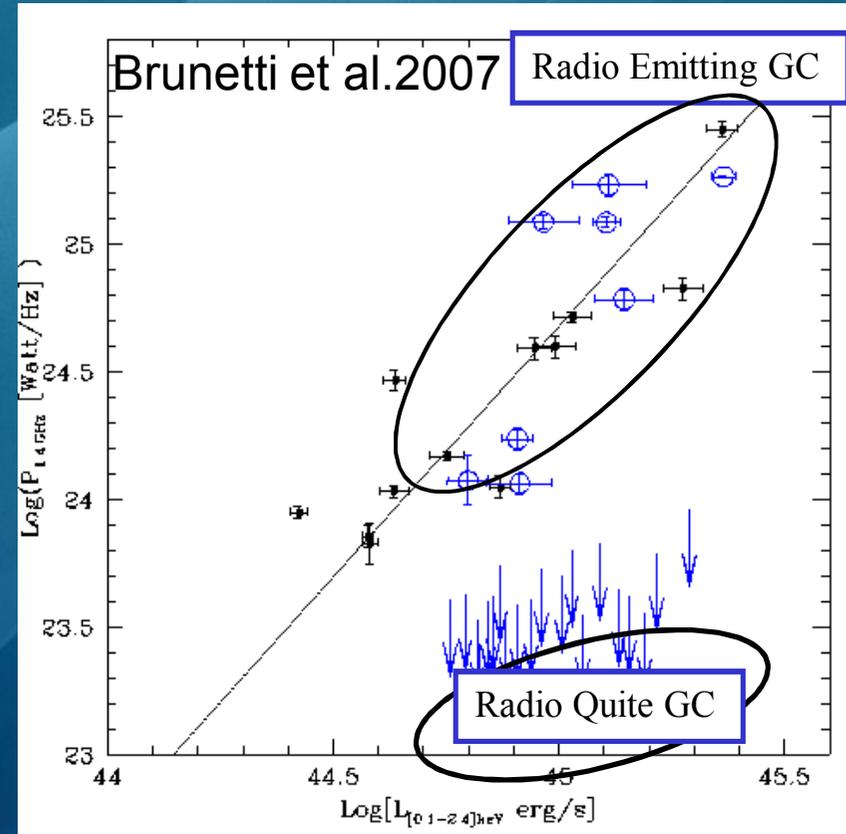
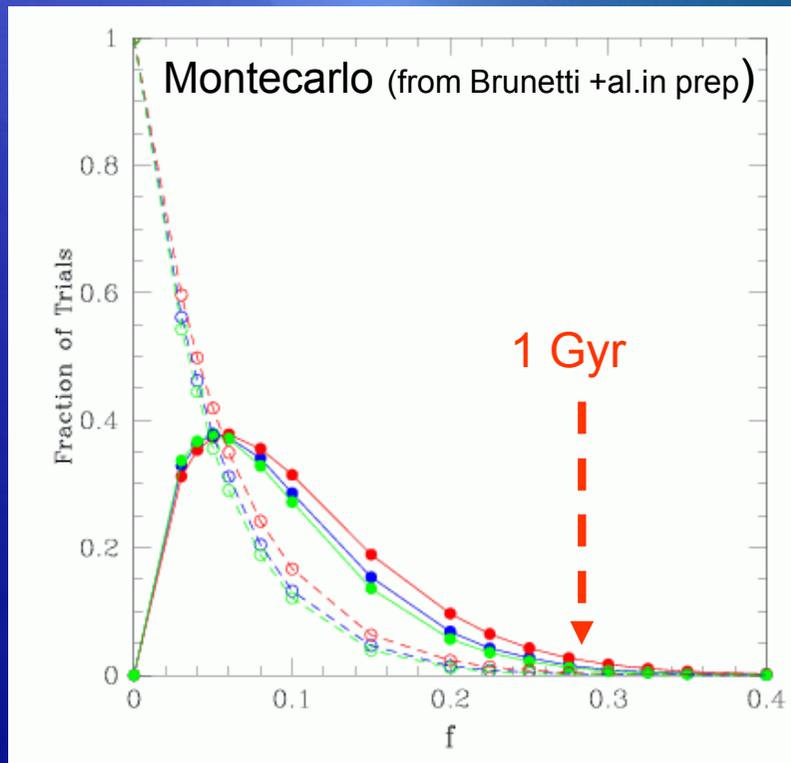
# The complex statistics of Radio Halos

## Halos

Connection with cluster mergers

(e.g. *Schuecher et al. 2001*, *Markevitch et al. 2002*, *Boschin et al. 2003* *Govoni et al. 2004*)

Does non thermal emission evolve?  
Which time-scale?



Magnetic field dissipation in the IGM must happen in  $\ll 1$  Gyr

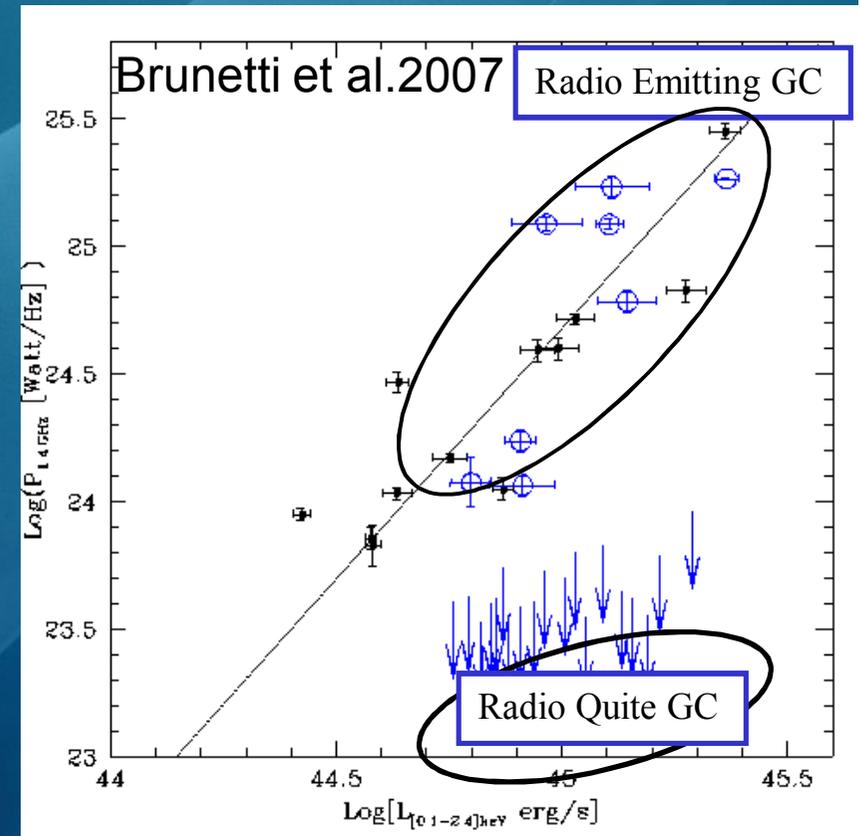
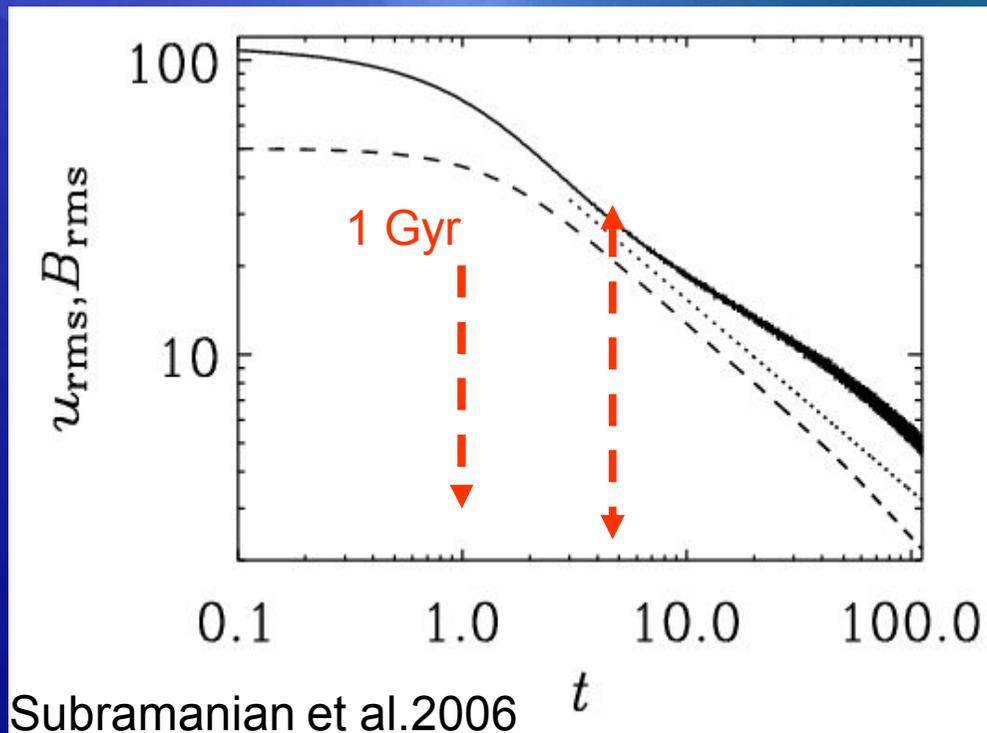
# The complex statistics of Radio Halos

## Halos

Connection with cluster mergers

(e.g. *Schuecher et al. 2001*, *Markevitch et al. 2002*, *Boschin et al. 2003* *Govoni et al. 2004*)

Does non thermal emission evolve?  
Which time-scale?

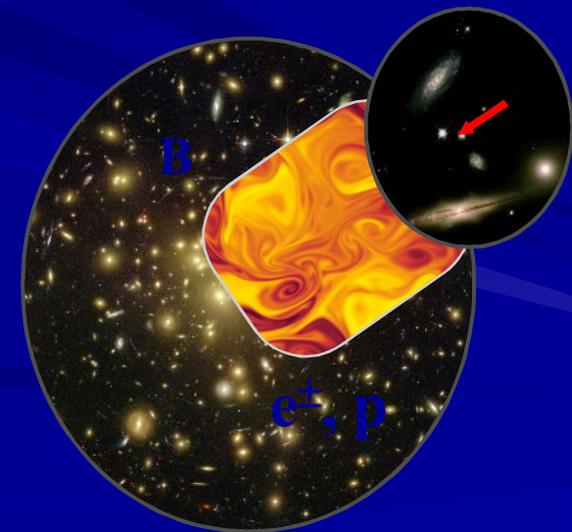
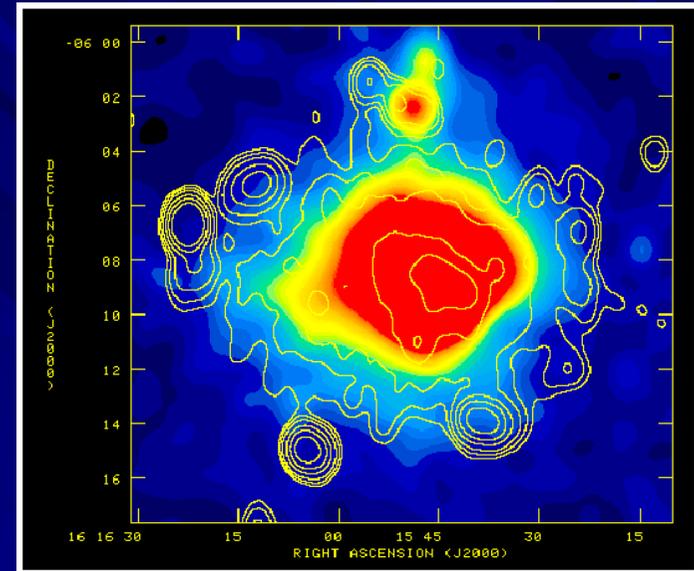


Thus the "bi-modality" is due to the evolution (acceleration and cooling) of the **emitting electrons**

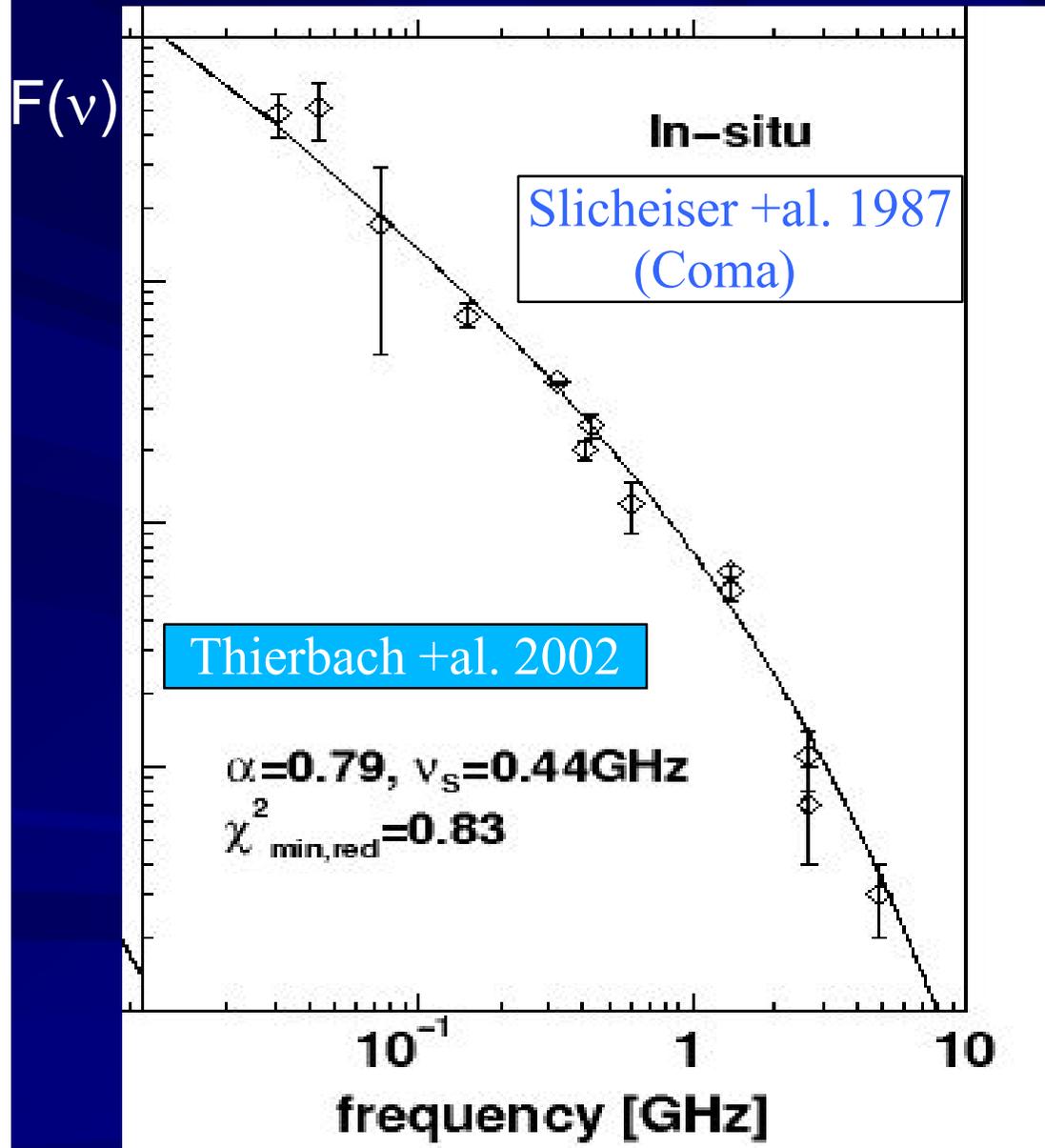
# Origin of the emitting electrons

***In situ re-acceleration of primary & secondary particles by cluster MHD turbulence*** (e.g., *Brunetti et al. 2001, 2004; Petrosian 2001; Ohno et al. 2002; Fujita et al. 2003; Brunetti & Blasi 2005; Cassano & Brunetti 2005; Brunetti & Lazarian 2007; Petrosian & Bykov 2008*)

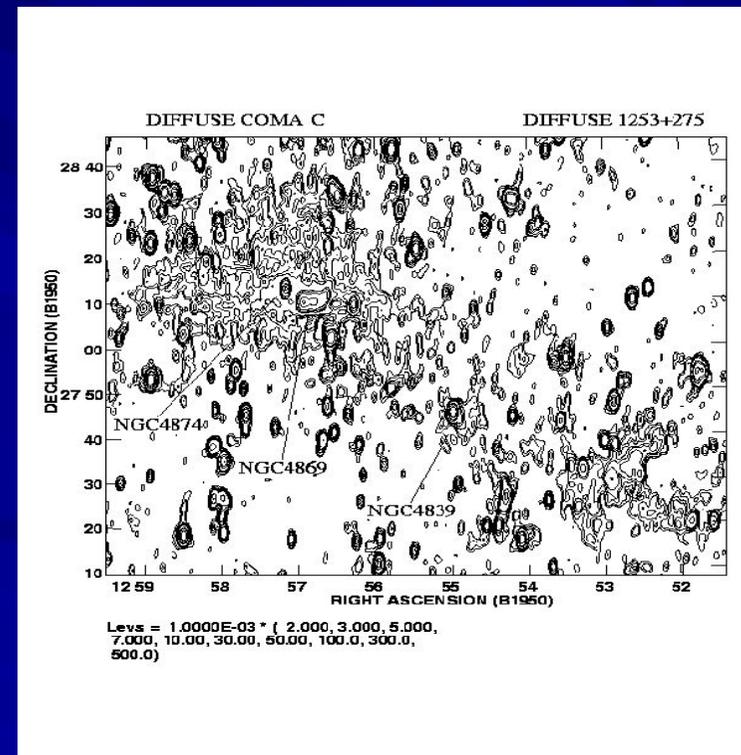
- *Radio halo – merger connection*
- *Fast dissipation (evolution) of synchrotron emission (CRe cooling)*



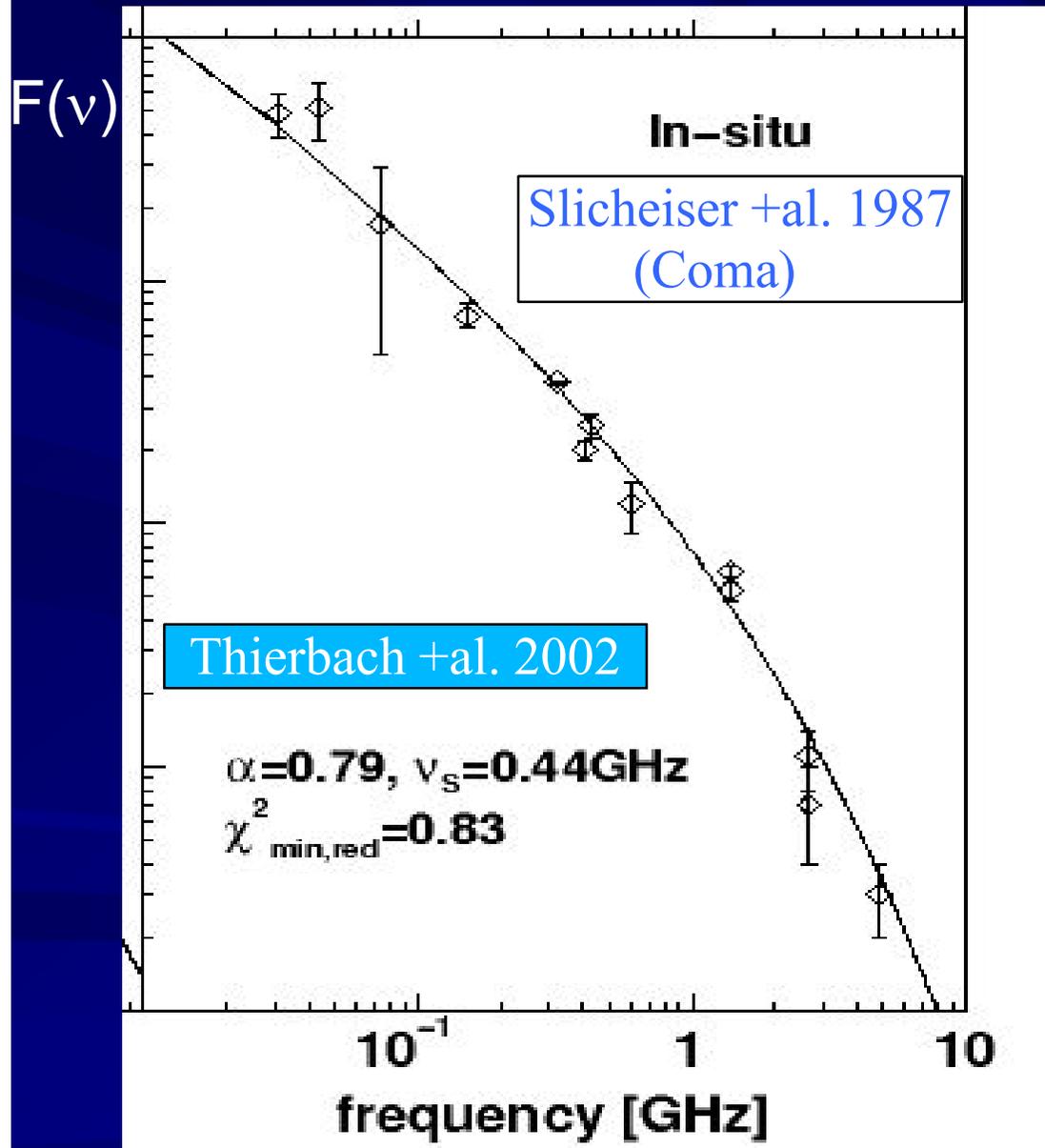
# Radio Halos : are they generated by "inefficient" mechanism of CRe acceleration ?



Evidence of break in the synchrotron spectrum



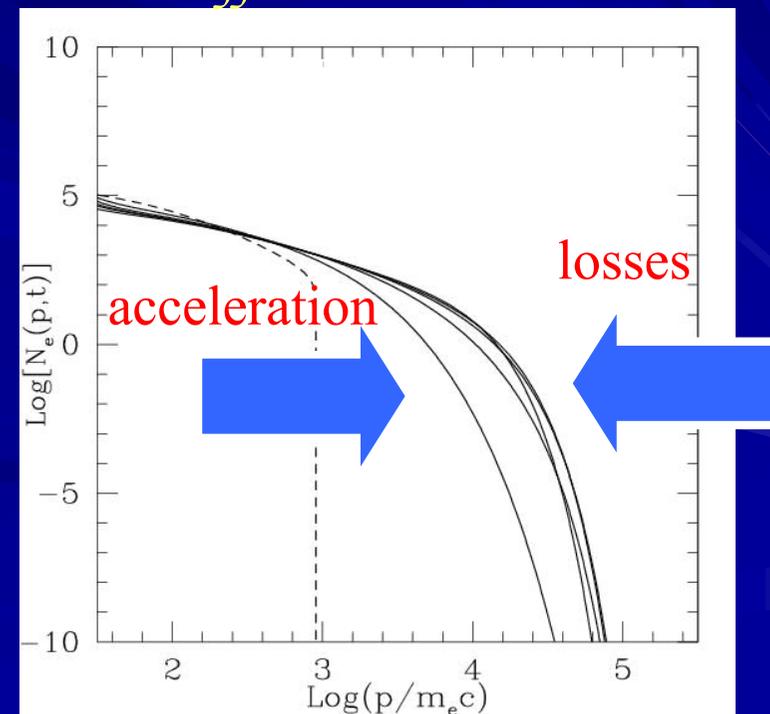
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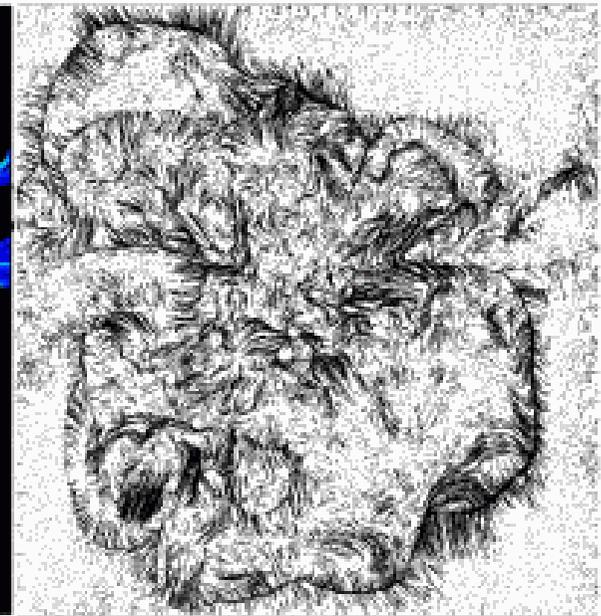
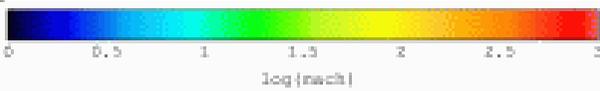
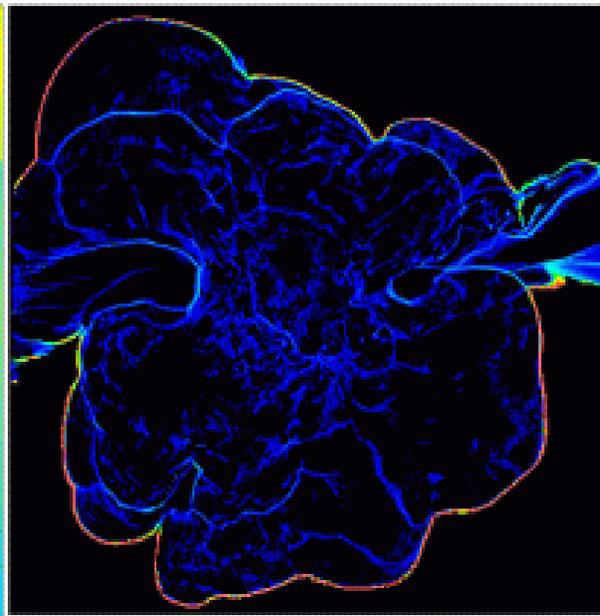
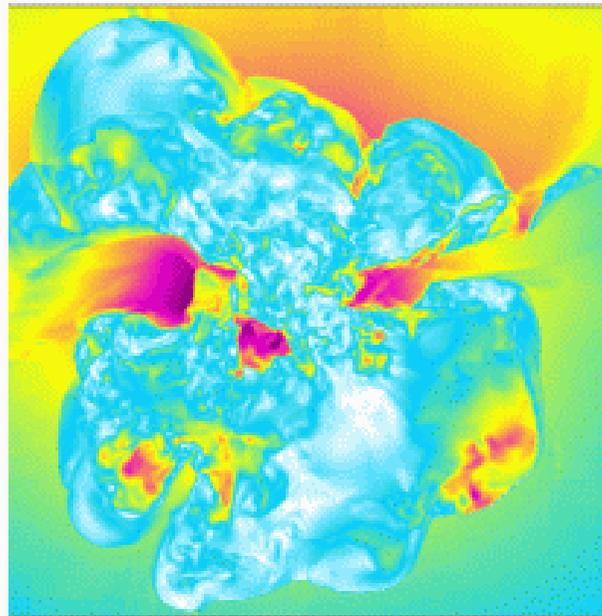
Evidence of break in the spectrum of the emitting electrons at energies of few GeV



*Acceleration mechanism not efficient !*



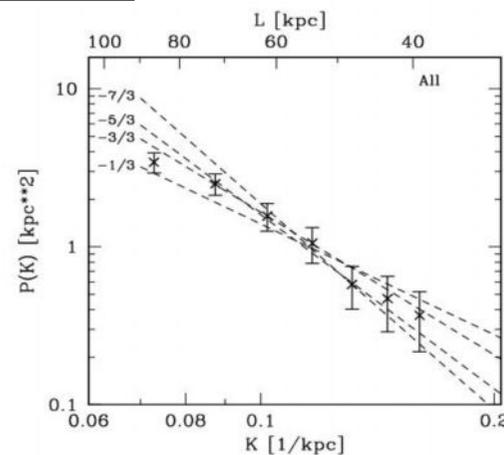
# Turbulence in galaxy clusters & cluster-mergers



Turbulent Velocity Field

Vazza +al. in prep.

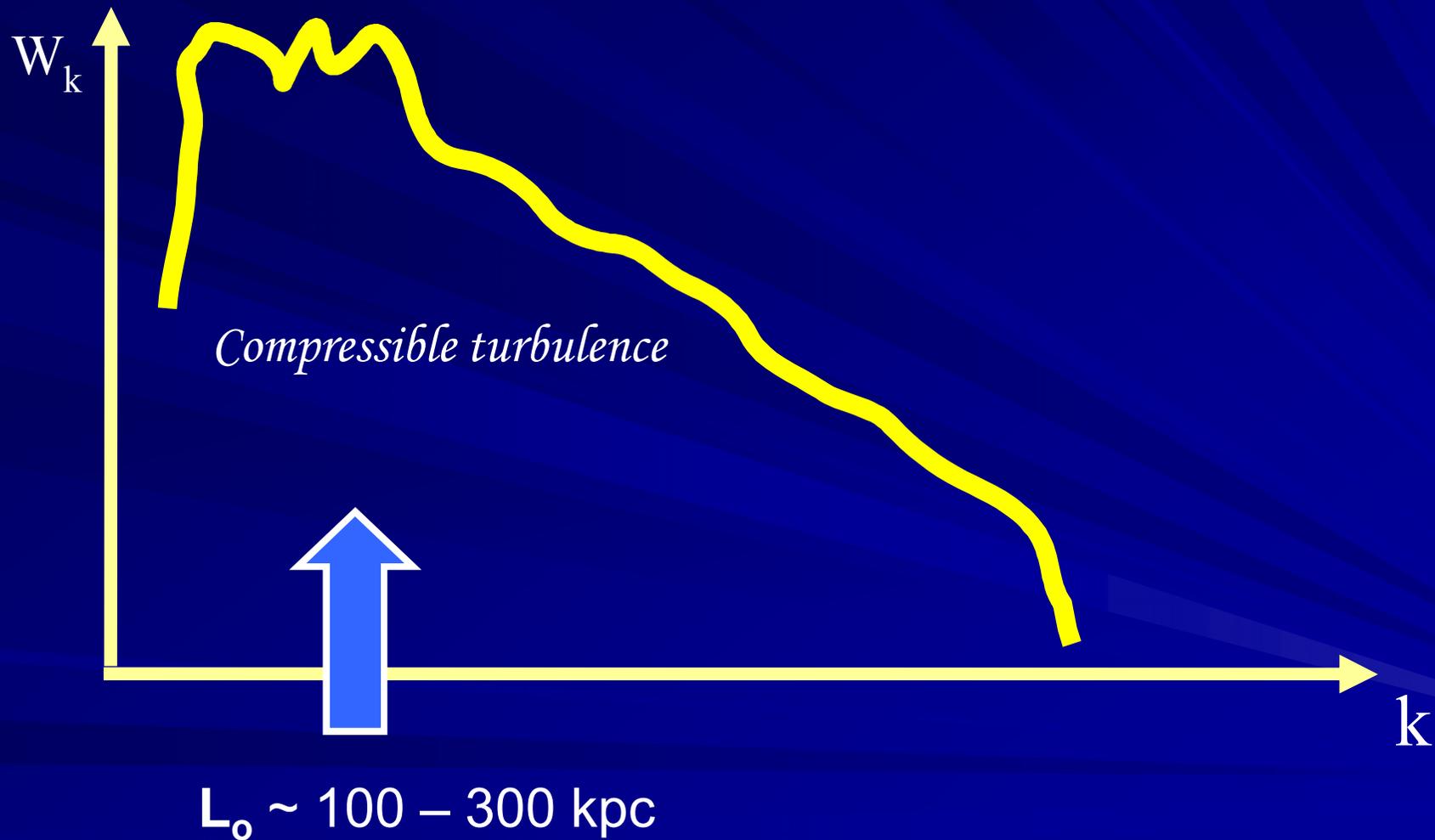
Schuecker +al. (2004)



Bryan & Norman 1998;  
 Ricker & Sarazin 2001;  
 Sunyaev et al. 2003;  
 Cassano & Brunetti 2005  
 Dolag et al. 2005;  
 Vazza et al. 2006;  
 Nagai et al. 2007;  
 Brunetti & Lazarian 2007;  
 Iapichino & Niemeyer 2008

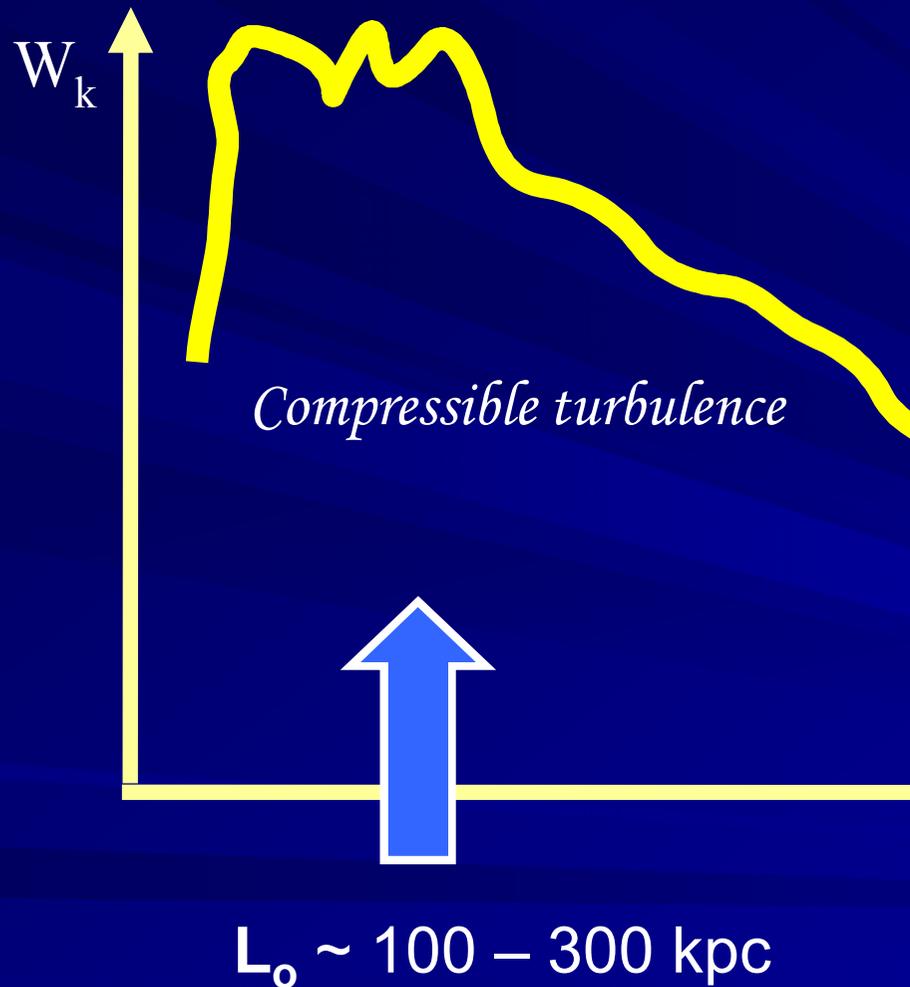
# Basics of turbulence in the ICM

Brunetti & Lazarian 2007



# Basics of turbulence in the ICM

Brunetti & Lazarian 2007



$$L_0 \sim 100 - 300 \text{ kpc}$$

$$V_0 \sim 500 - 1000 \text{ km/s}$$

$$c_s \sim 1200 - 1800 \text{ km/s}$$

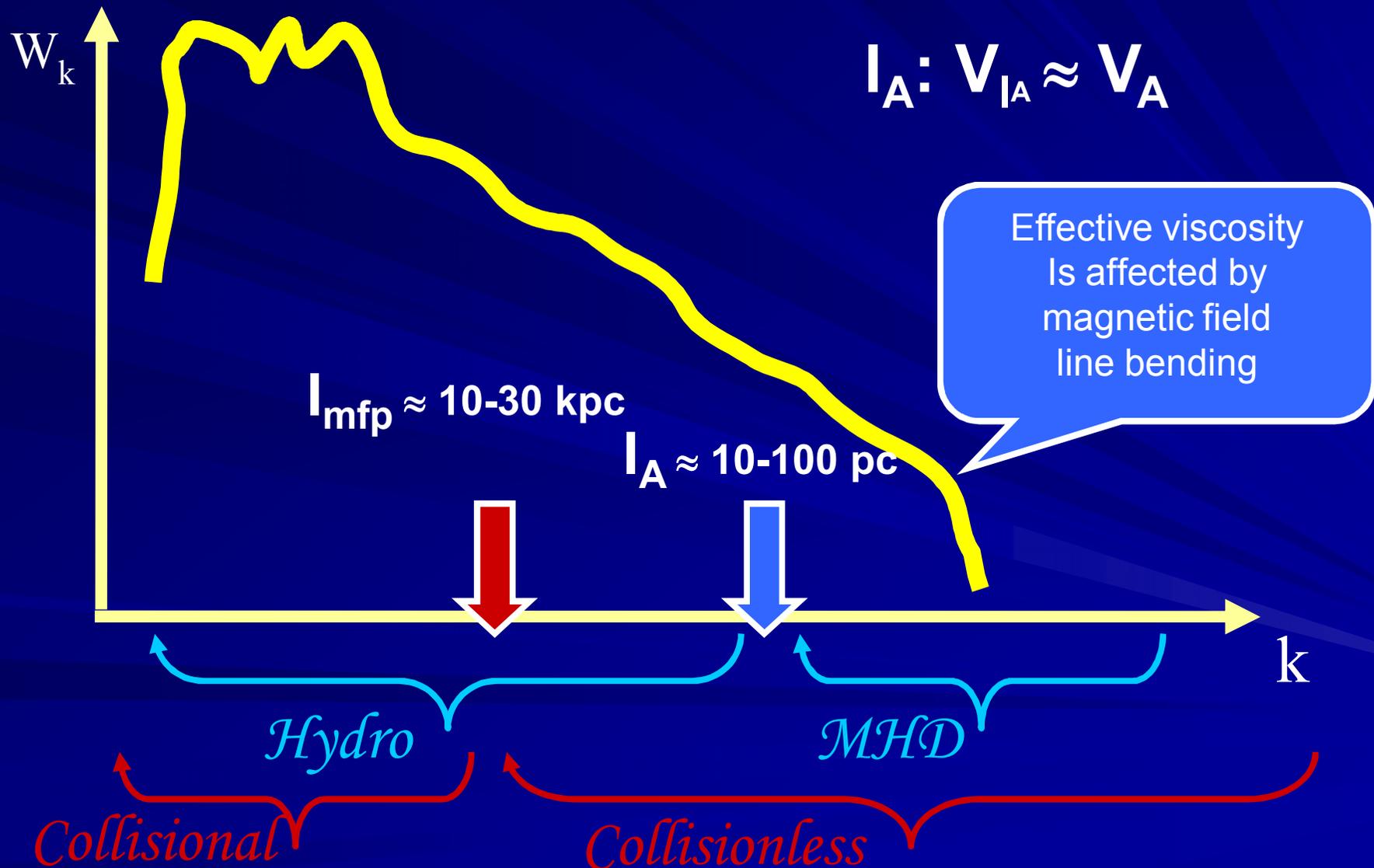
$$V_A \sim 30 - 100 \text{ km/s}$$

*Sub-sonic Turbulence*

*Super-Alfvénic Turbulence*

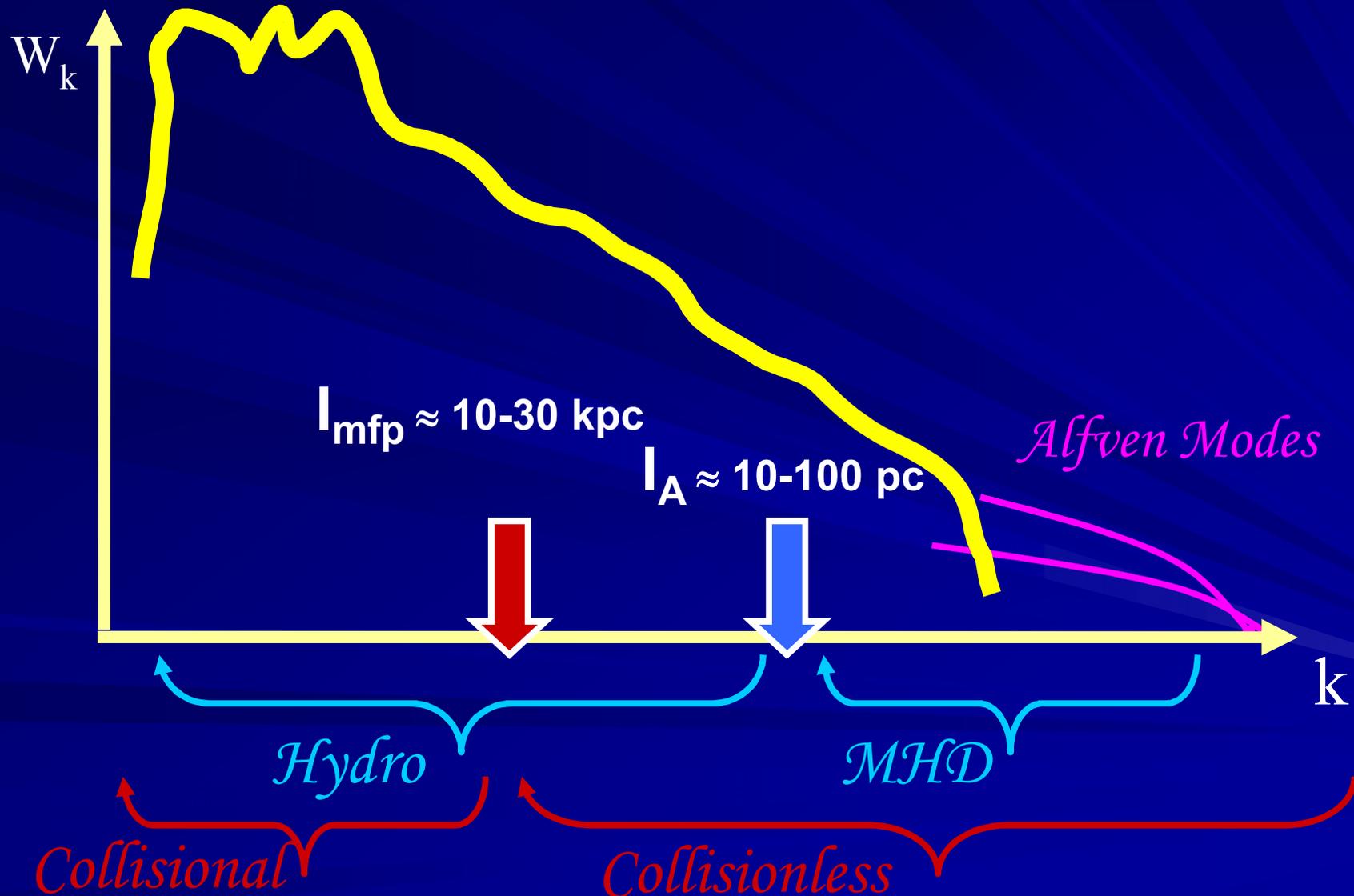
# Basics of turbulence in the ICM

Brunetti & Lazarian 2007



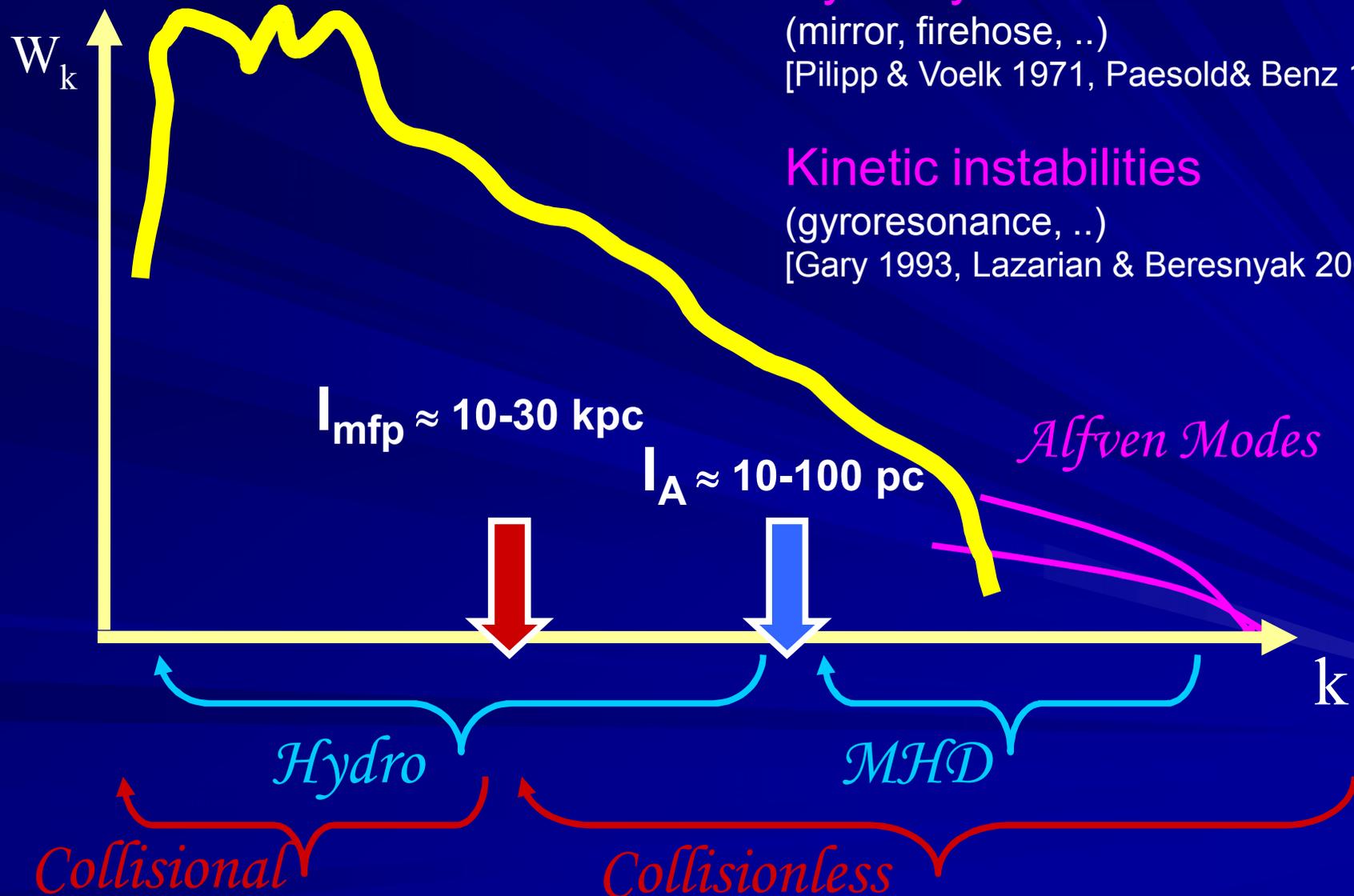
# Basics of turbulence in the ICM

Brunetti & Lazarian 2007



# Basics of turbulence in the ICM

Brunetti & Lazarian 2007



Hydrodynamic instabilities

(mirror, firehose, ..)

[Pilipp & Voelk 1971, Paesold & Benz 1999]

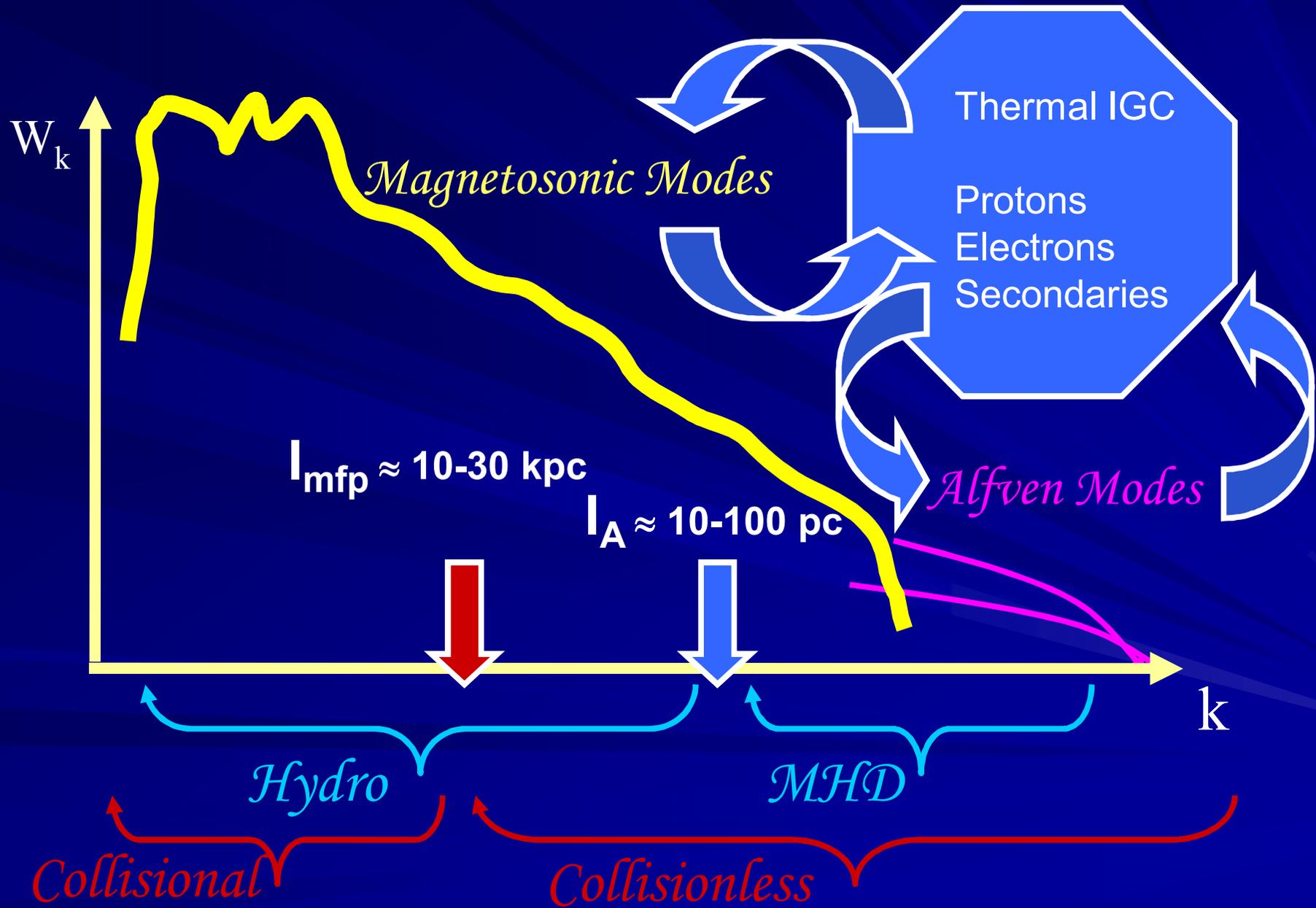
Kinetic instabilities

(gyroresonance, ..)

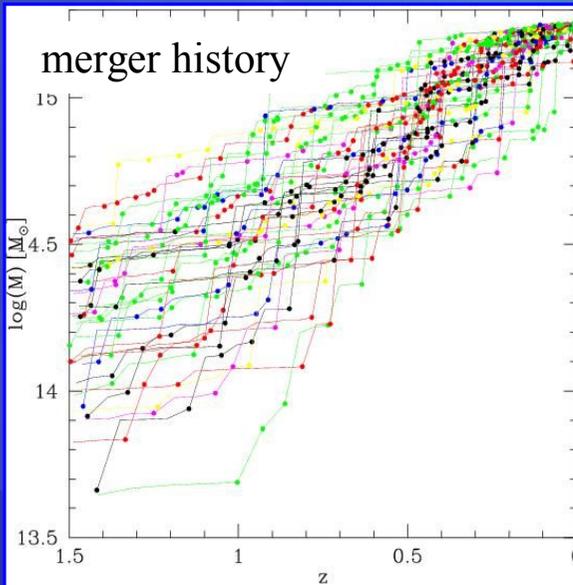
[Gary 1993, Lazarian & Beresnyak 2006]

*Alfven Modes*

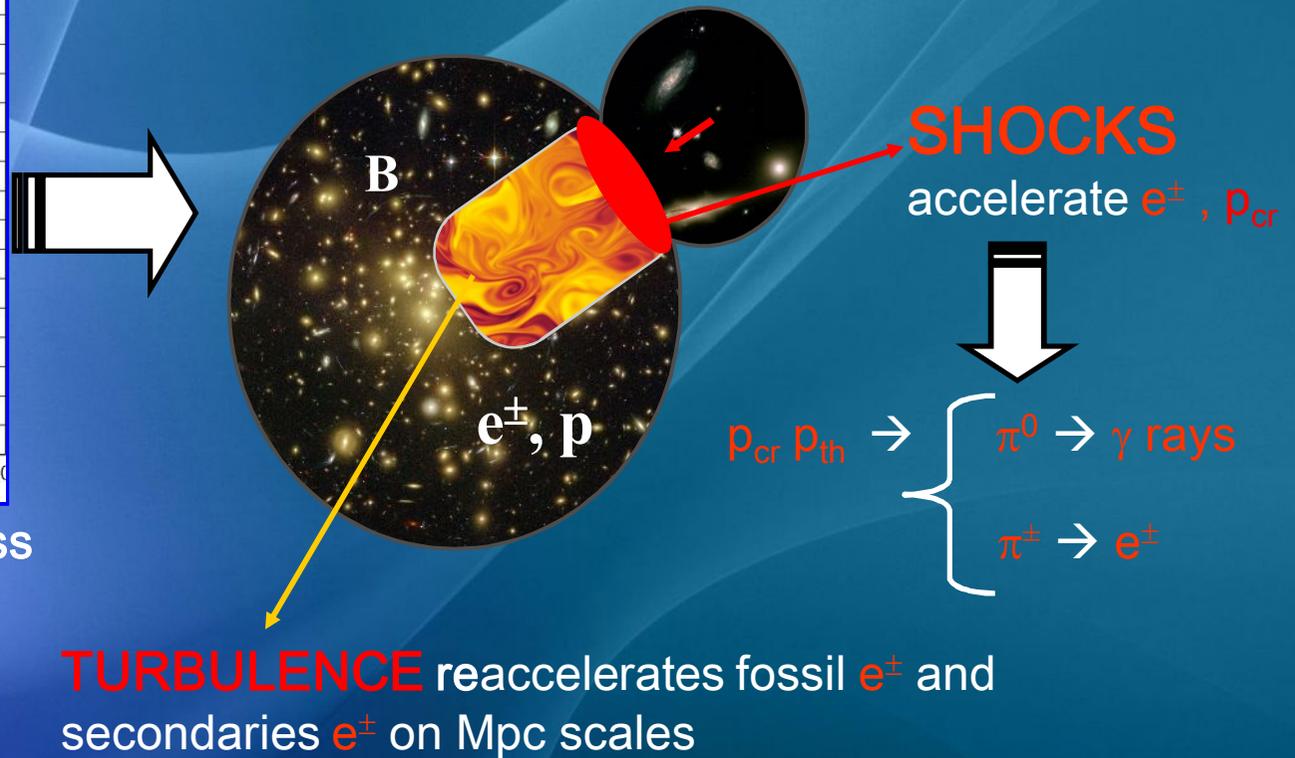
# Basics of turbulence in the ICM



# The general picture

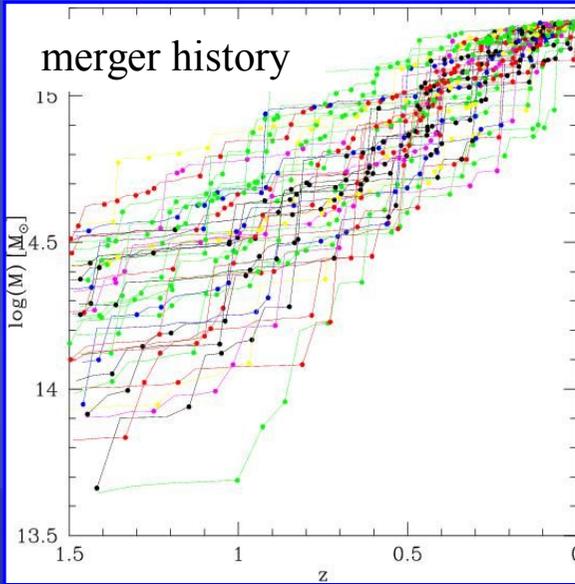


clusters increase their mass via merger with smaller subclusters

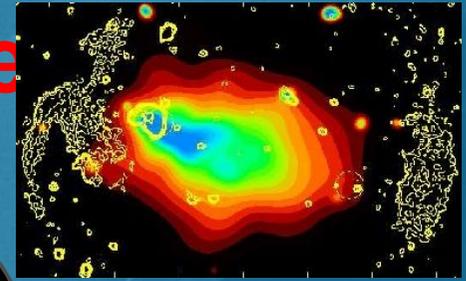
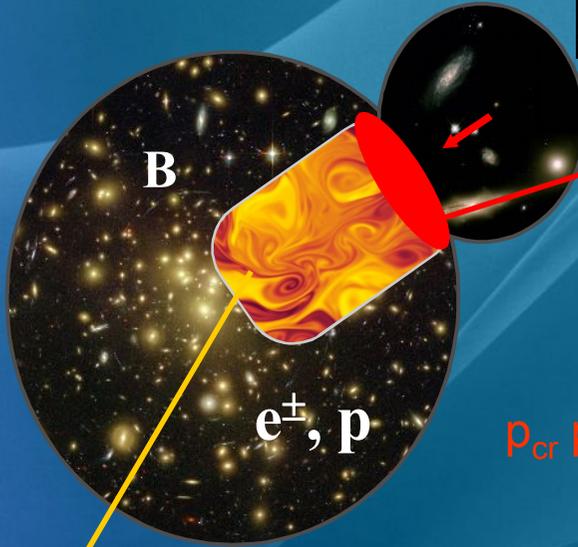
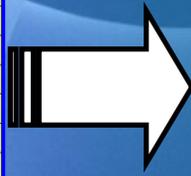


**TURBULENCE** reaccelerates fossil  $e^{\pm}$  and secondaries  $e^{\pm}$  on Mpc scales

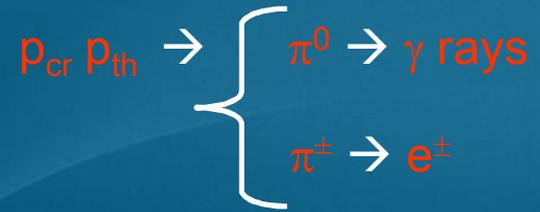
# The general picture



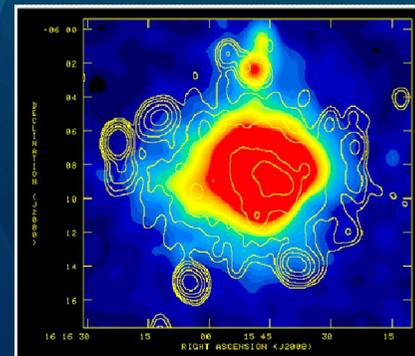
clusters increase their mass via merger with smaller subclusters



**SHOCKS**  
accelerate  $e^{\pm}, p_{cr}$



**TURBULENCE** reaccelerates fossil  $e^{\pm}$  and secondaries  $e^{\pm}$  on Mpc scales



# Alfvenic: results

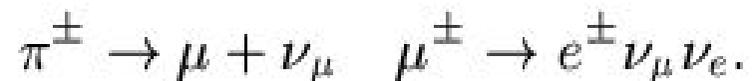
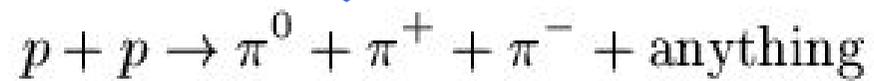
$n_{th}, T, B_o, N_p(p,0)$

$I(k)$

# Alfvenic: results

$n_{th}, T, B_0, N_p(p,0)$

$I(k)$

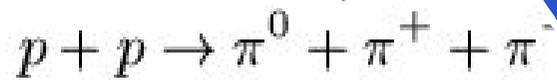


# Alfvenic: results

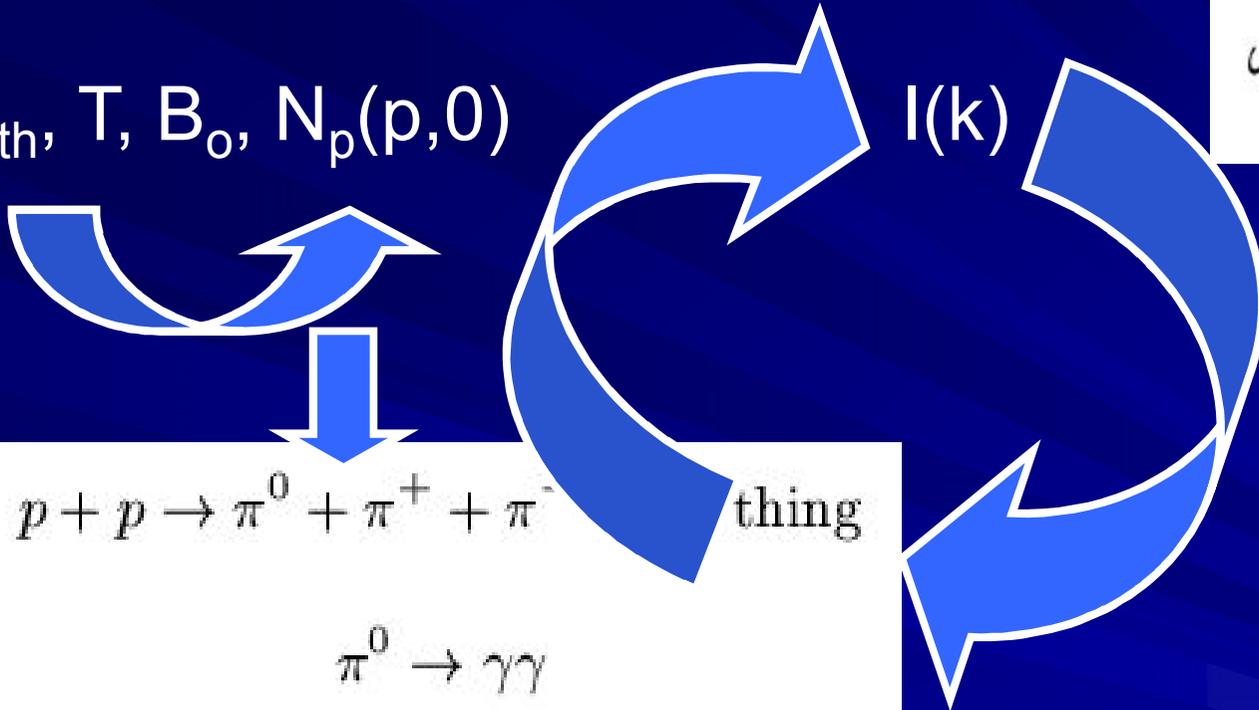
$n_{th}, T, B_o, N_p(p,0)$

$I(k)$

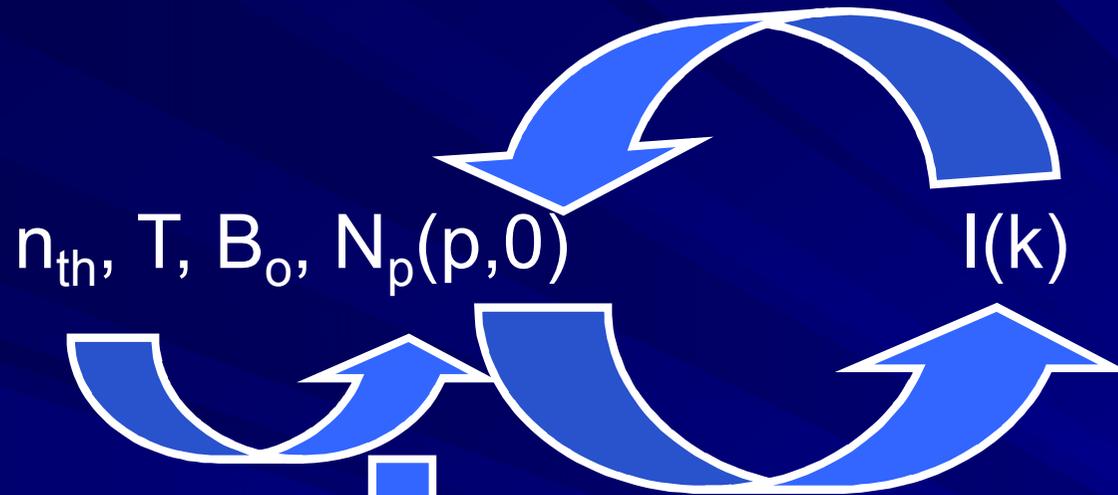
$$\omega - k_{\parallel} v_{\parallel} - n \frac{\Omega_o}{\gamma} = 0$$



thing



# Alfvenic: results



$$\omega - k_{\parallel} v_{\parallel} - n \frac{\Omega_o}{\gamma} = 0$$

$p + p \rightarrow \pi^0 + \pi^+ + \pi^- + \text{anything}$

$\pi^0 \rightarrow \gamma\gamma$

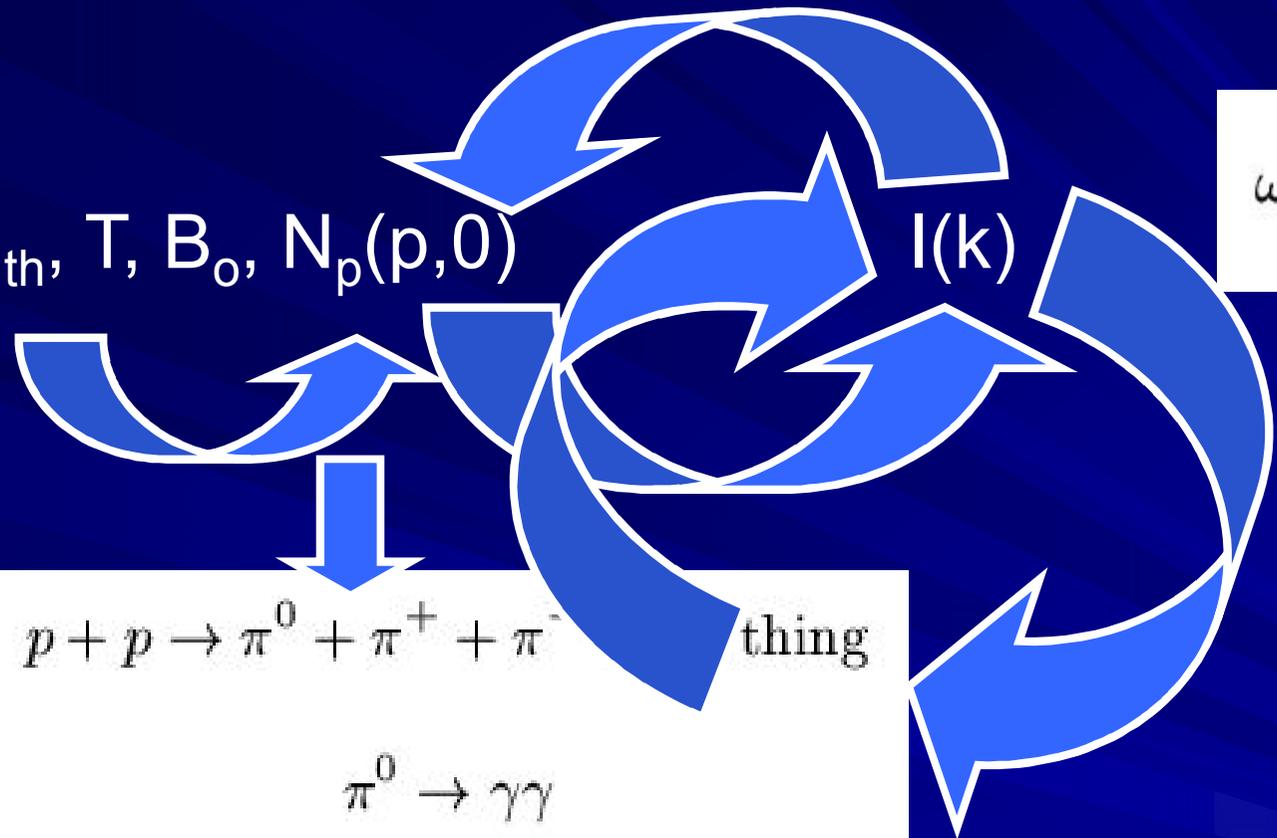
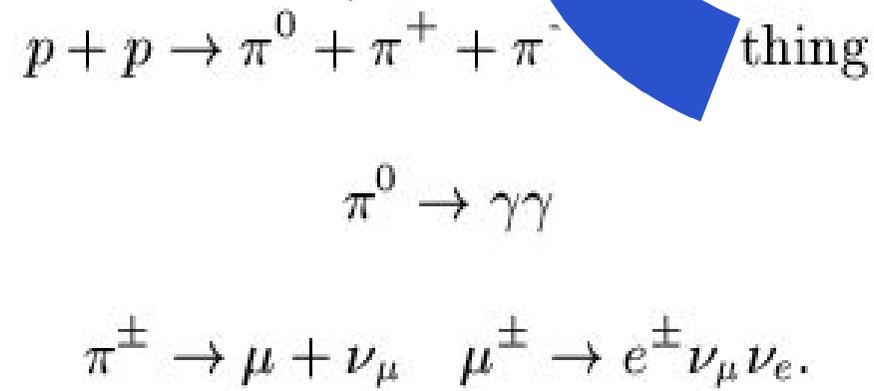
$\pi^{\pm} \rightarrow \mu + \nu_{\mu} \quad \mu^{\pm} \rightarrow e^{\pm} \nu_{\mu} \nu_e.$

# Alfvenic: results

$n_{th}, T, B_o, N_p(p,0)$

$I(k)$

$$\omega - k_{\parallel} v_{\parallel} - n \frac{\Omega_o}{\gamma} = 0$$



# Stochastic Particle Acceleration (formalism)

Brunetti +al. 2004, Brunetti & Blasi 2005, Brunetti +al. 2009

## Electrons/Positrons

$$\frac{\partial N_e(p, t)}{\partial t} = \frac{\partial}{\partial p} \left( N_e(p, t) \left[ \left( \frac{dp}{dt} \right)_{\text{rad}} + \left( \frac{dp}{dt} \right)_i - \frac{2}{p} D_{pp} \right] \right) + \frac{\partial}{\partial p} \left( D_{pp} \frac{\partial N_e(p, t)}{\partial p} \right) + Q_e(p, t)$$

## Protons

$$\frac{\partial N_p(p, t)}{\partial t} = \frac{\partial}{\partial p} \left( N_p(p, t) \left[ \left( \frac{dp}{dt} \right)_i - \frac{2}{p} D_{pp} \right] \right) + \frac{\partial}{\partial p} \left( D_{pp} \frac{\partial N_p(p, t)}{\partial p} \right) + Q_p(p, t)$$

$Q_e$ : secondaries from (CR)p-p collisions

## Waves

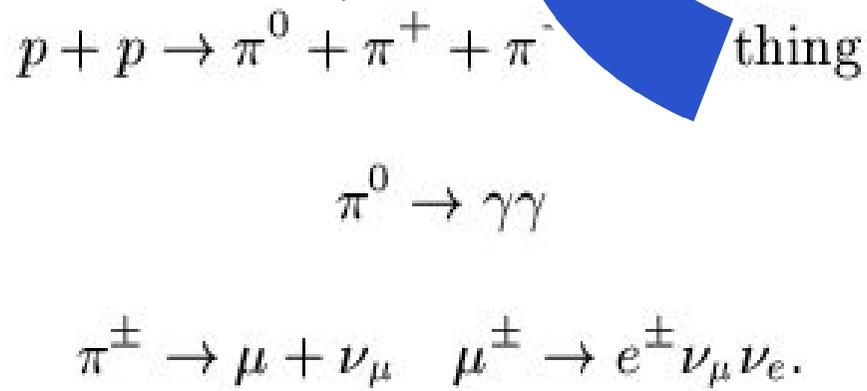
$$\frac{\partial \mathcal{W}(k, t)}{\partial t} = \frac{\partial}{\partial k} \left( k^2 D_{kk} \frac{\partial}{\partial k} \left( \frac{\mathcal{W}(k, t)}{k^2} \right) \right) - \sum_i \Gamma_i(k, t) \mathcal{W}(k, t) + I(k, t)$$

most could be with CR protons

# Alfvenic: results

$n_{th}, T, B_0, N_p(p,0)$

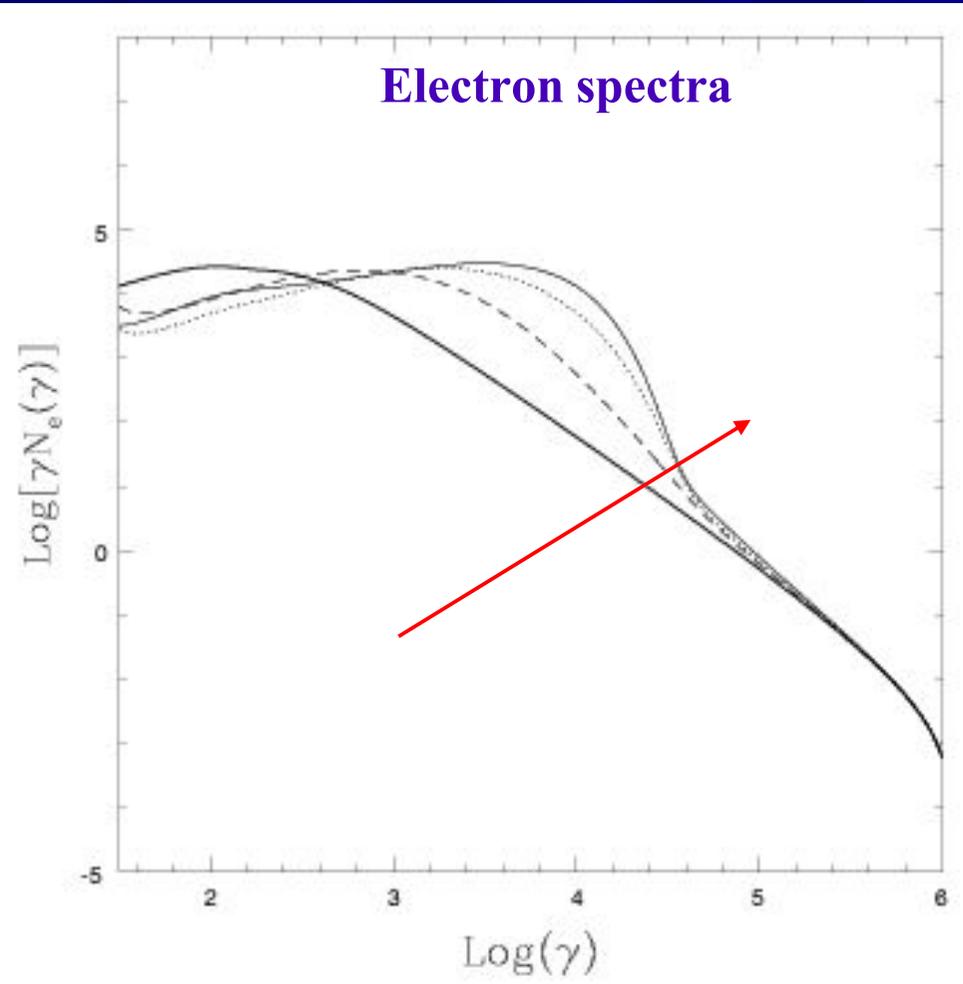
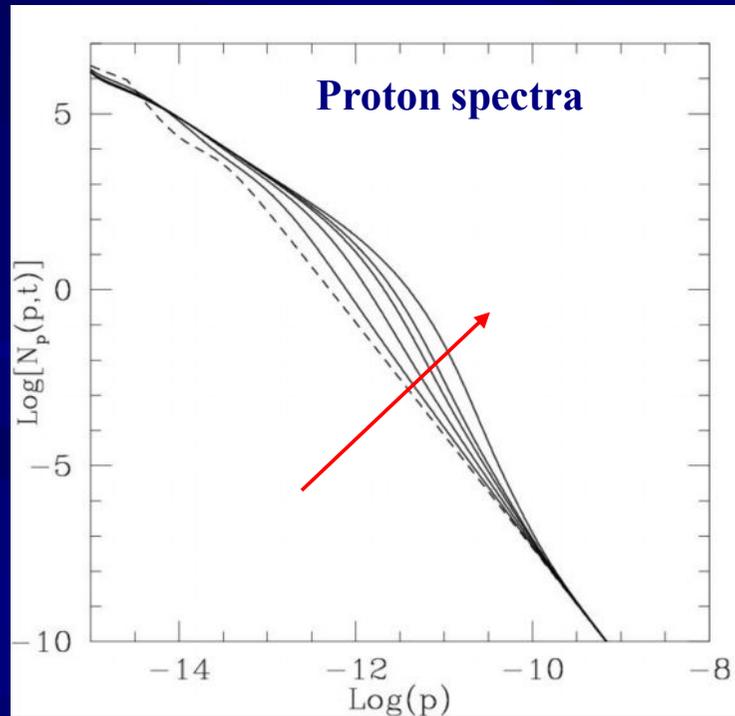
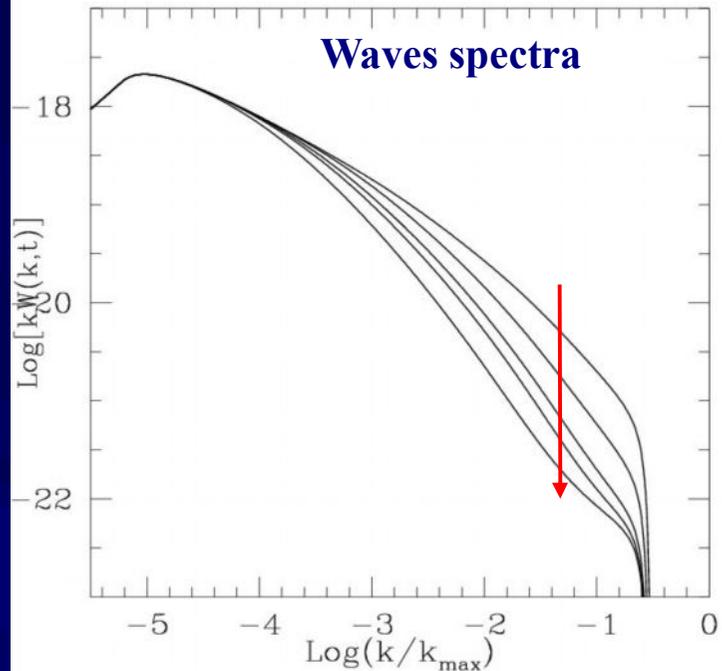
$I(k)$



$N_p(p,t), N_{e^\pm}(p,t), W(k,t), Q_{e^\pm}(p,t), Q_\pi(p,t)$

# Full Alfven-Wave--Particle Coupling

(Brunetti & Blasi 2005; Brunetti et al. 2009)

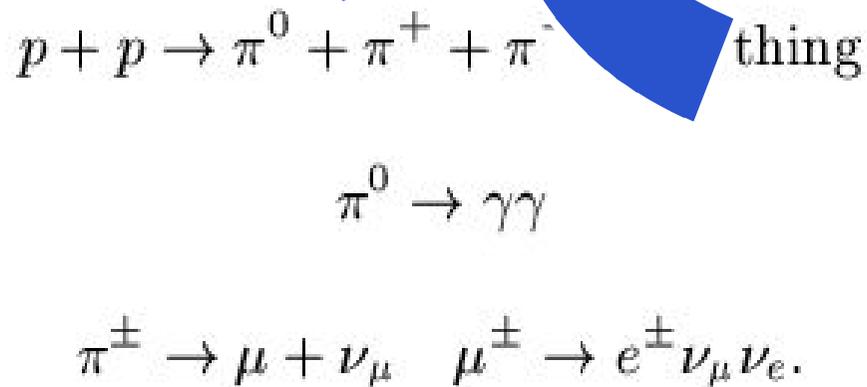


Waves + Protons + Secondaries

# Alfvenic: results

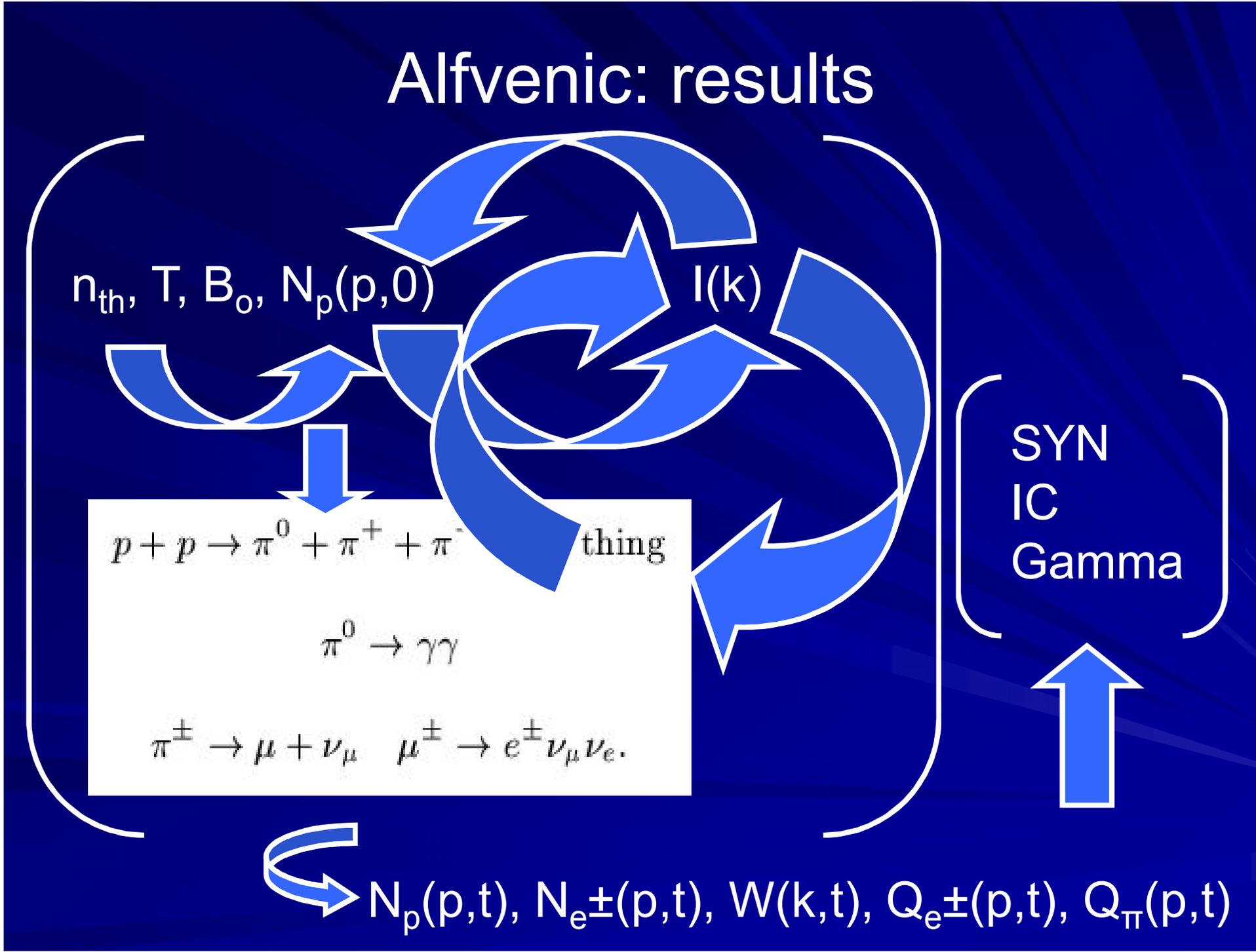
$n_{th}, T, B_0, N_p(p,0)$

$I(k)$



SYN  
 IC  
 Gamma

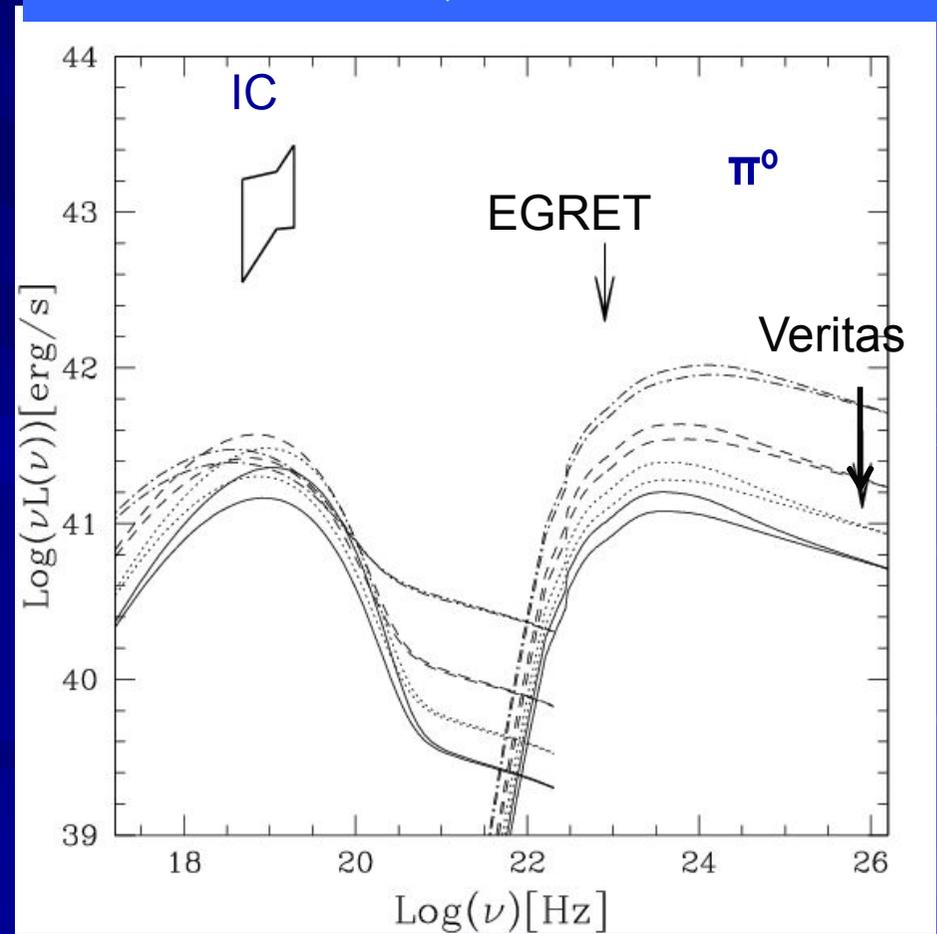
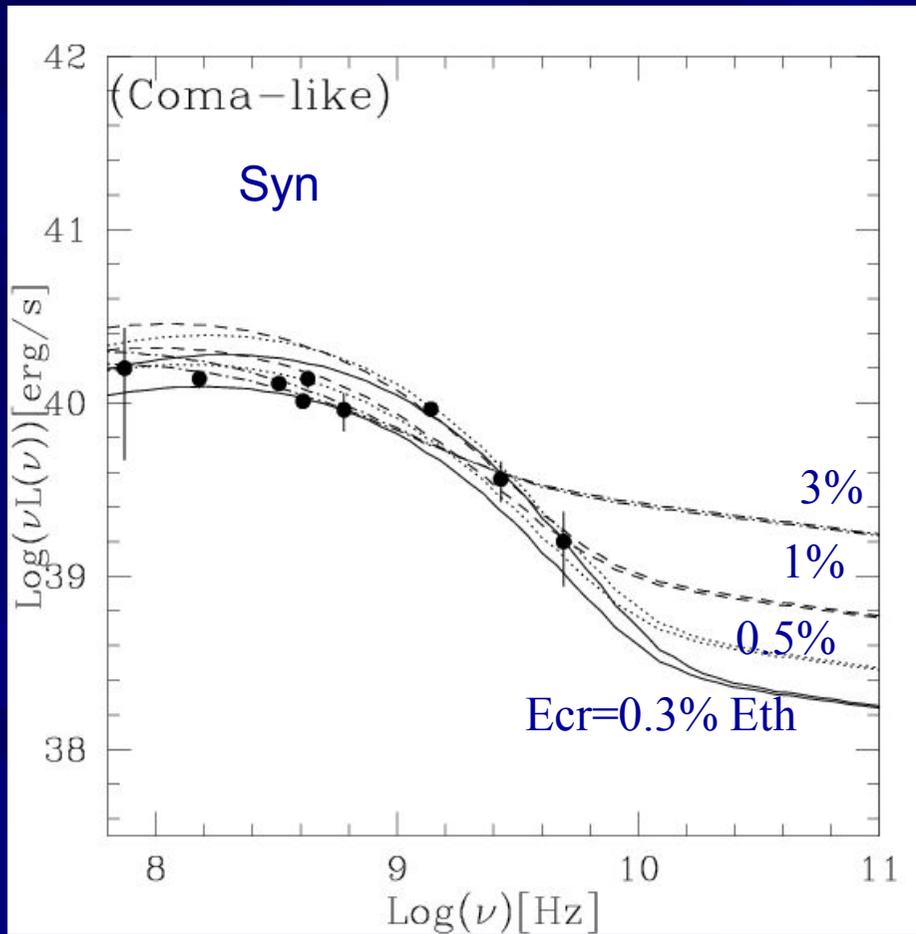
$N_p(p,t), N_{e^\pm}(p,t), W(k,t), Q_{e^\pm}(p,t), Q_\pi(p,t)$



# Alfvenic: results

Toy Model:  $\beta$ -profile,  $B_0 \approx A n_{th}$ ,  $B_0(0)=2\mu\text{G}$ ,  $W_{CR} \approx f W_{th}$ ,  $P_A \approx Q n_{th}^{5/6}$

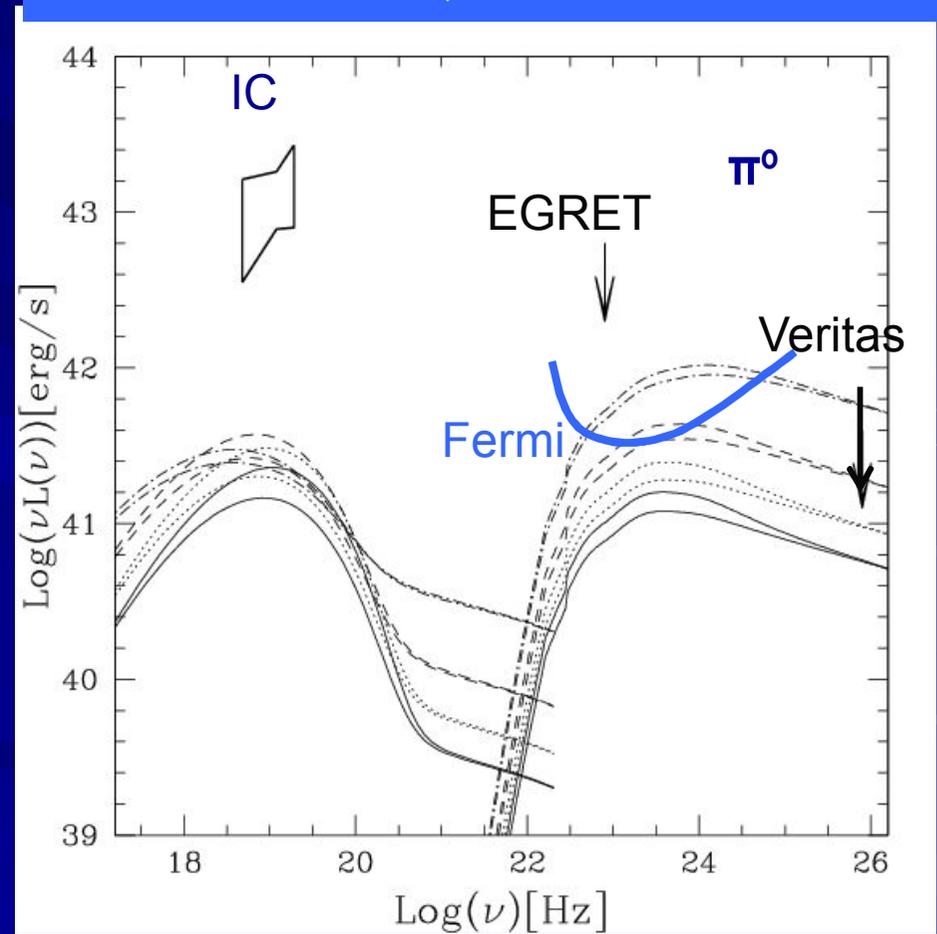
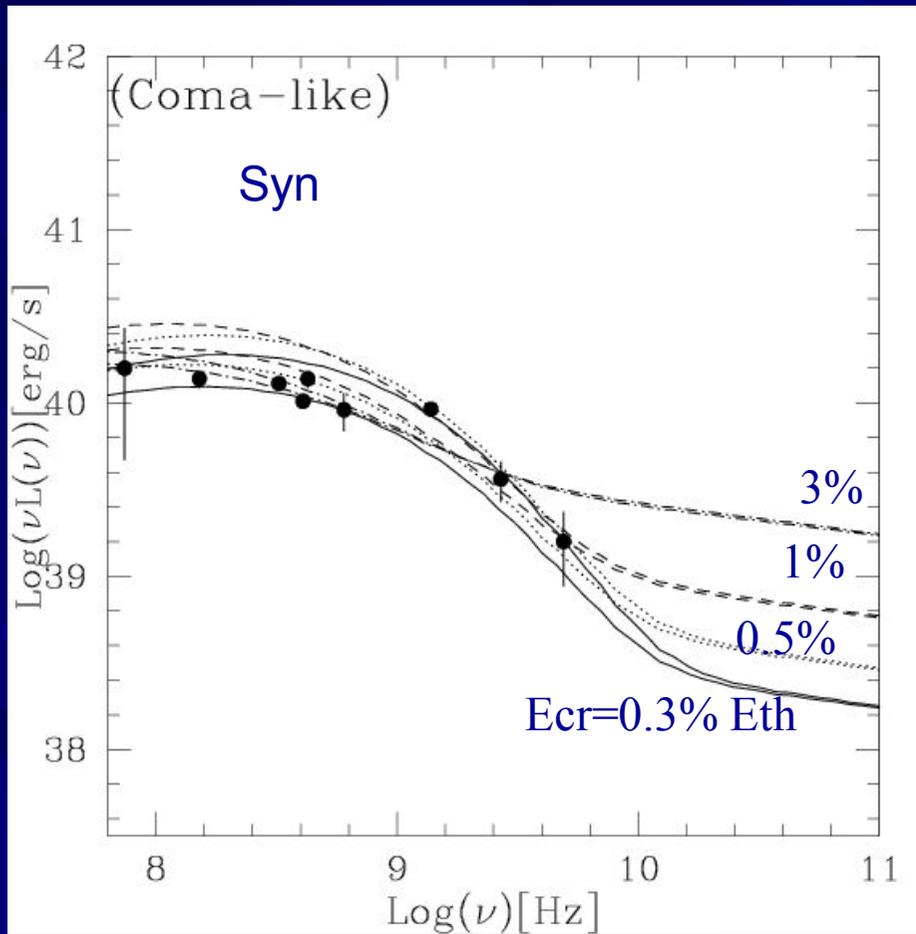
Brunetti, et al. 2009



# Alfvenic: results

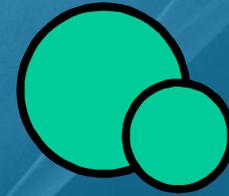
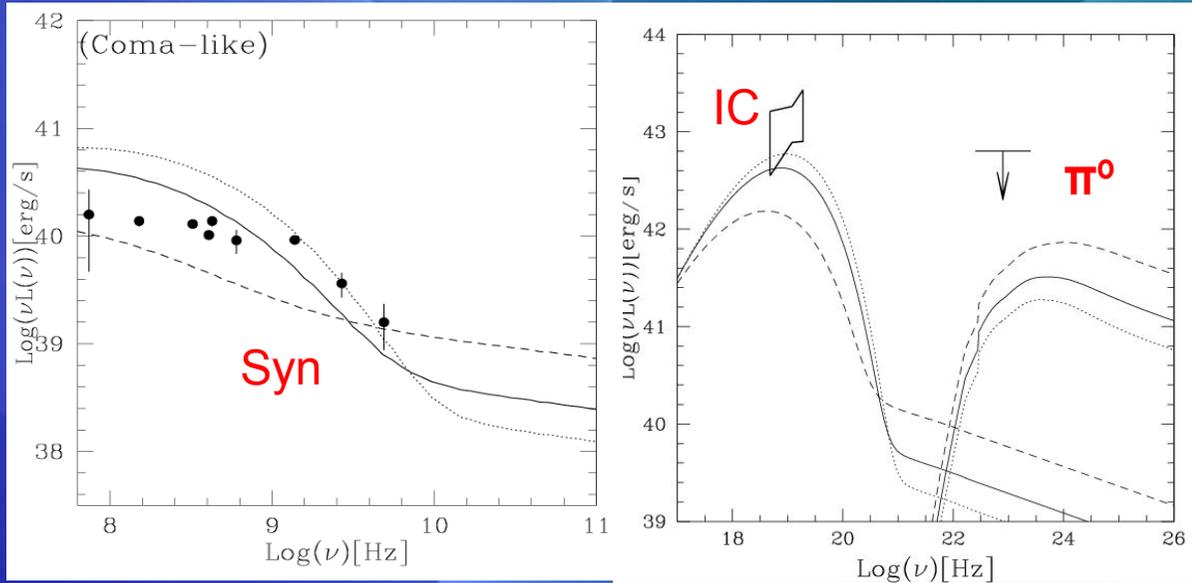
Toy Model:  $\beta$ -profile,  $B_0 \approx A n_{th}$ ,  $B_0(0)=2\mu\text{G}$ ,  $W_{CR} \approx f W_{th}$ ,  $P_A \approx Q n_{th}^{5/6}$

Brunetti, et al. 2009

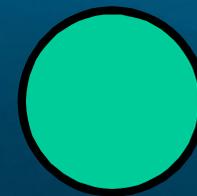
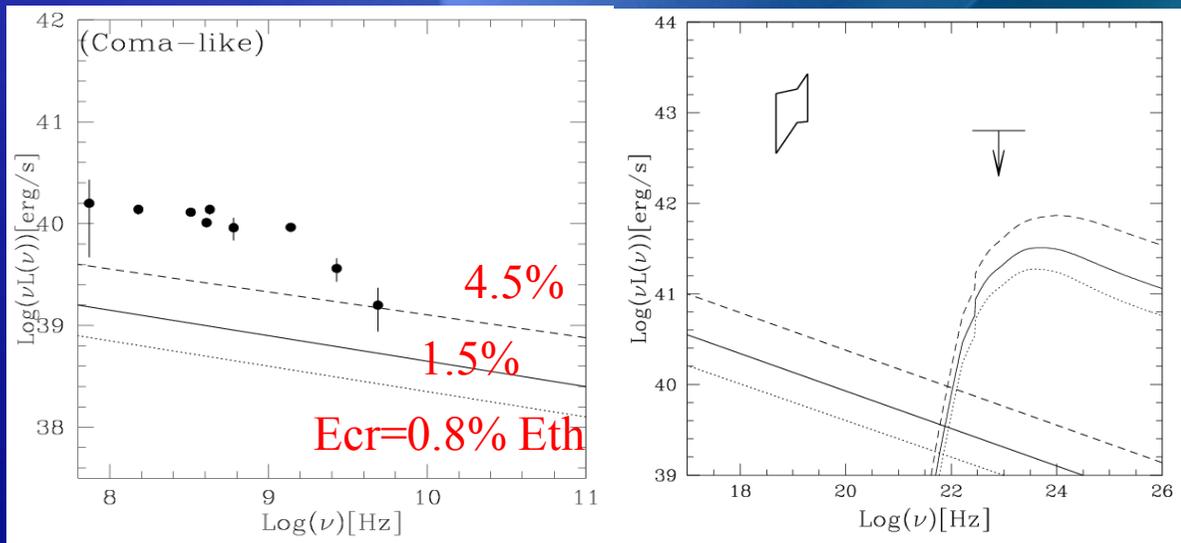


# General multiwavelength expectations

Brunetti 2008; Brunetti +al. 2009

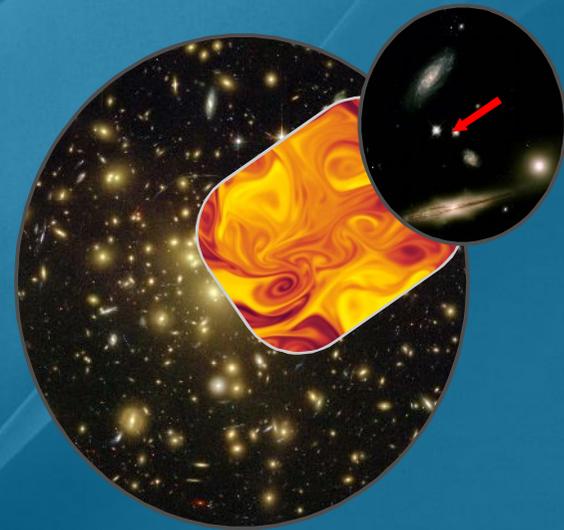
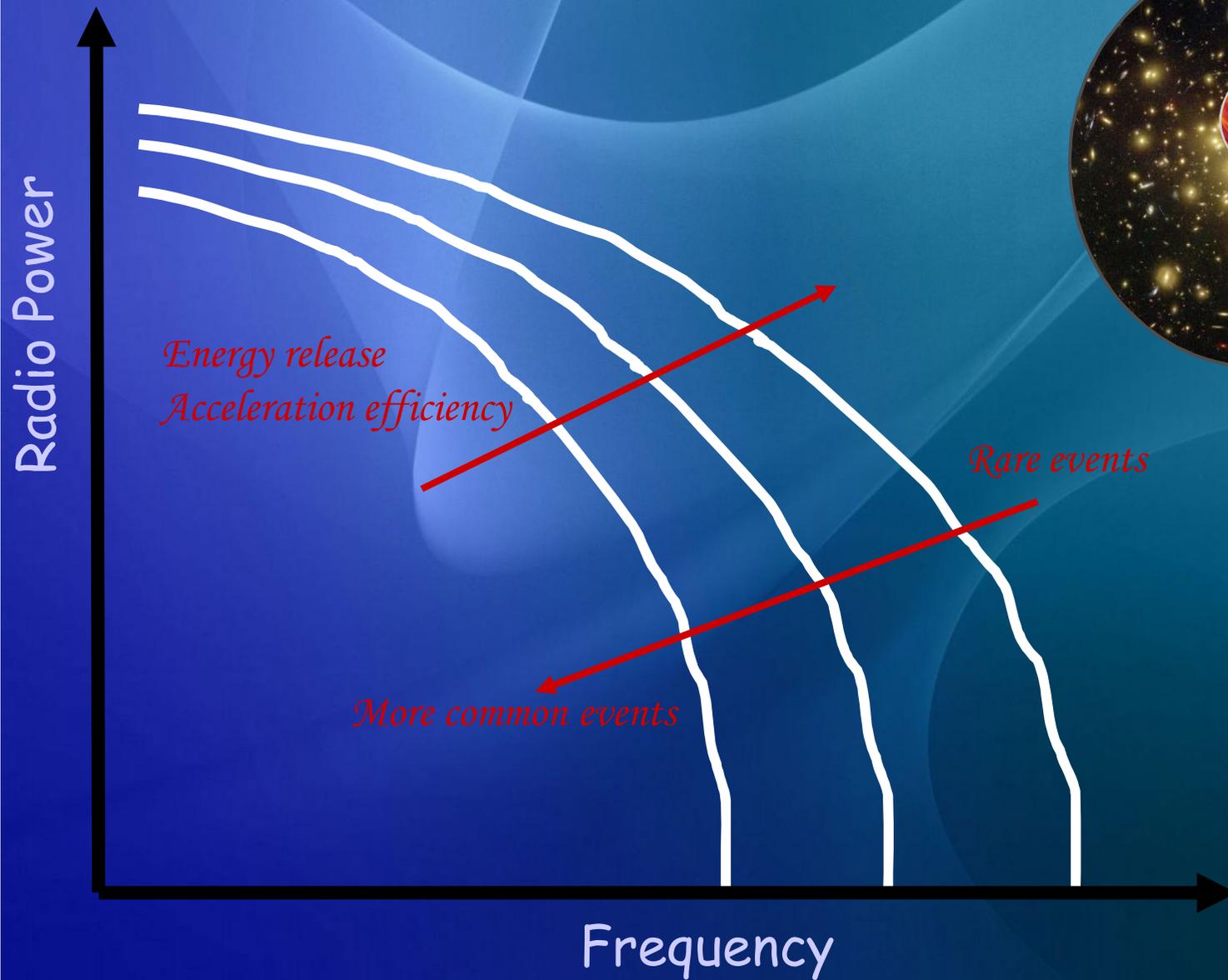


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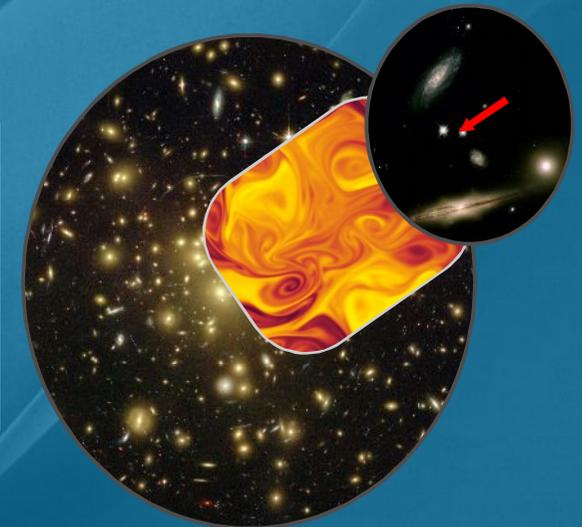
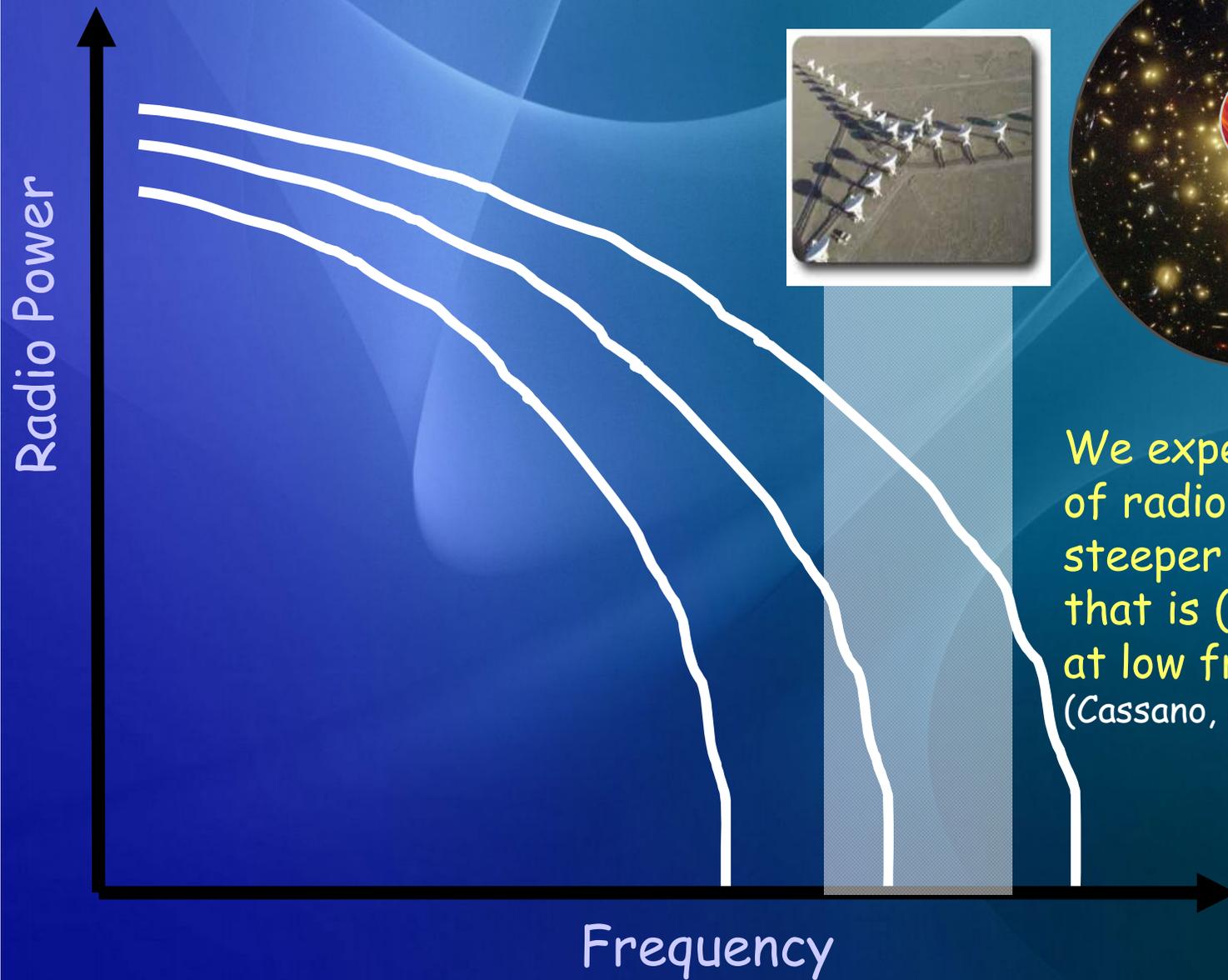


ALL  
CLUSTERS

# The case of the “ultra steep” spectrum radio halos

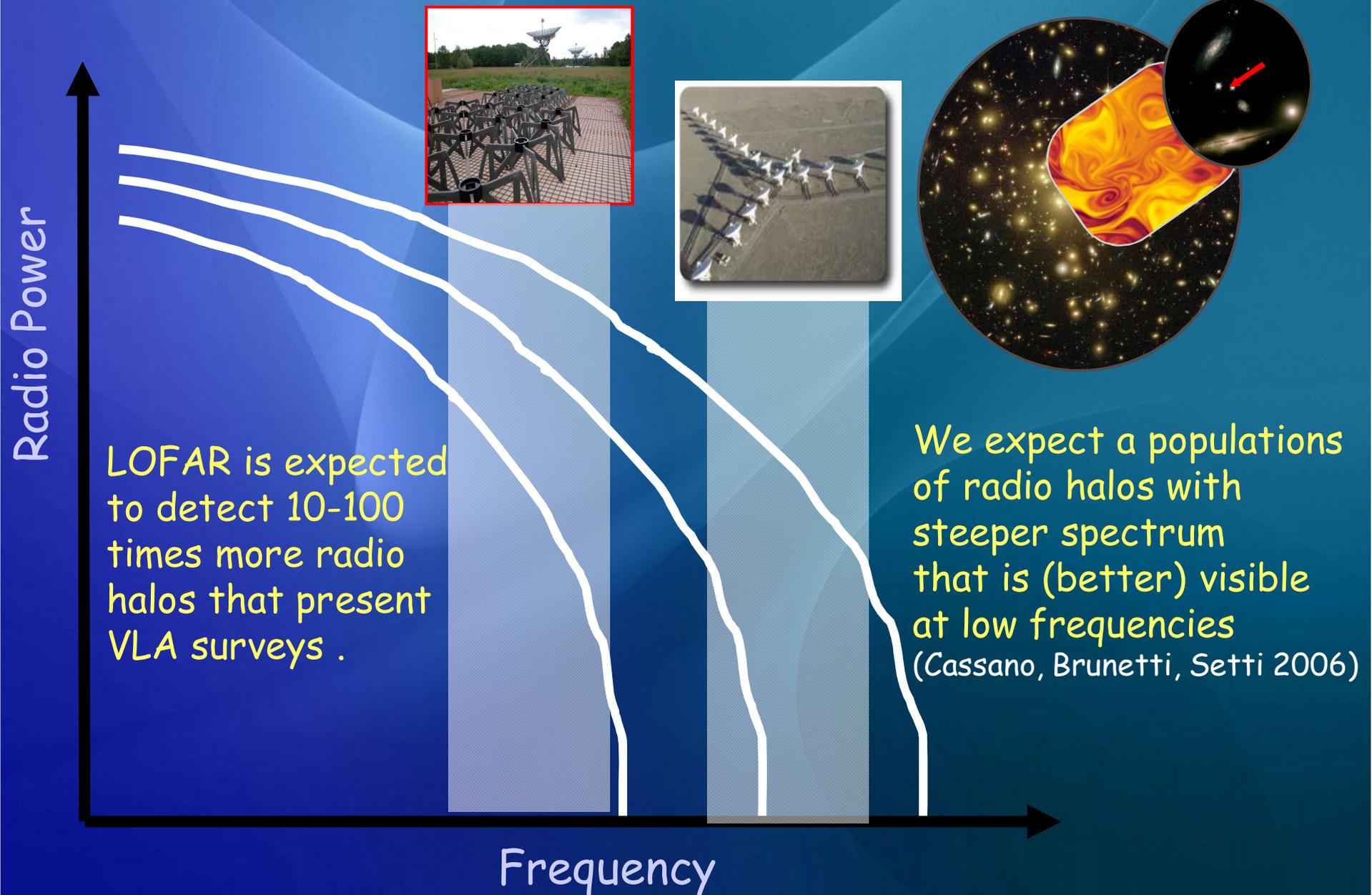


# The case of the “ultra steep” spectrum radio halos

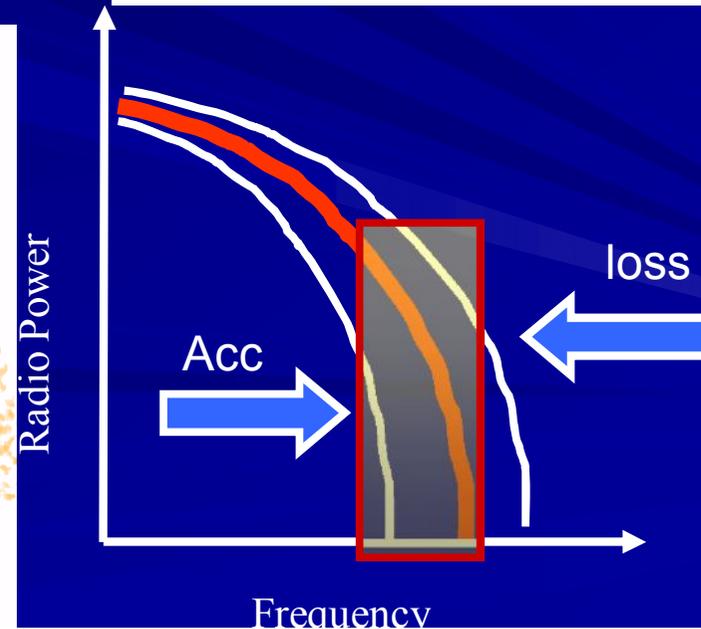
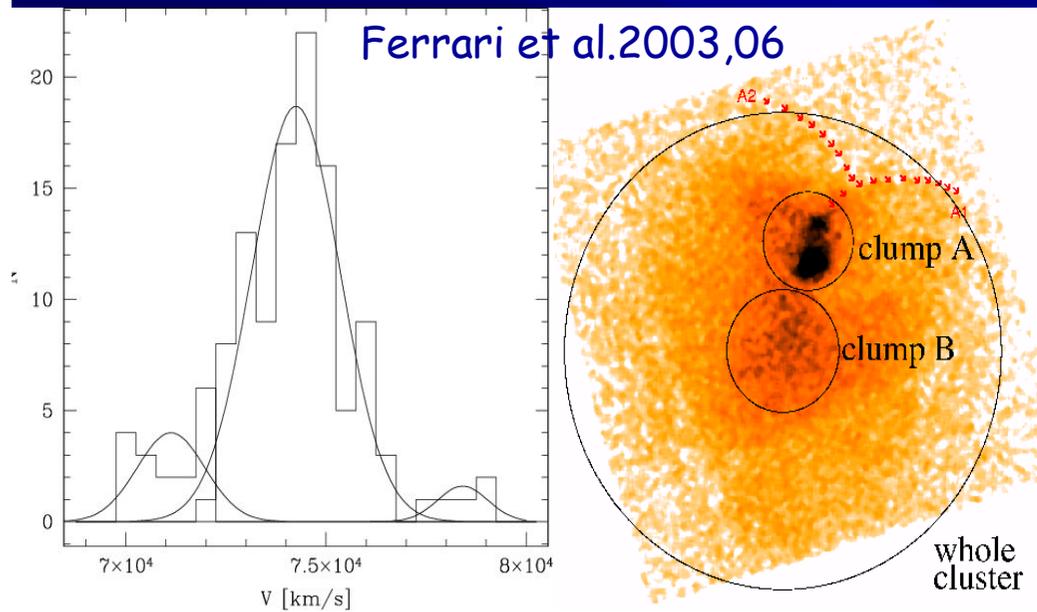
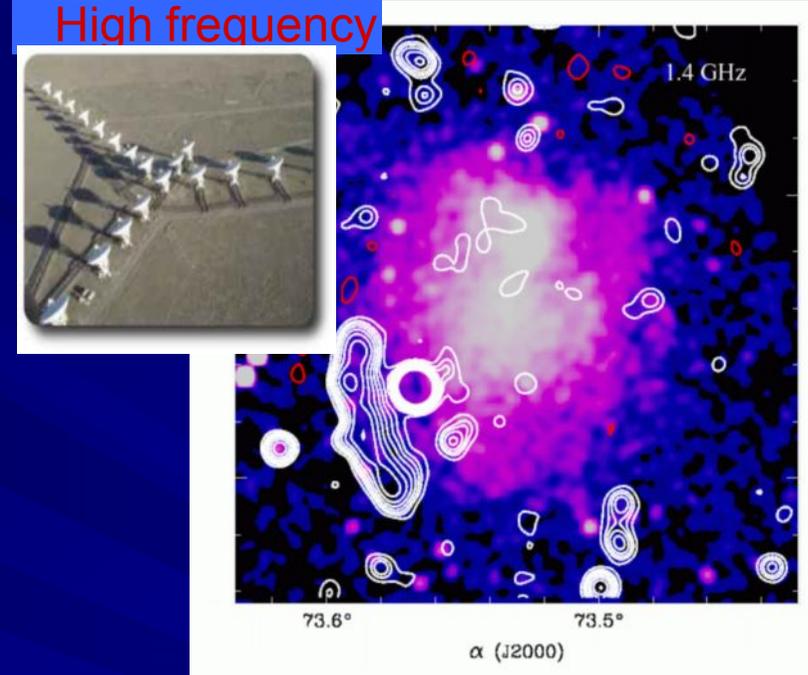
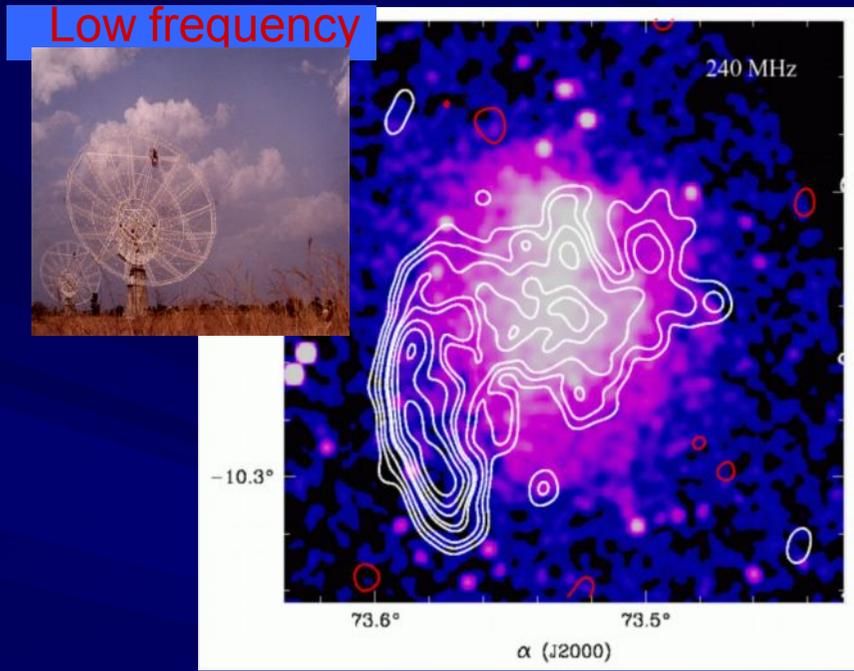


We expect a populations of radio halos with steeper spectrum that is (better) visible at low frequencies  
(Cassano, Brunetti, Setti 2006)

# The case of the “ultra steep” spectrum radio halos

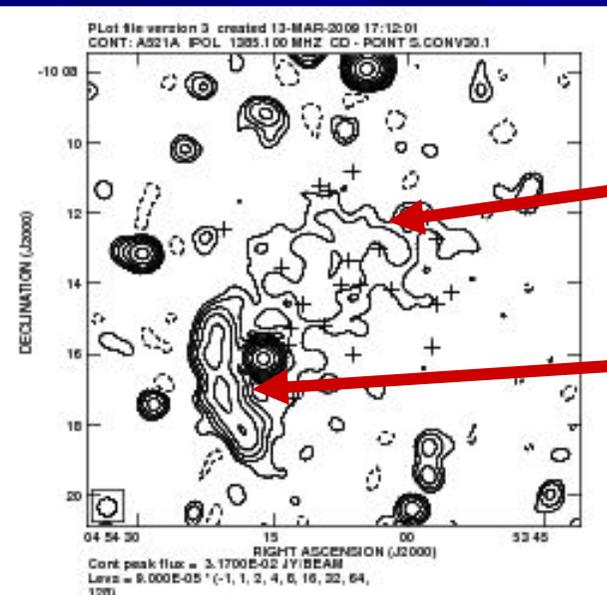
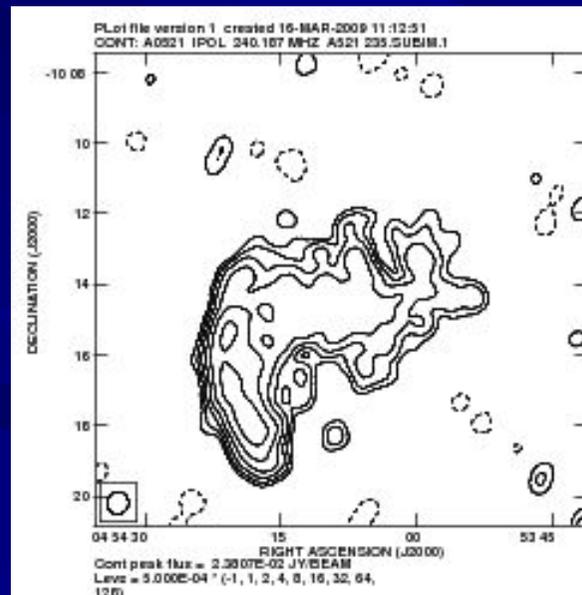
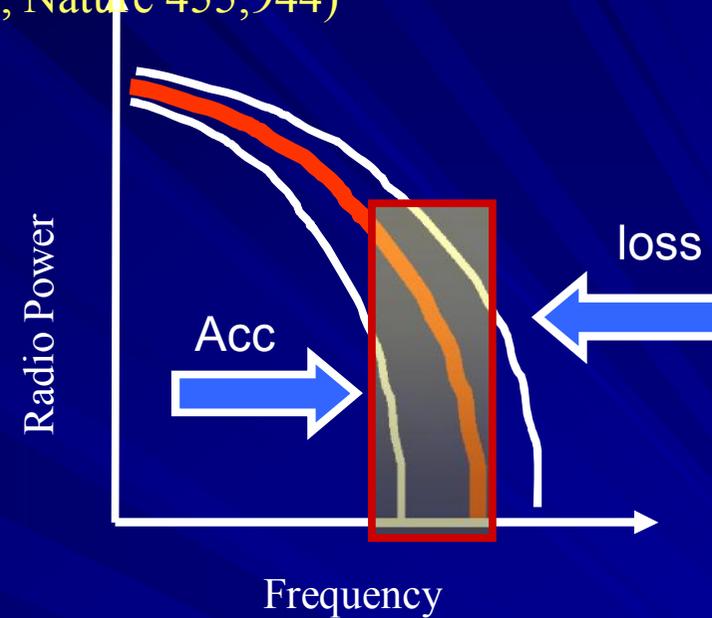
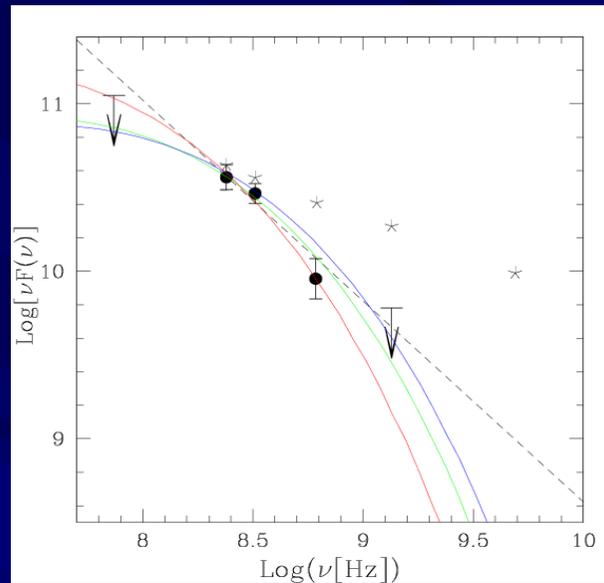


# Do they exist ? (Brunetti +al. 2008, Nature 455,944)



# (indirect) evidence for turbulent acceleration

(Brunetti +al. 2008, Nature 455,944)



Dallacasa, Brunetti, et al. 2009

# Conclusions

Theoretically protons should be the dominant non thermal particle-component in the IGM (yet only limits)

Theoretically shocks may be an important source of non thermal particles in the IGM, in addition present data suggest that turbulence plays a role in the acceleration of particles in galaxy clusters

The non-thermal emission from galaxy clusters is a mixture of a transient (turbulence) and long-living component

LOFAR & FERMI will step into an essentially unexplored territory where theories can be tested (eg "ultra steep halos")



**LOFAR**



*The FUTURE*



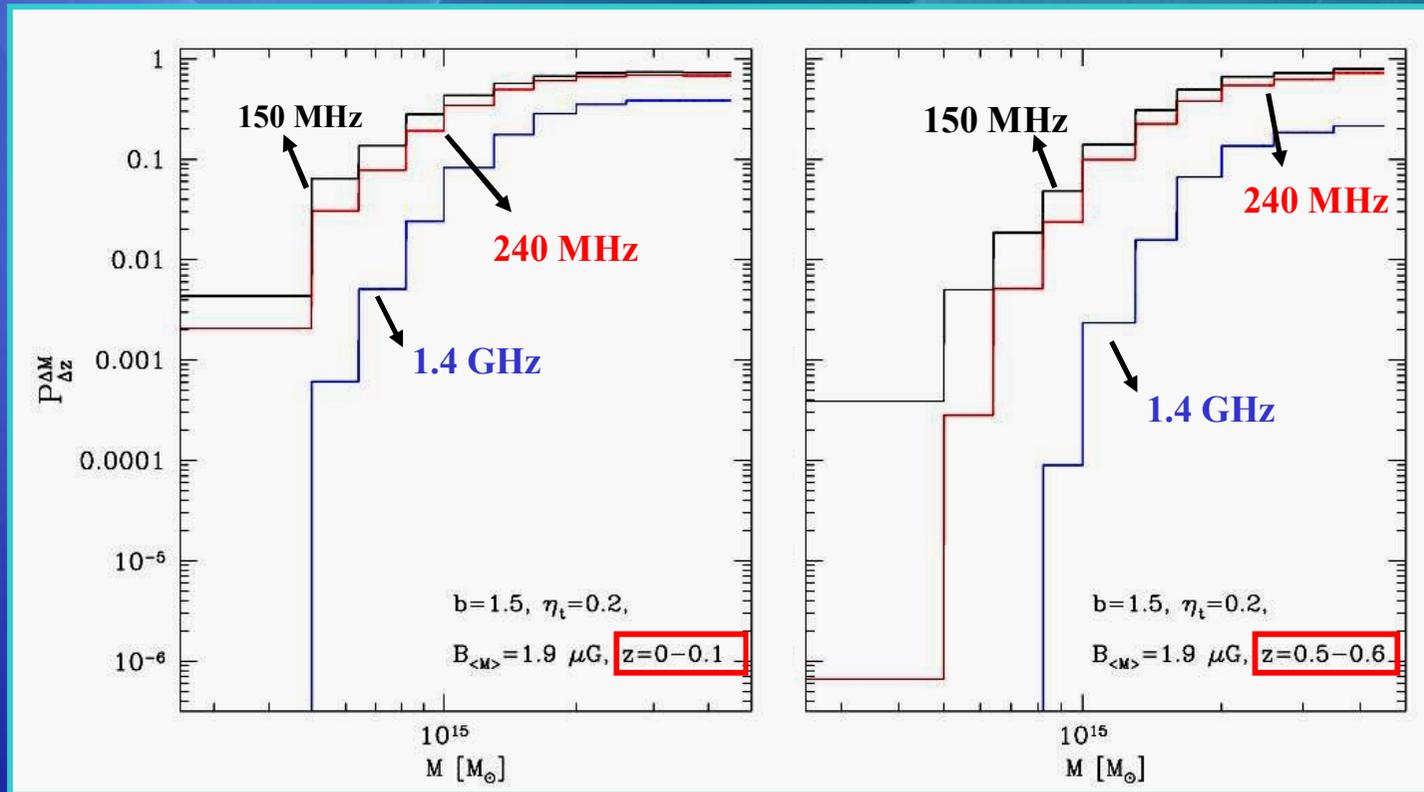
**Fermi**

**Cherenkov**



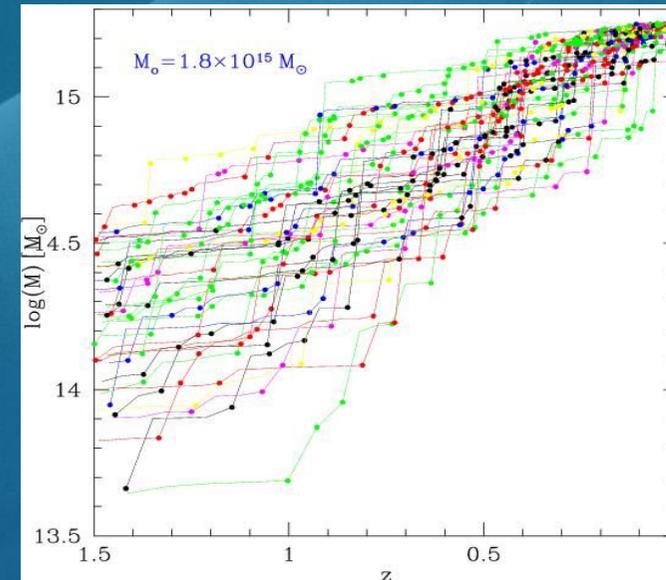
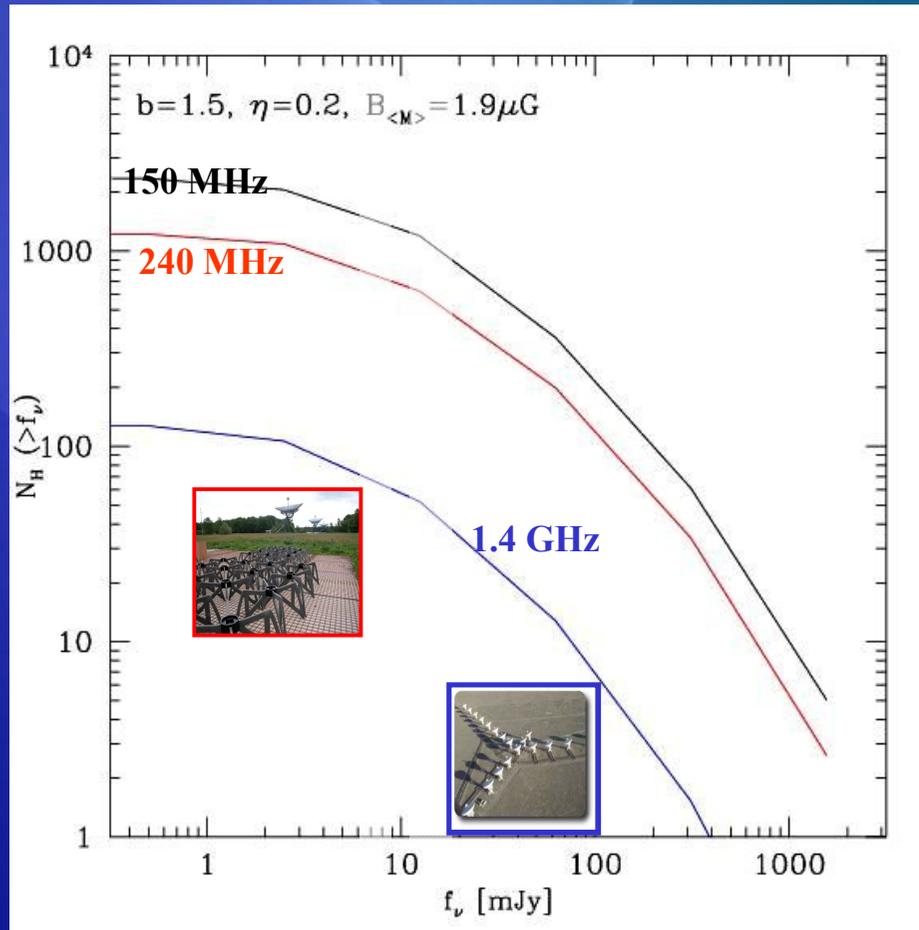
# Fraction of galaxy clusters with radio halos at low $\nu$

*Cassano et al. 2008*



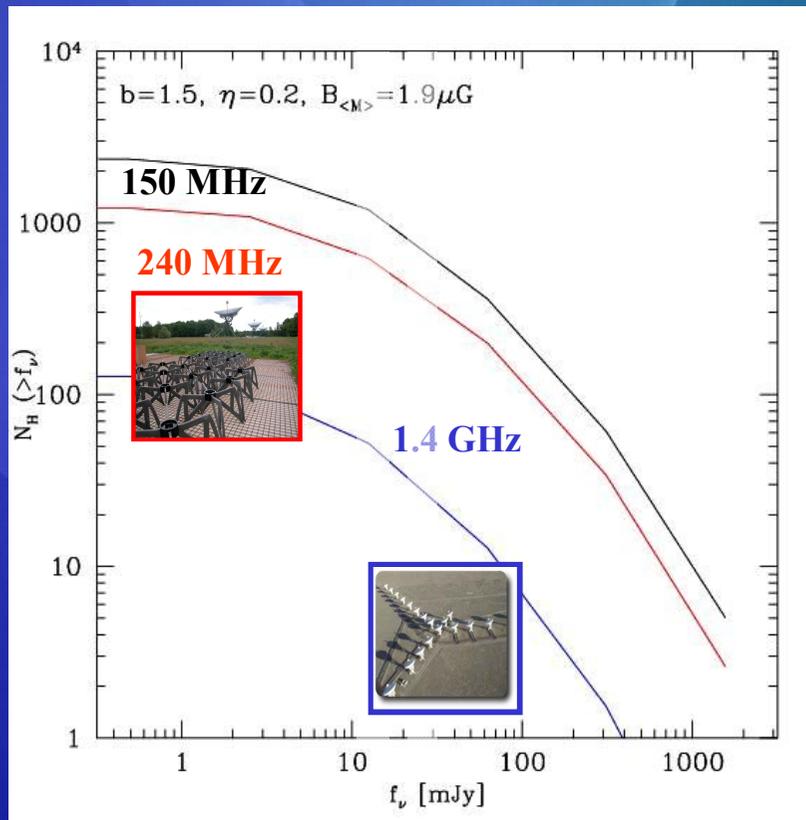
- ❖ The expected fraction of clusters with radio halos increases at low  $\nu$
- ❖ This increase is even stronger for **smaller clusters** ( $M < 10^{15} M_{\odot}$ )

# Radio halos in the LOFAR era ...

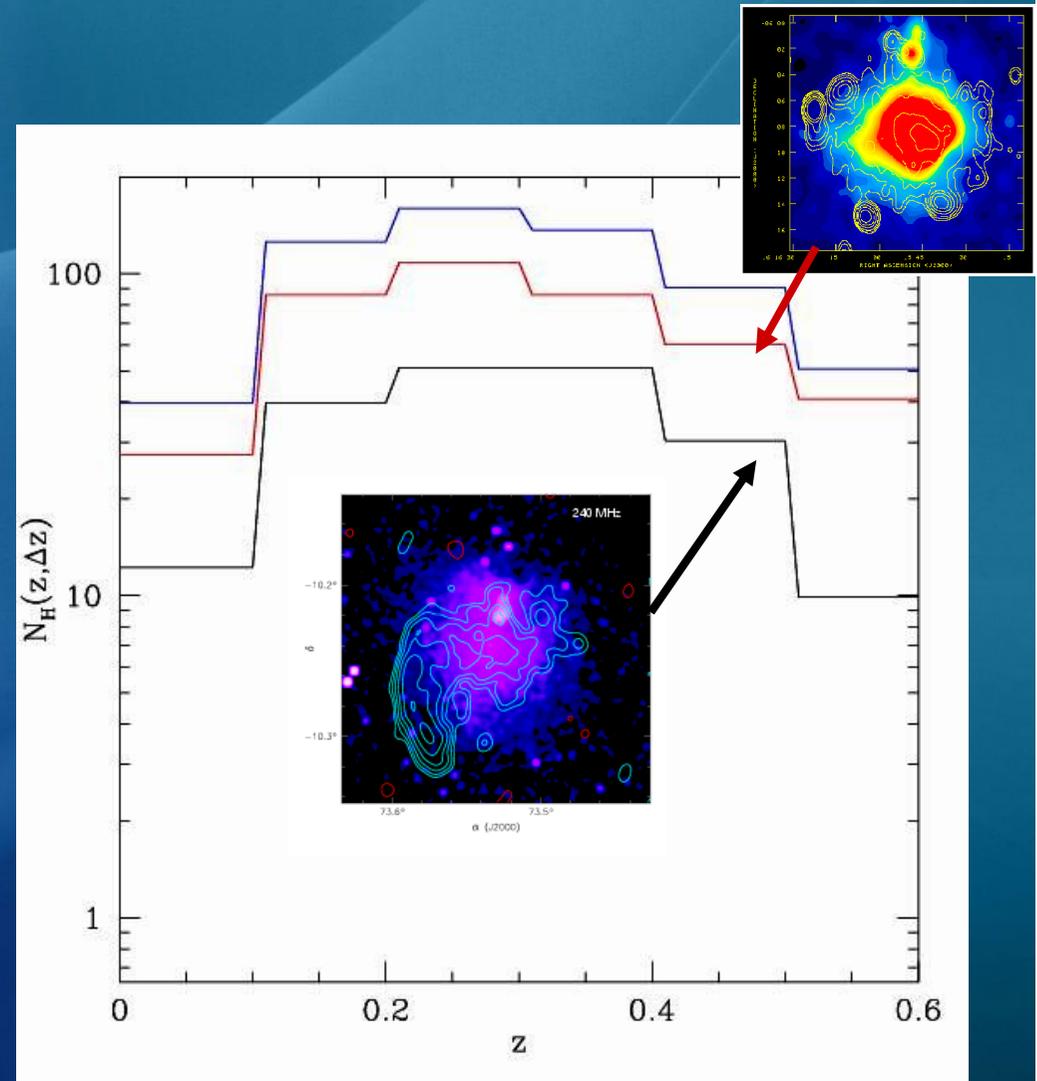


The number of radio halos detectable by deep low frequency observations is expected 10 times larger than that from present VLA observations at 1.4 GHz : **LOFAR** and **LWA** will catch these sources !

# Radio halos in the LOFAR era ...



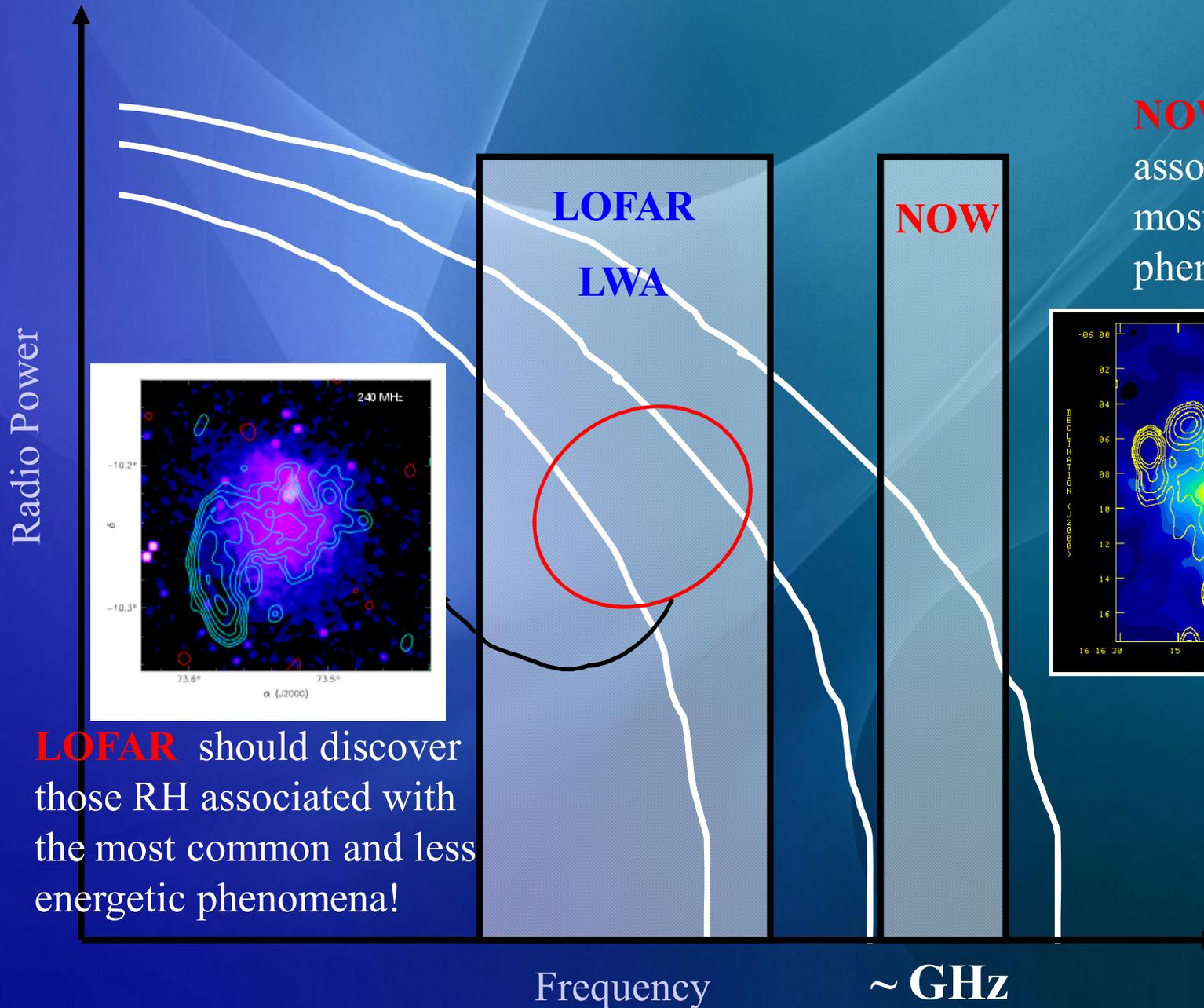
We expect that the number of RHs detectable by deep low frequency observations is 10 times larger than that from present VLA observations at 1.4 GHz : **LOFAR** and **LWA** would catch these RHs !



**LOFAR** “20” beam=25”x 25”  
 counts at 120 MHz (Cassano et al., in prep.).

Number

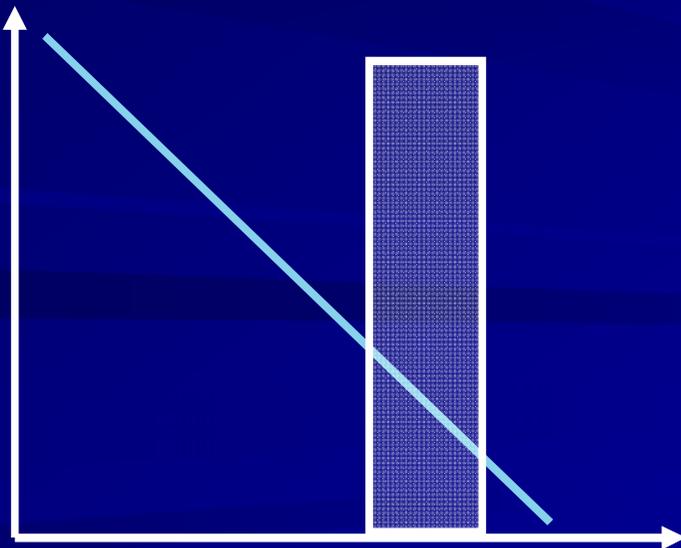
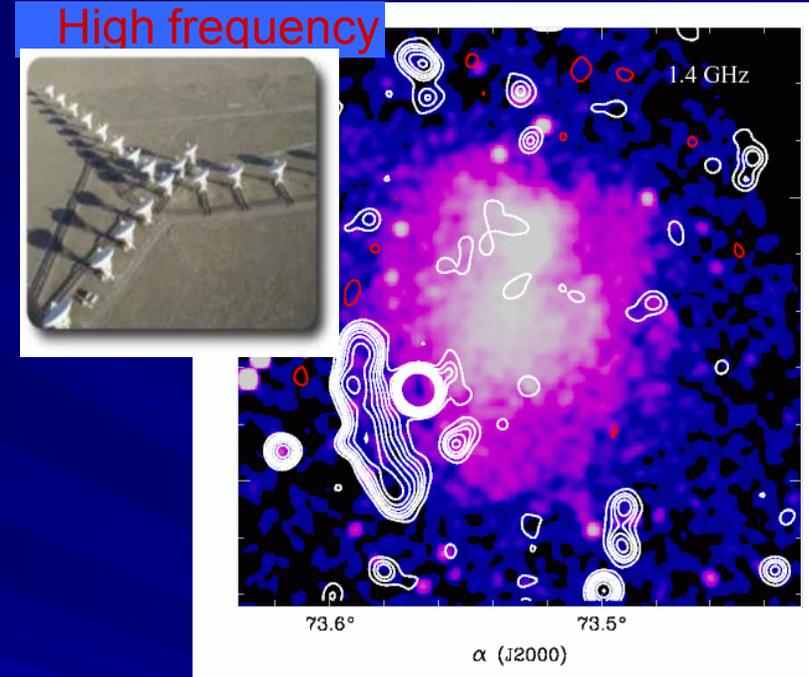
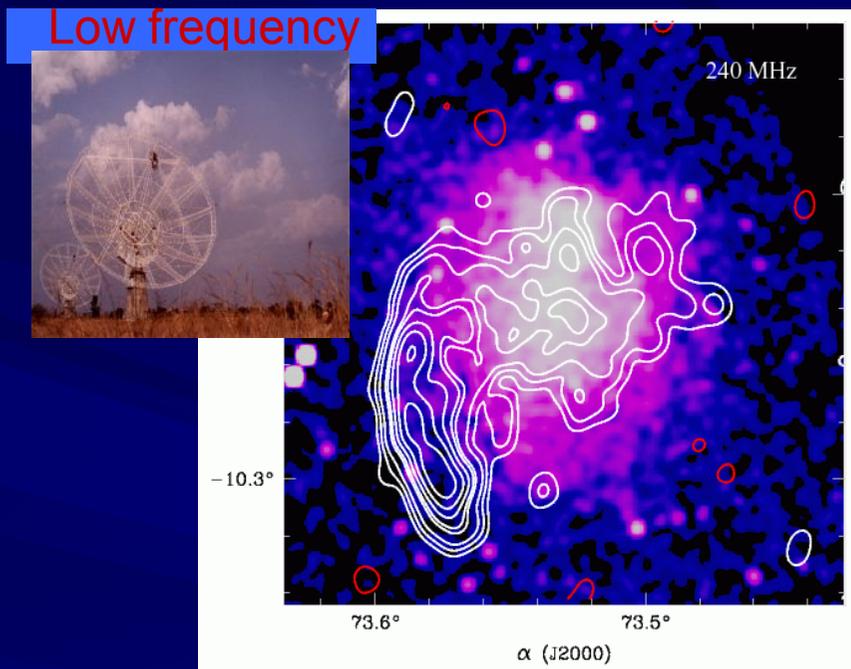
# Radio halos at lower radio frequencies



**NOW** we see RH associated with the most energetic phenomena!

**LOFAR** should discover those RH associated with the most common and less energetic phenomena!

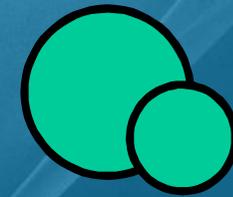
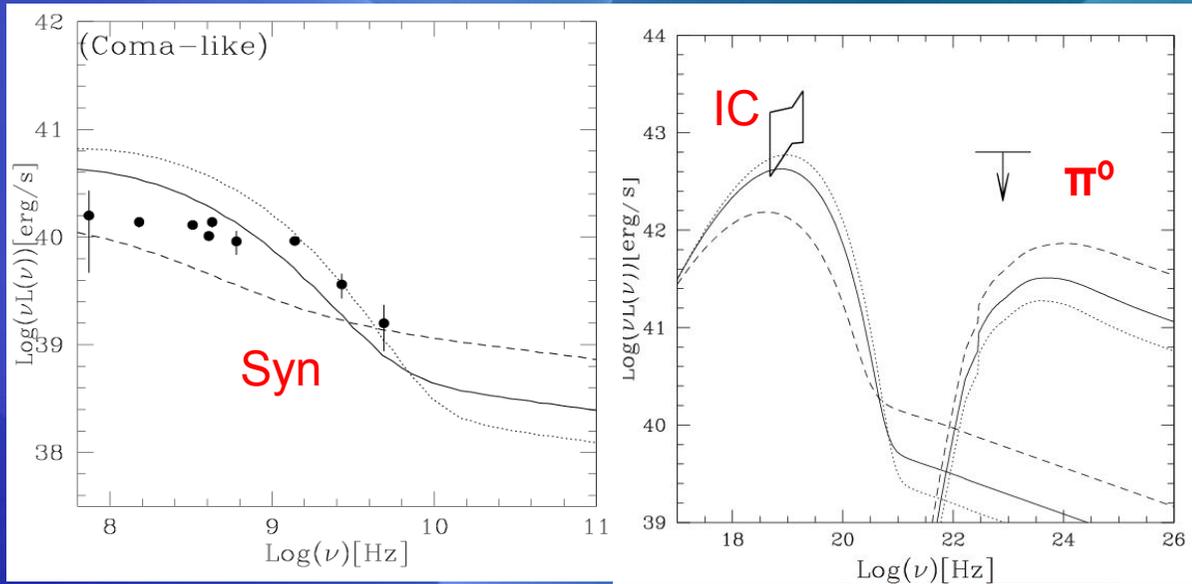
# Do they exist ? (Brunetti +al. 2008, Nature 455,944)



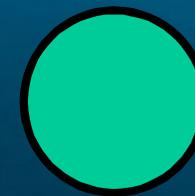
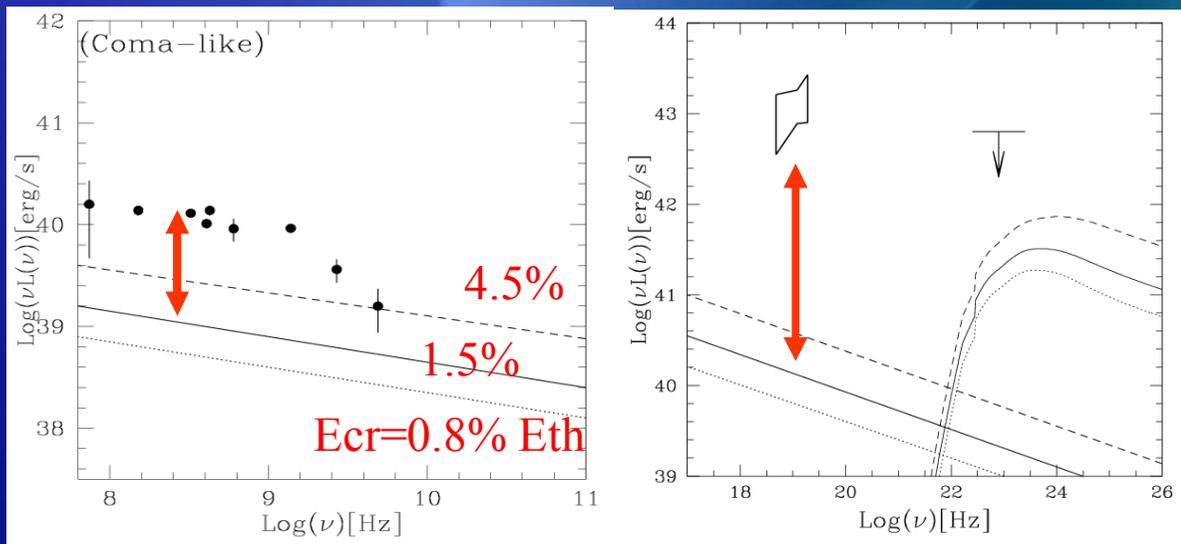
*Supposing that the observed synchrotron radiation is from secondary electrons generated during p-p collisions in the IGM .. we arrive at the untenable scenario of a relativistic proton population whose energy density exceeds that of the thermal IGM*

# General multiwavelength expectations

Brunetti 2008; Brunetti +al. 2009



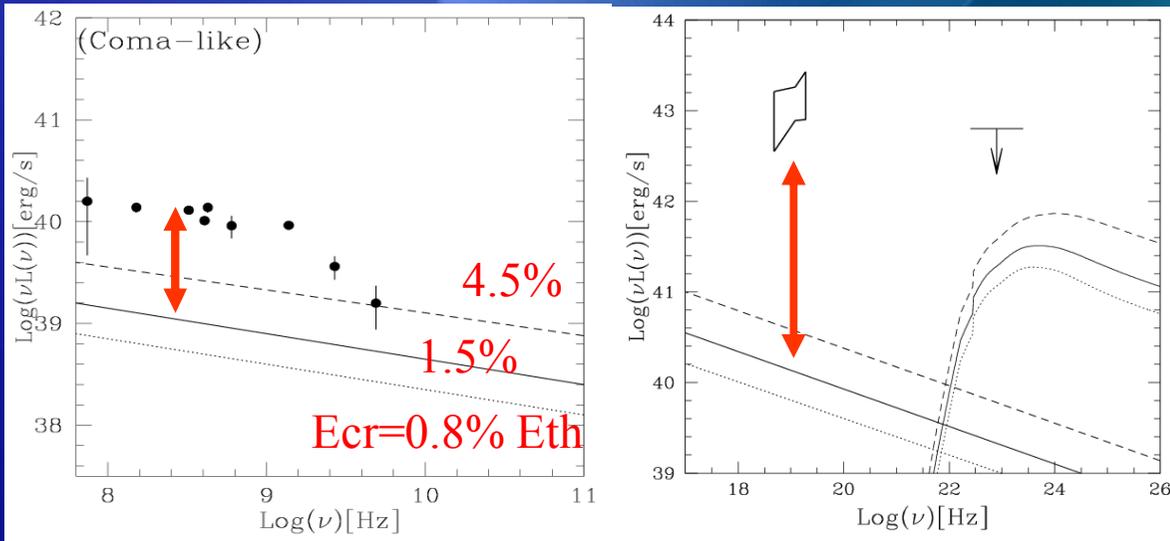
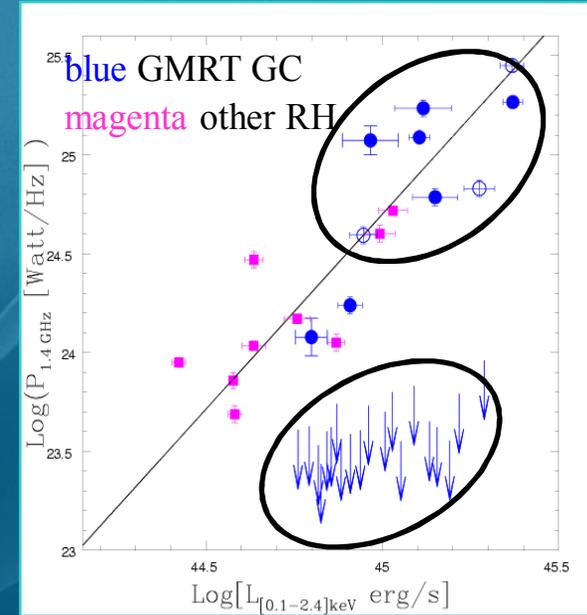
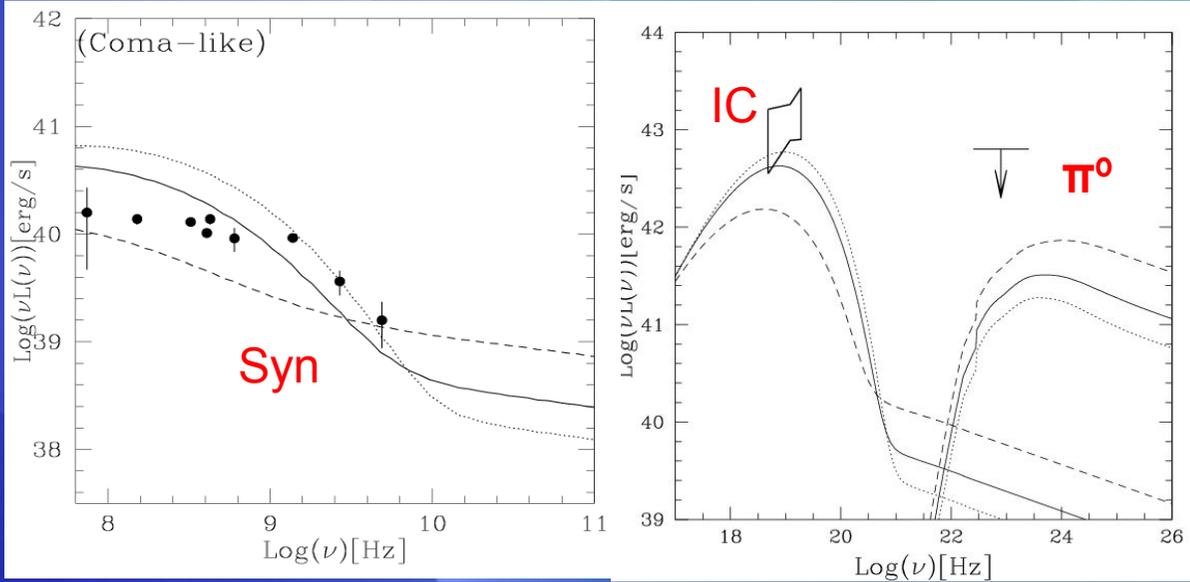
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CLUSTERS



ALL  
CLUSTERS

# General multiwavelength expectations

Brunetti 2008; Brunetti +al. 2009

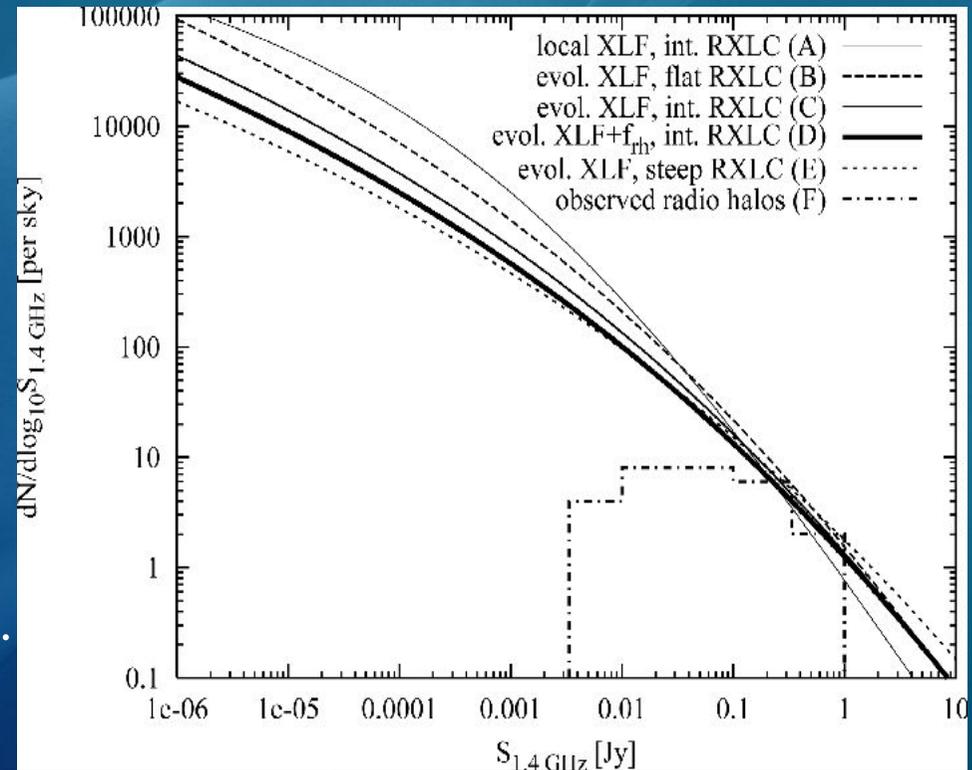


**TRANSIENT PHENOMENA**

# Why low frequency ?

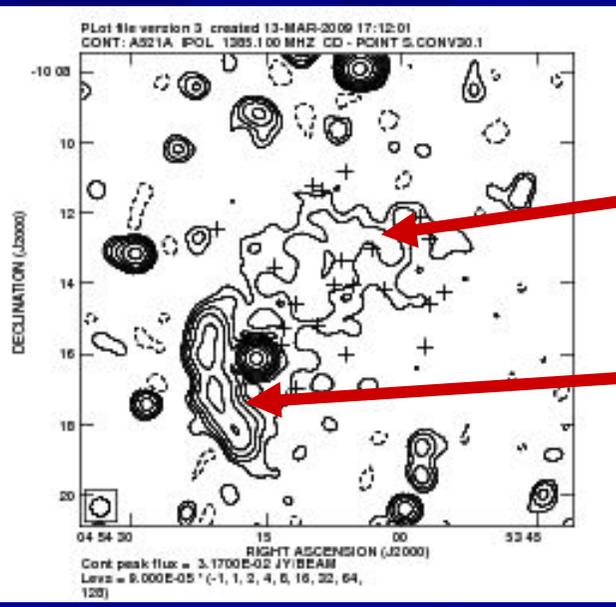
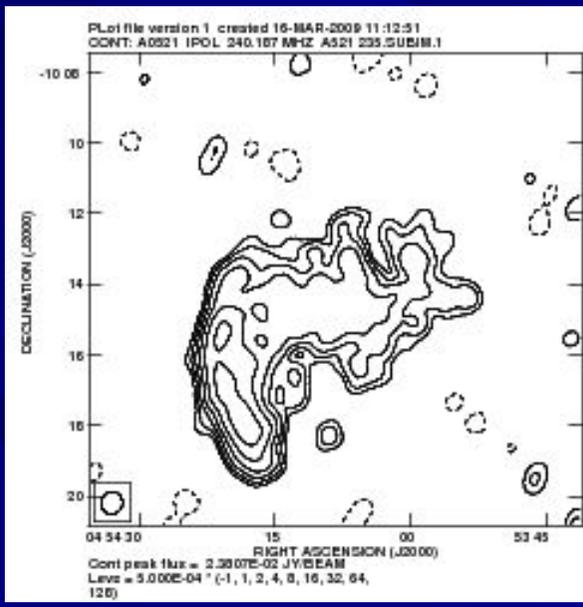
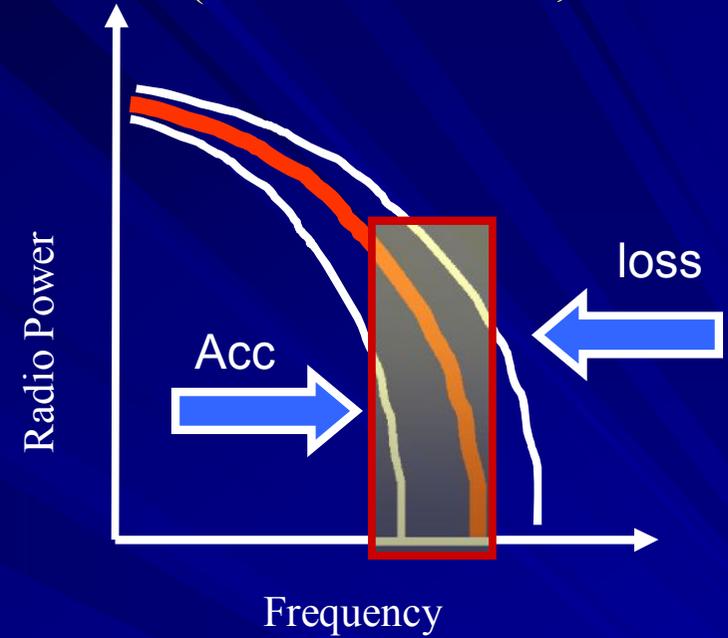
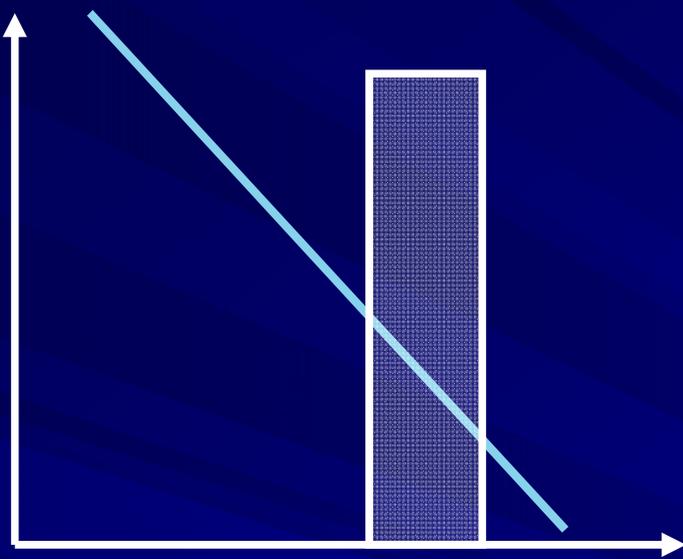
Ensslin & Roettgering 2002

Regardless of the origin of Radio Halos, extrapolations of their number counts at 1.4 GHz based on the Radio-X ray correlation observed for Radio Halos suggest that **a large fraction** of these Halos is **at faint fluxes**.



Due to their **steep synchrotron spectrum**, faint Radio Halos should appear more luminous at low frequencies and thus LOFAR and LWA are expected to discover a large number of these objects.

# Turbulent acceleration in GC (Brunetti +al. 2008, Nature 455,944)



Dallacasa + al. ApJL submitted

ASTRON

LOFAR

# The LOFAR Array



- Core area - 2 km around Exloo
  - Min. 18 stations
- Remote stations - 100 km
  - Min. 18 stations
- International stations
  - Min. 8 stations

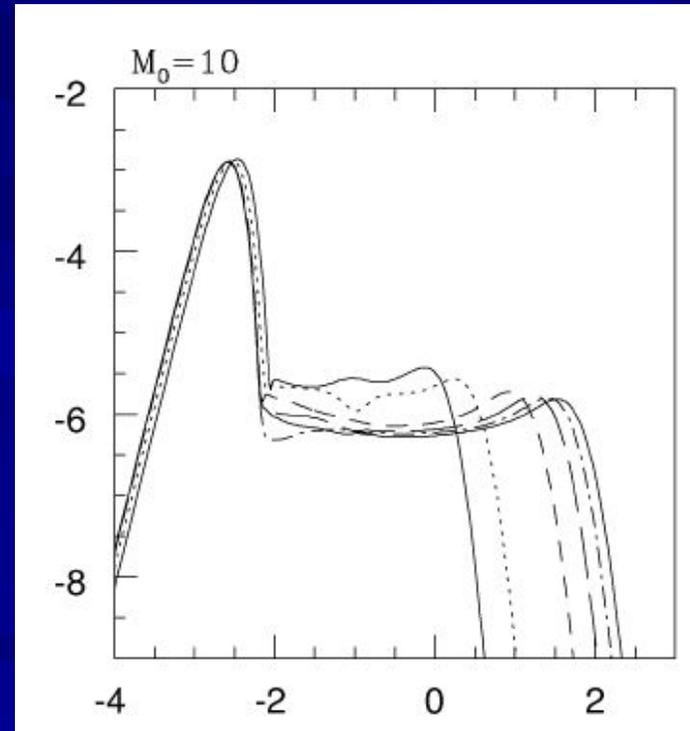
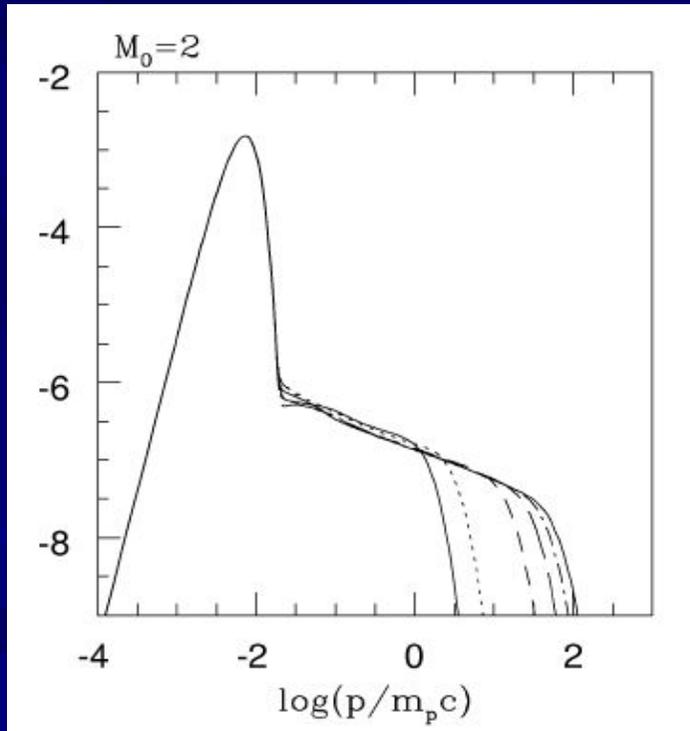
# Acceleration of CRp at shocks

$$N(p) \propto p^{-\delta}$$

$$\delta = 2 \frac{\mathcal{M}^2 + 1}{\mathcal{M}^2 - 1}$$

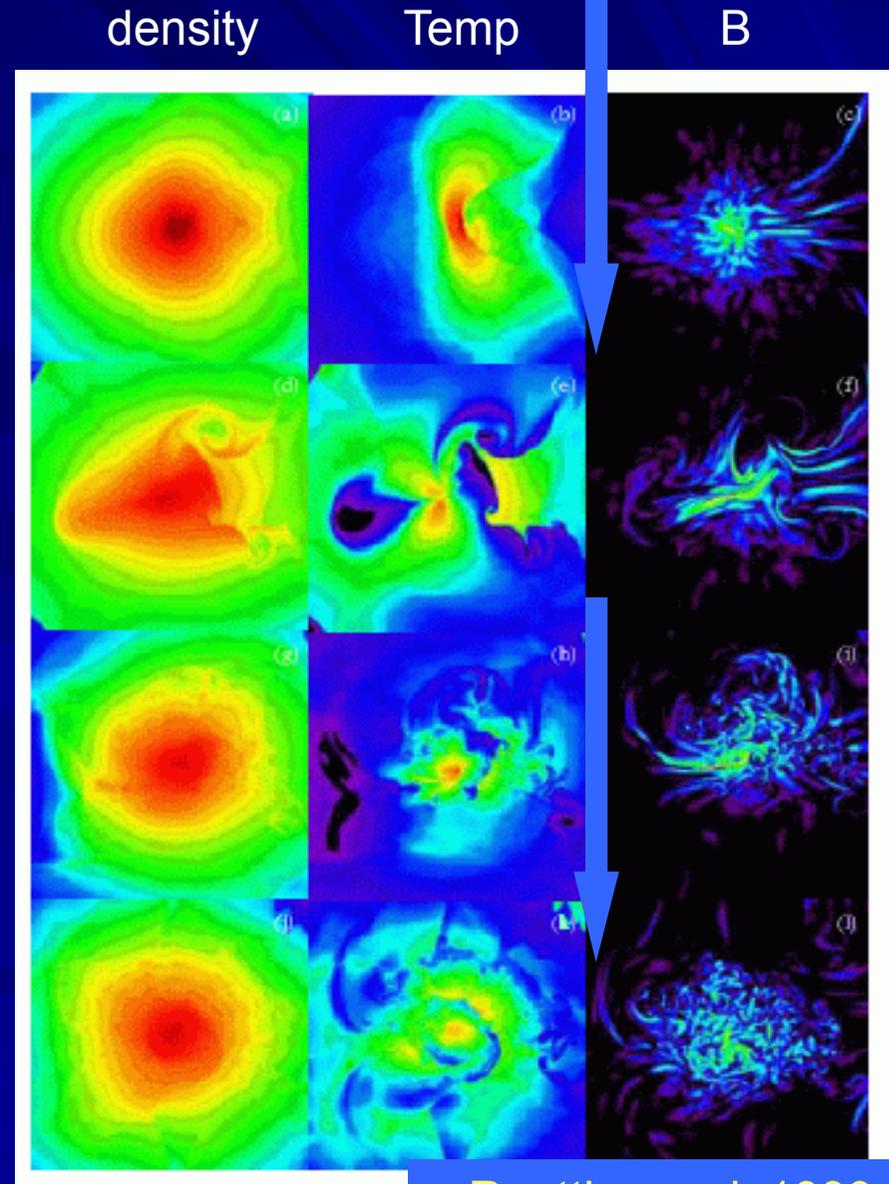
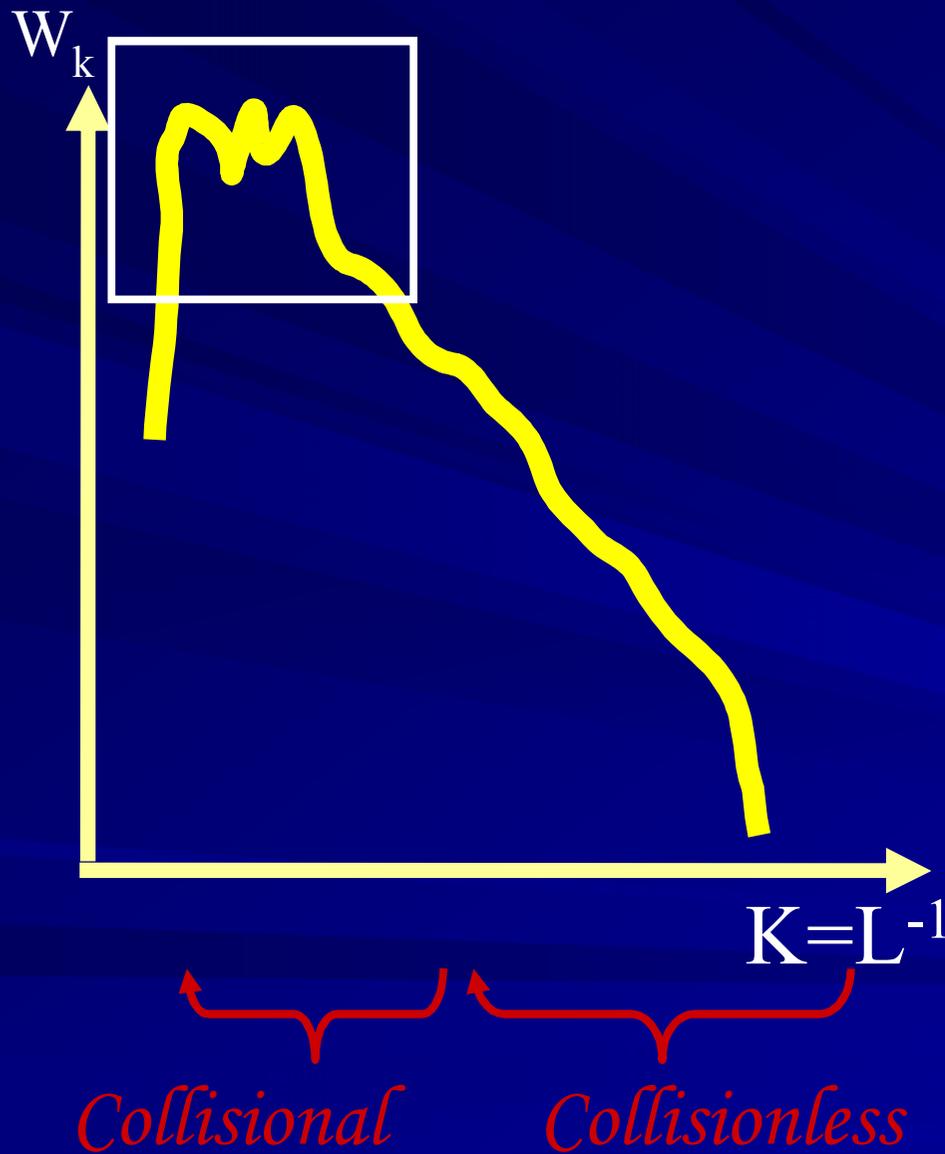
Linear Theory  
(e.g., Blandford & Eichler 1987)

$N p^2$



(Kang & Jones 2002; Malkov 1997, Kang & Jones 2005, 07, Amato & Blasi 2006)

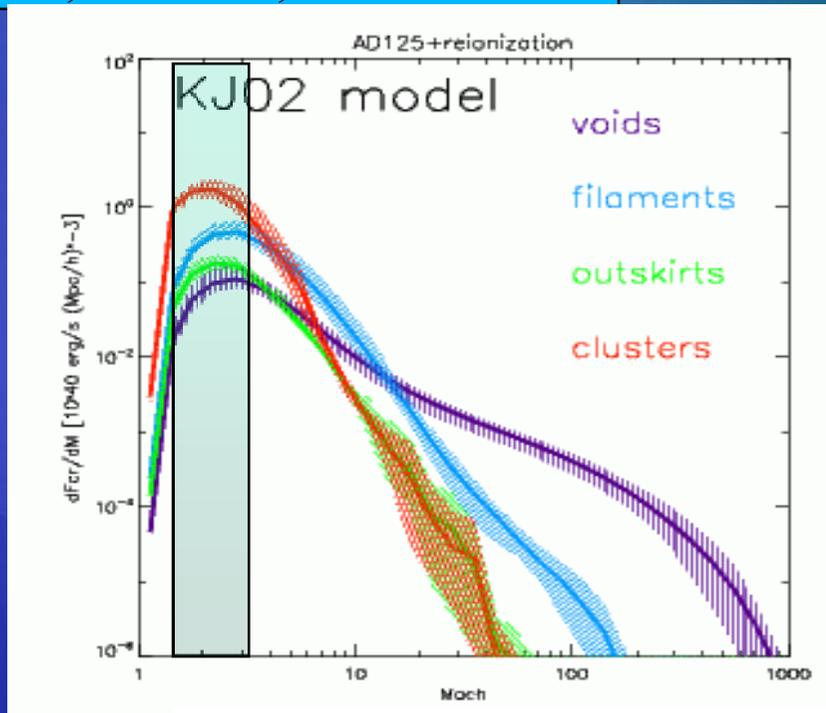
# Turbulence in the ICM



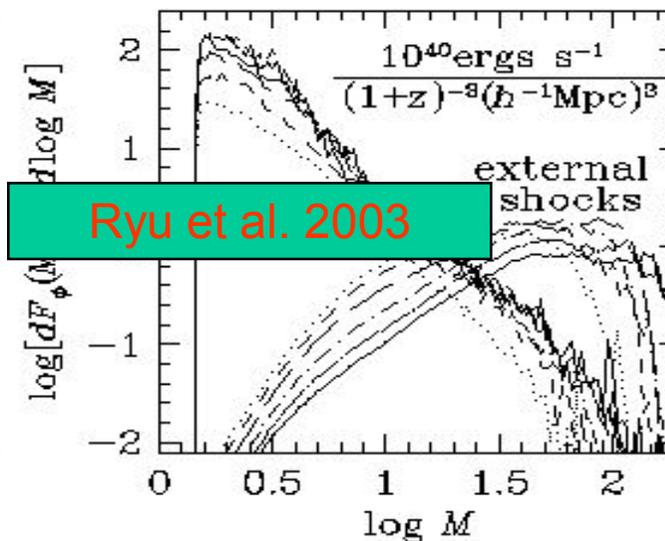
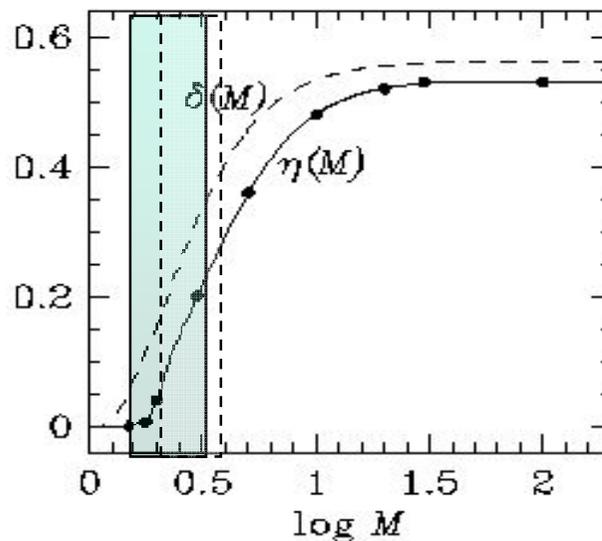
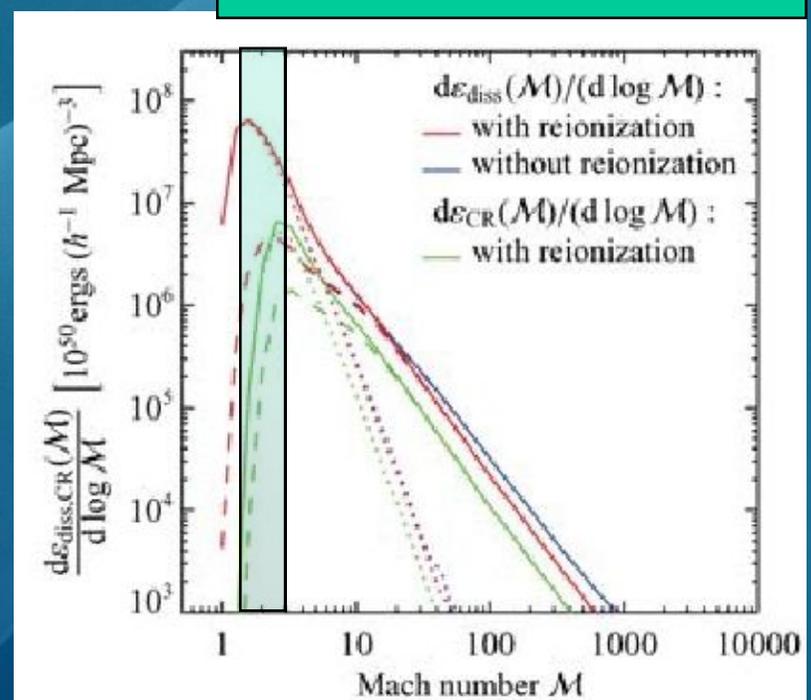
Roettiger +al. 1999

# Shocks in Galaxy Clusters (I)

Vazza, Brunetti, Gheller 2008

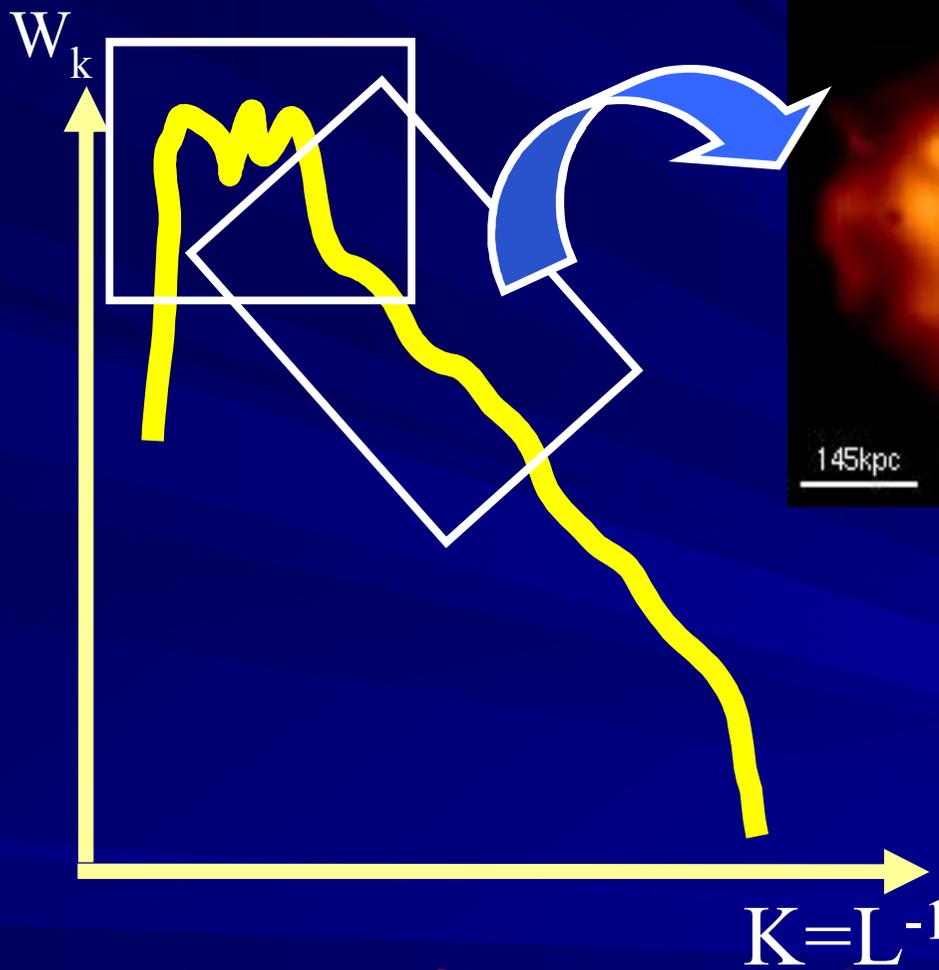


Pfrommer et al. 2008



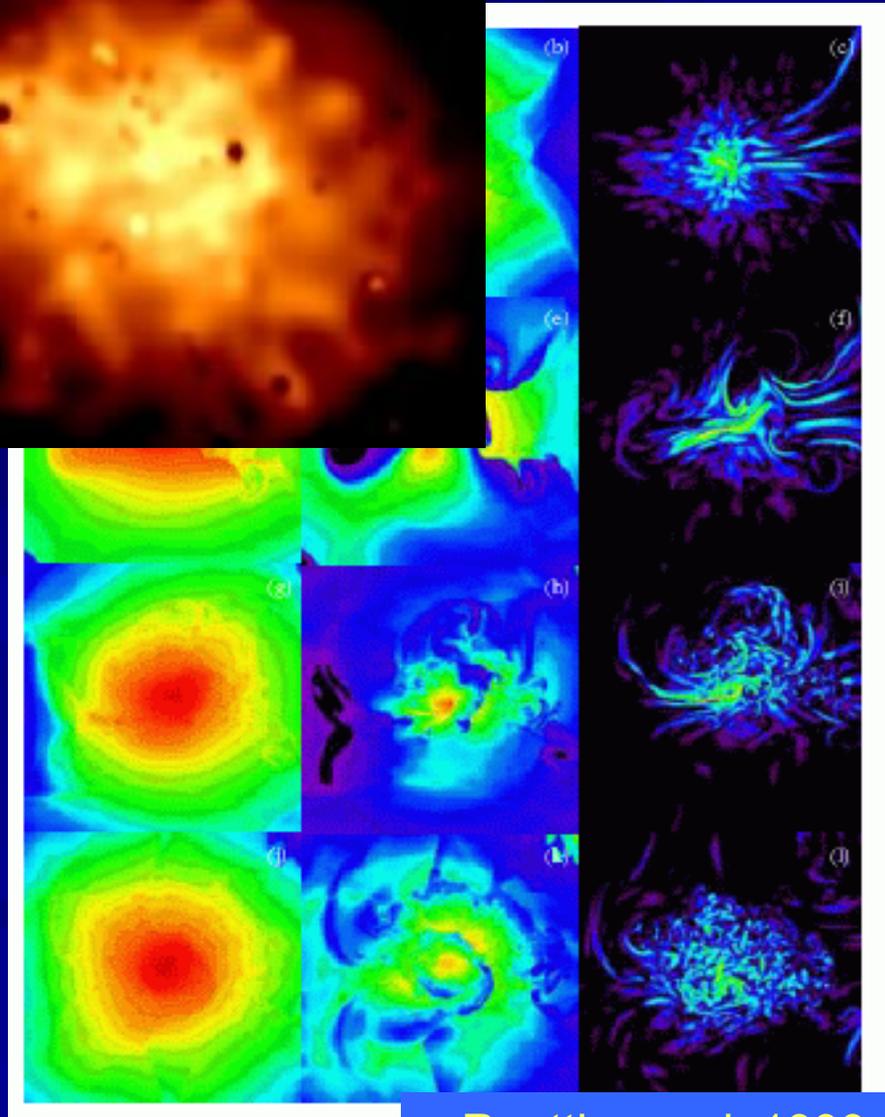
# Turbulence in the ICM

Schueker +al. 2004



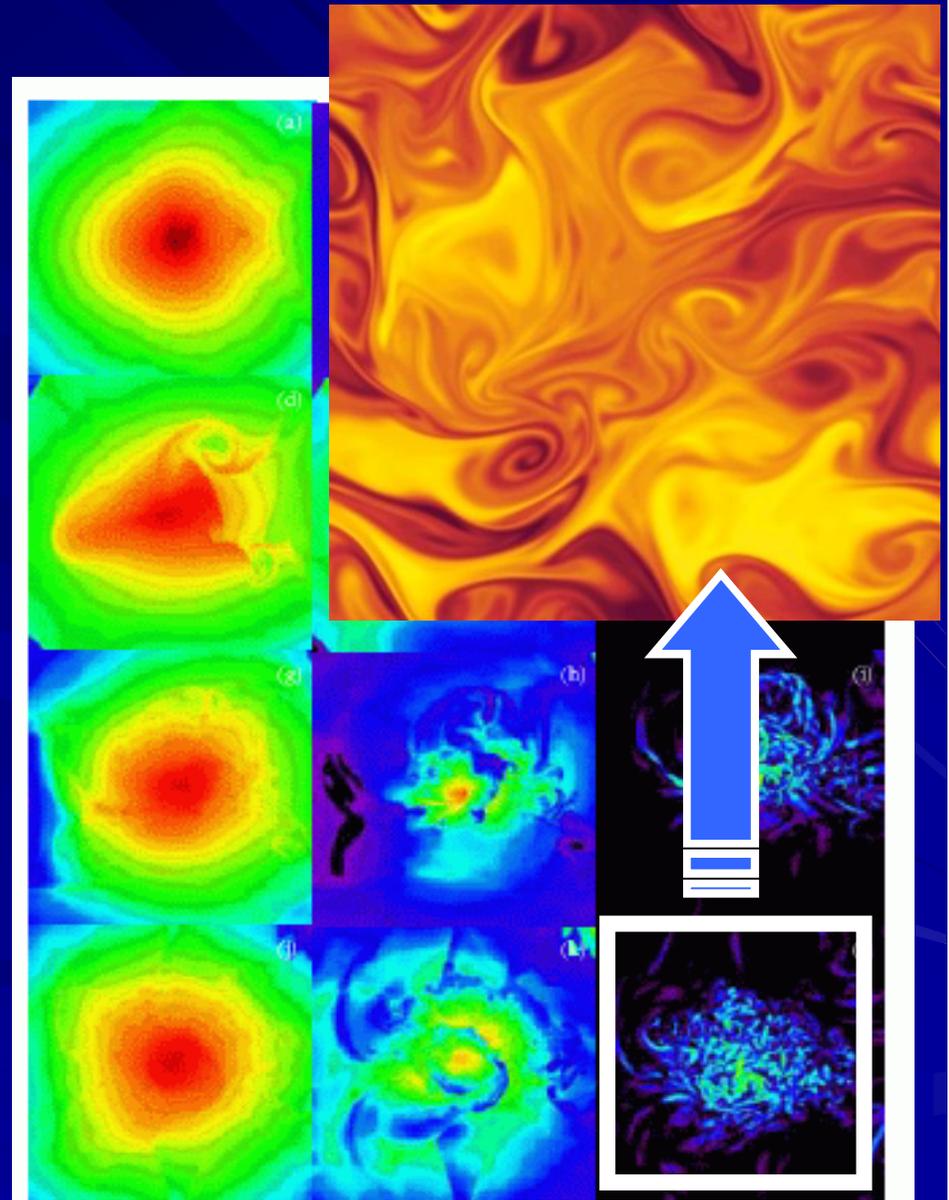
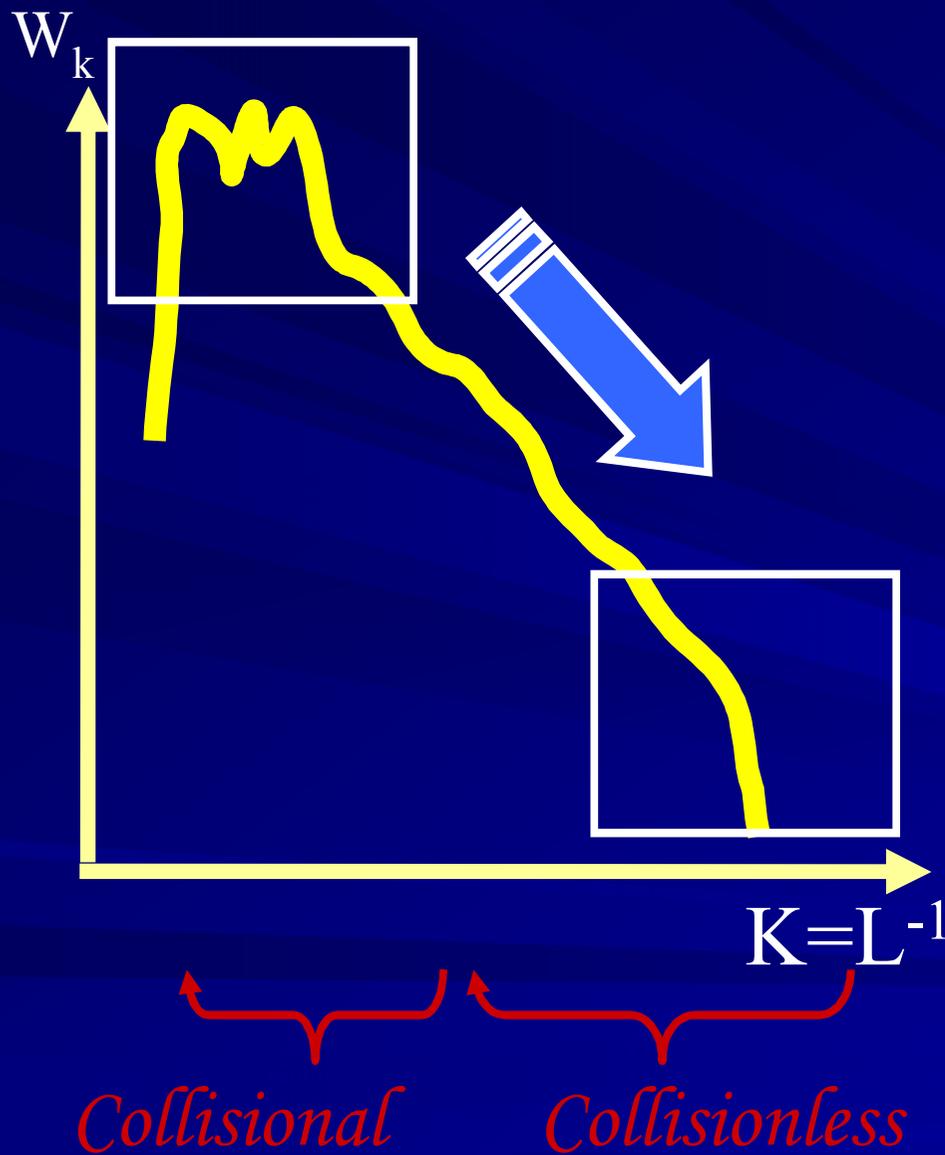
145kpc

*Collisional*      *Collisionless*

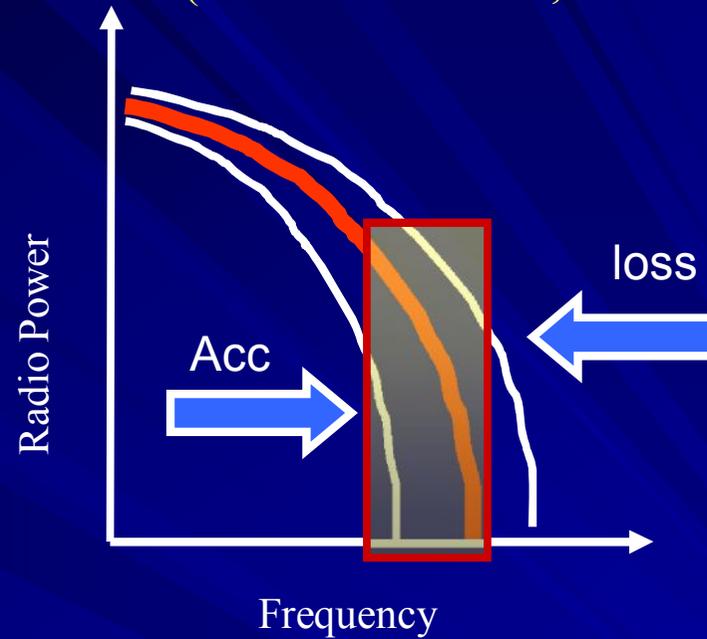
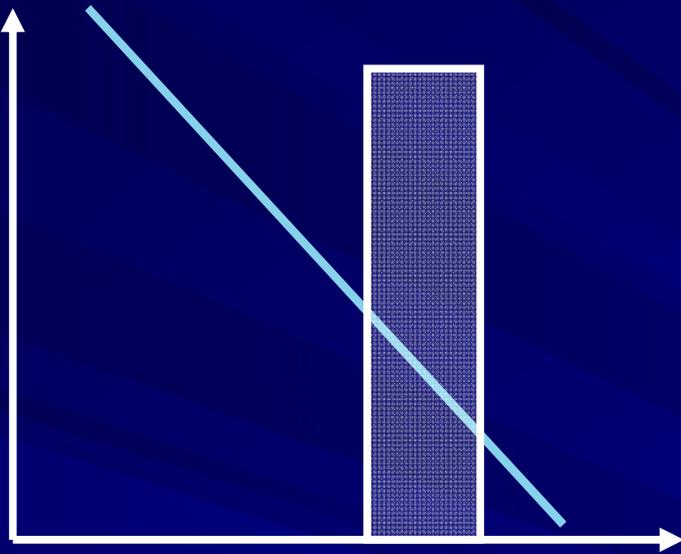


Roettiger +al. 1999

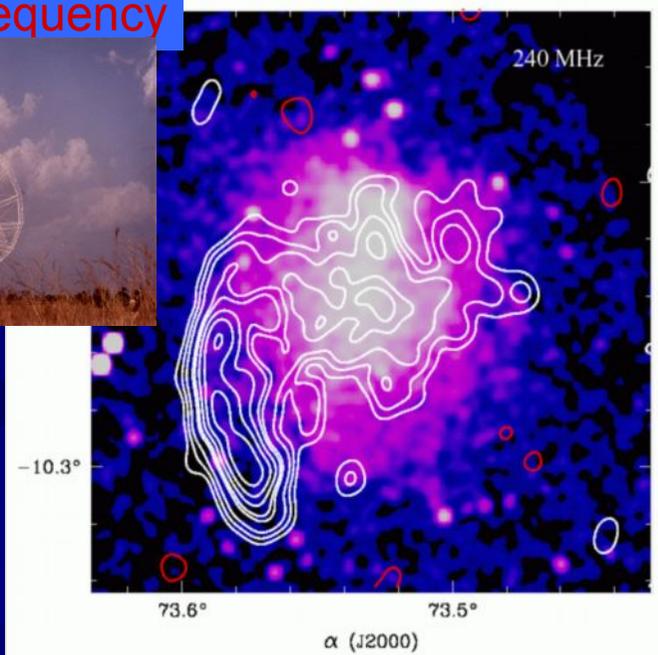
# Turbulence in the ICM



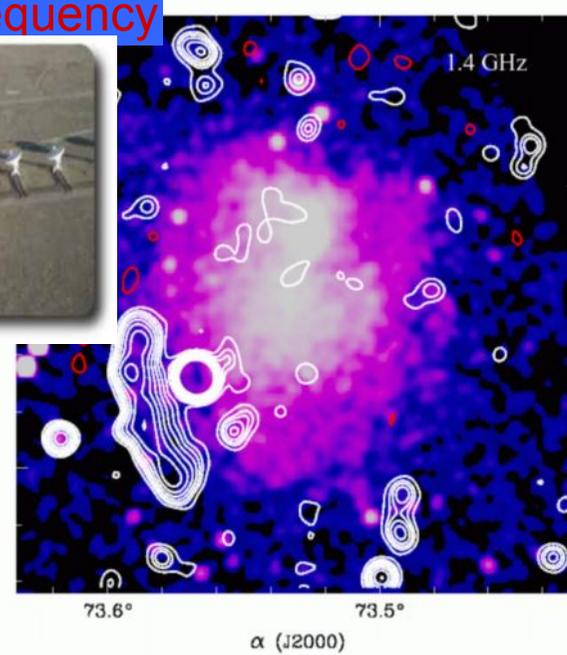
# Turbulent acceleration in GC (Brunetti +al. 2008, Nature 455,944)

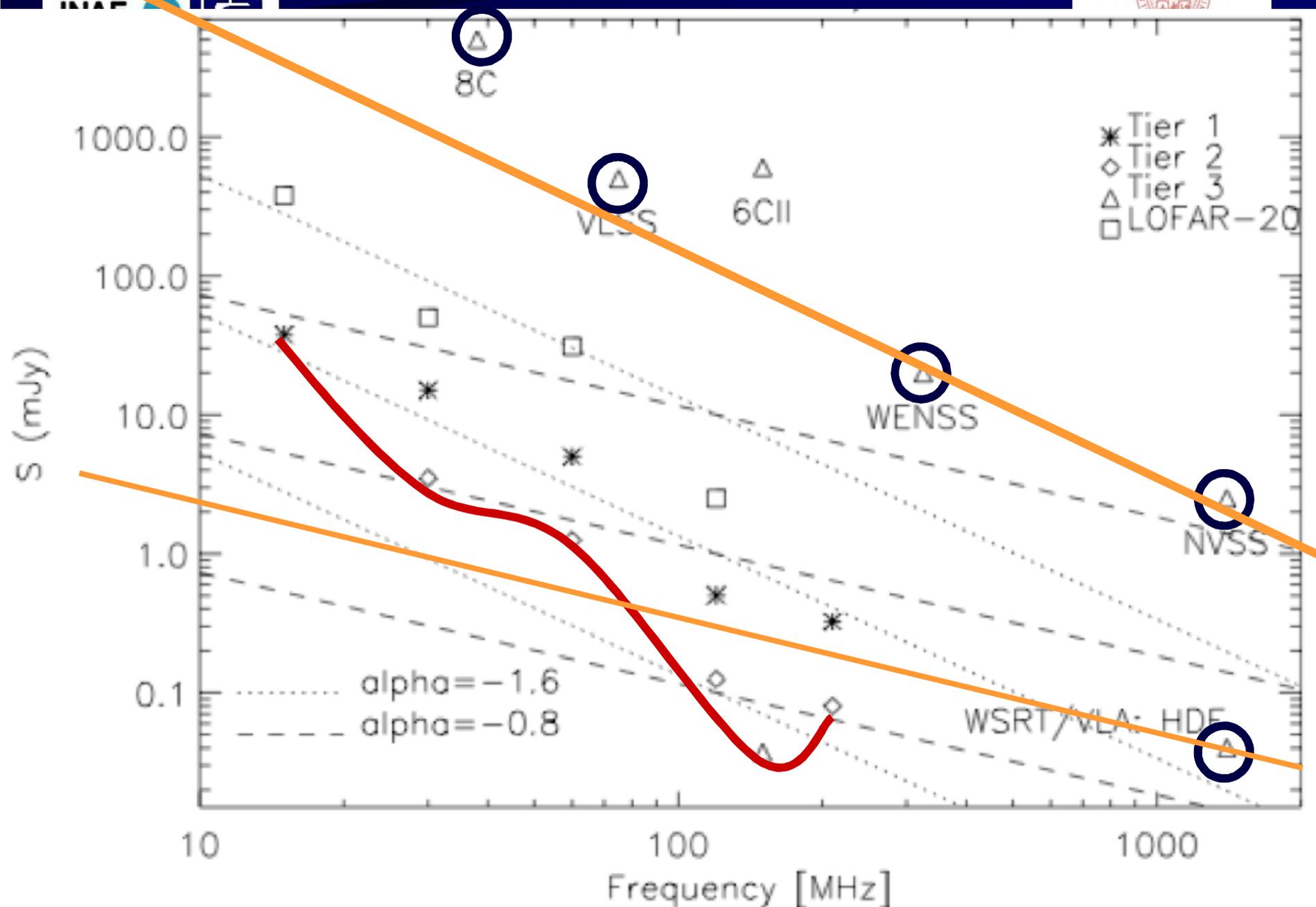


Low frequency



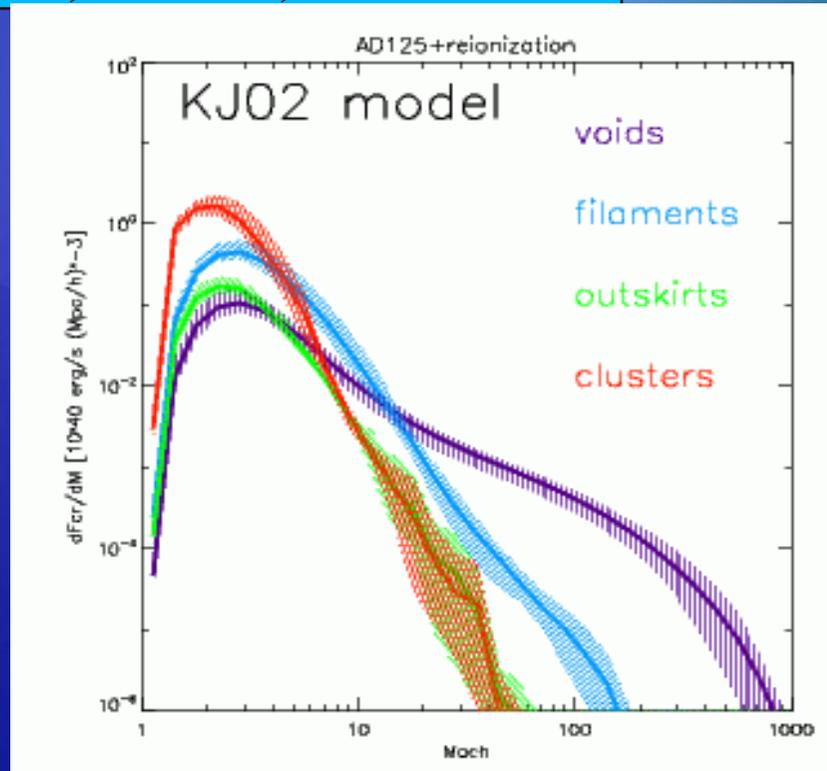
High frequency



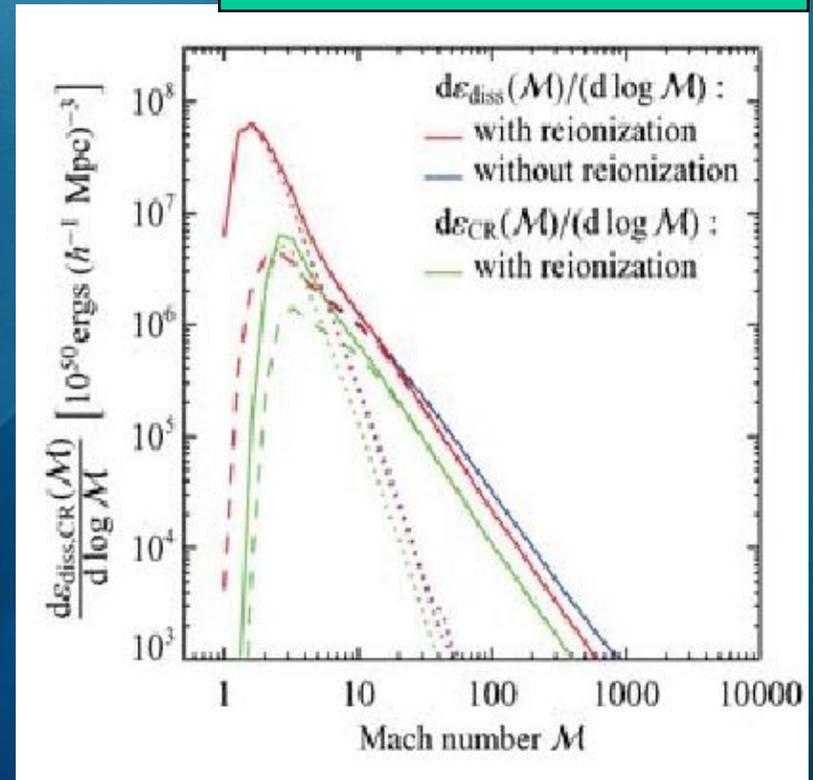


# Shocks in Galaxy Clusters

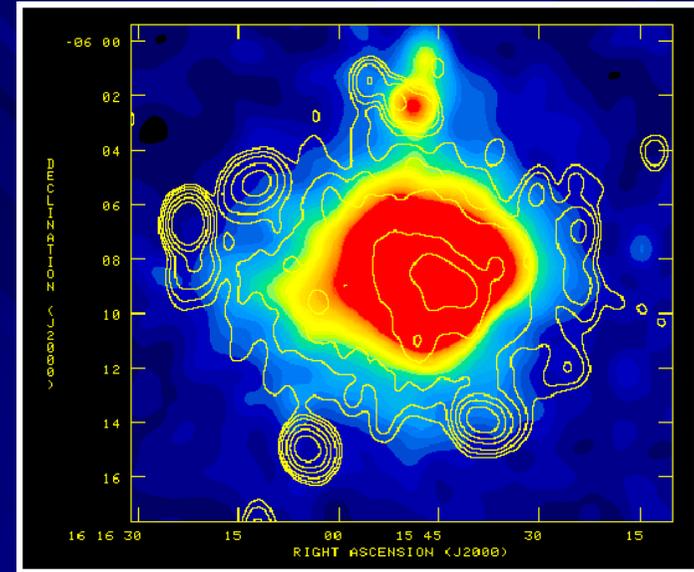
Vazza, Brunetti, Gheller 2008



Pfrommer et al. 2008



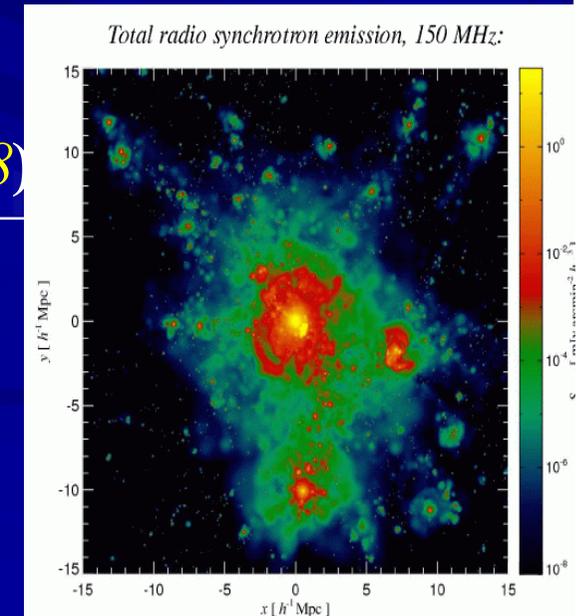
# Origin of the emitting electrons



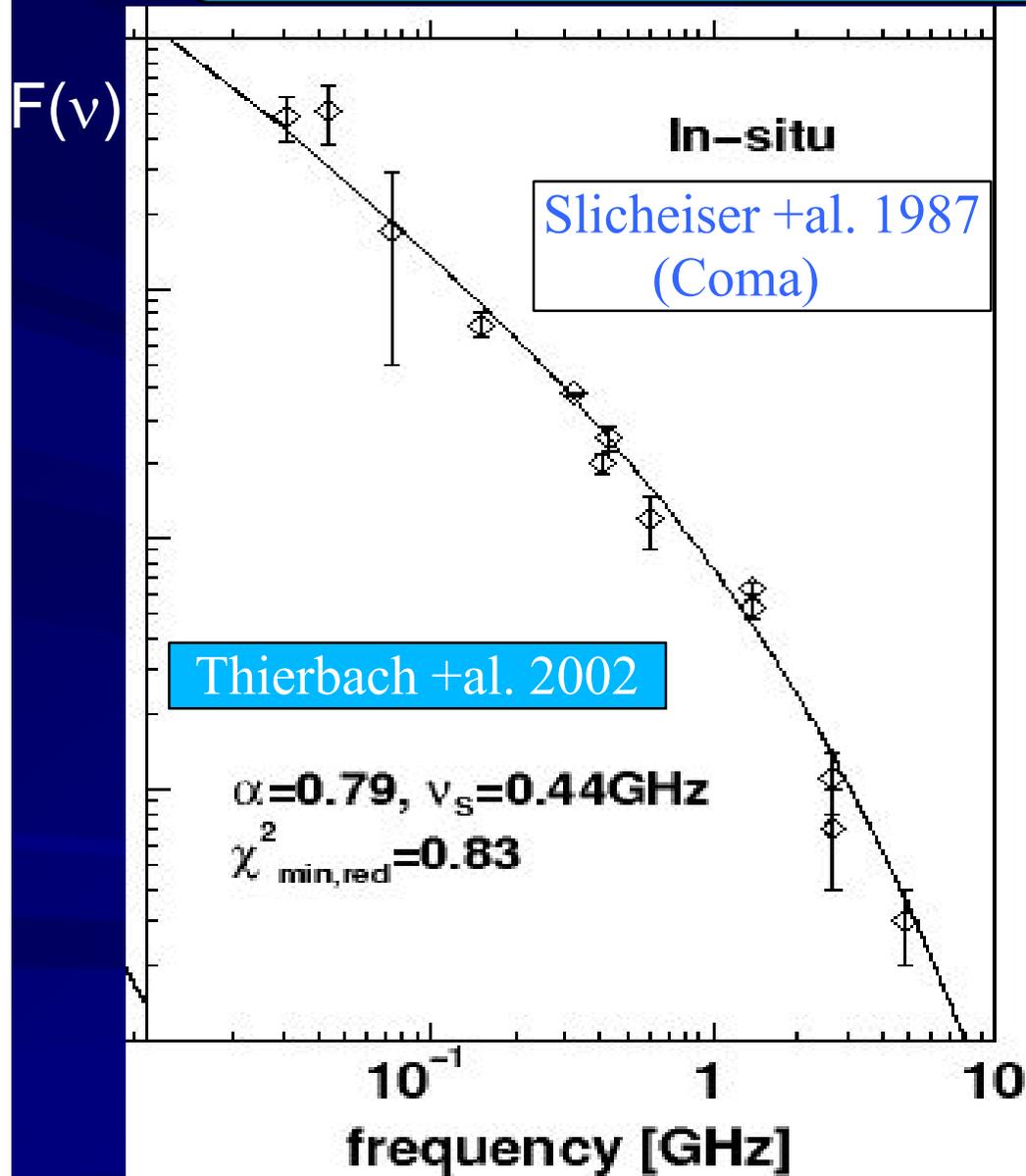
First possibility: *secondary models*, relativistic electrons continuously injected in the ICM by inelastic proton-proton collisions through productions and decay of charged pions (e.g., *Dennison 1980, Blasi & Colafrancesco 1999, Dolag & Ensslin 2000; Pfrommer & Ensslin 2004,08*)

Since protons accumulate in galaxy clusters and clusters are magnetised at  $\mu\text{G}$  level, we expect that the synchrotron emission from secondary electrons in the IGM should be common.

- Which is the level of this emission ?
- Are Radio Halos due to secondary emission ?

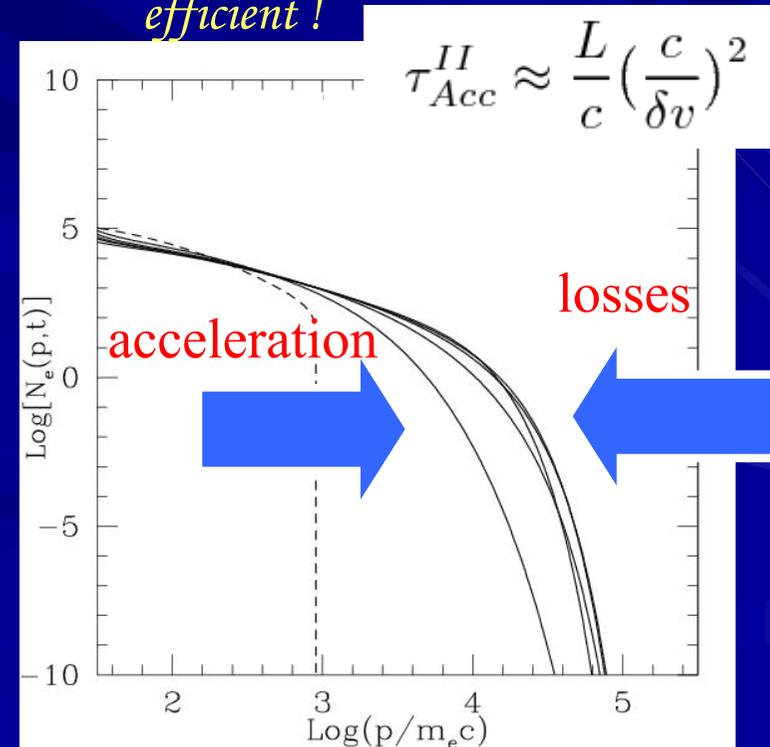


# Observations: Spectral Cut-Off

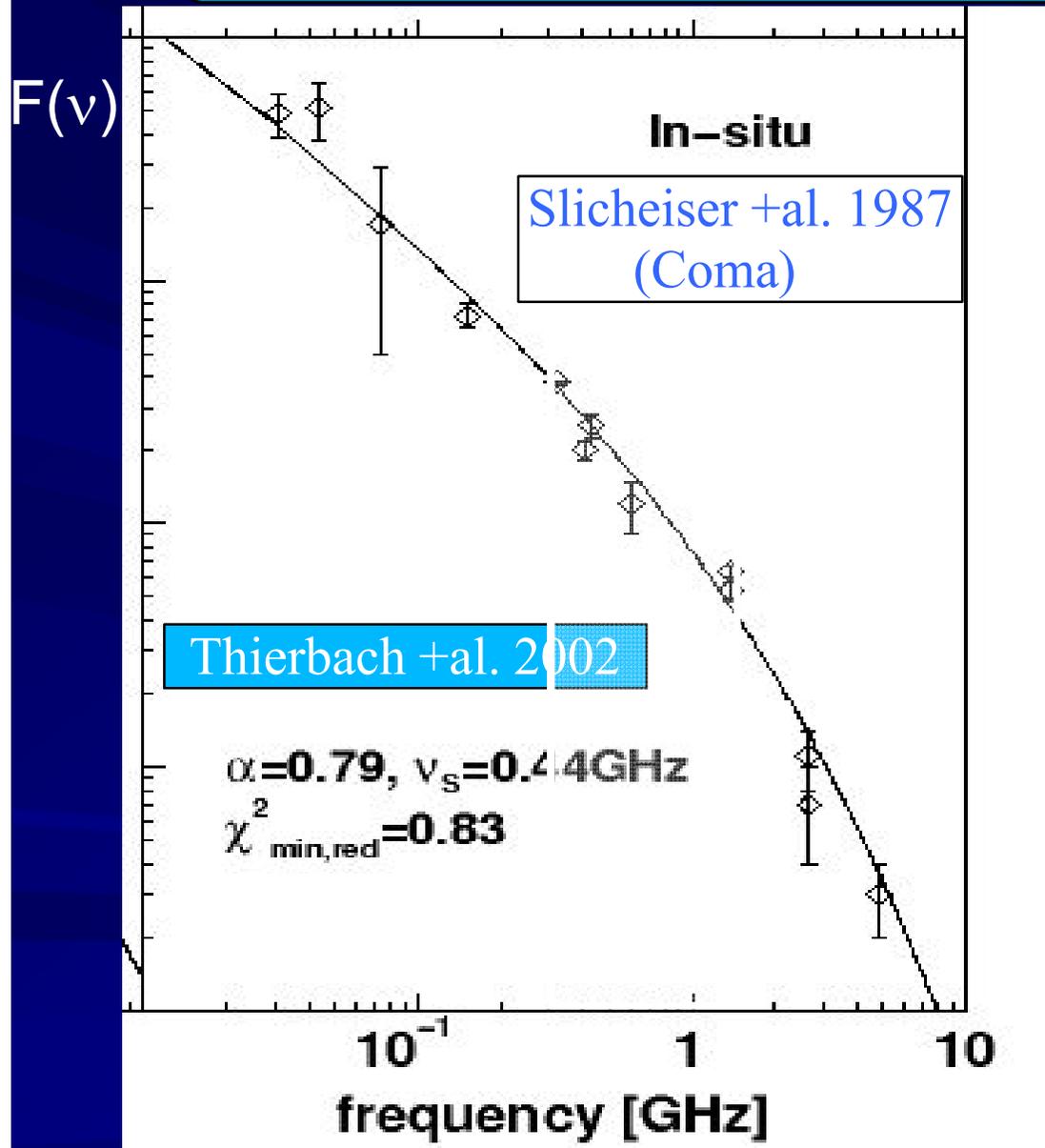


We expect a break in the spectrum of the emitting electrons at energies of few GeV

*Acceleration mechanism not efficient!*

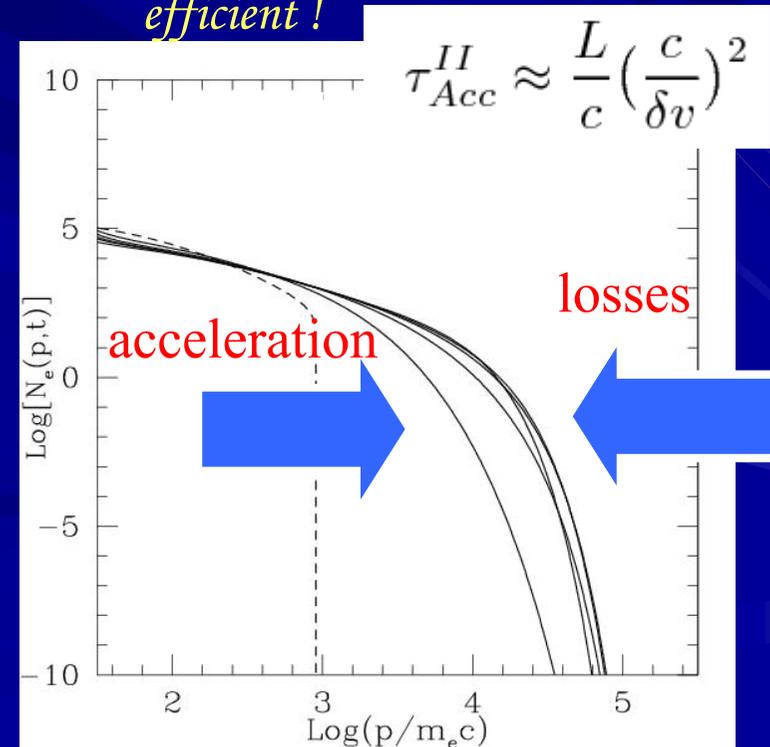


# Observations: Spectral Cut-Off

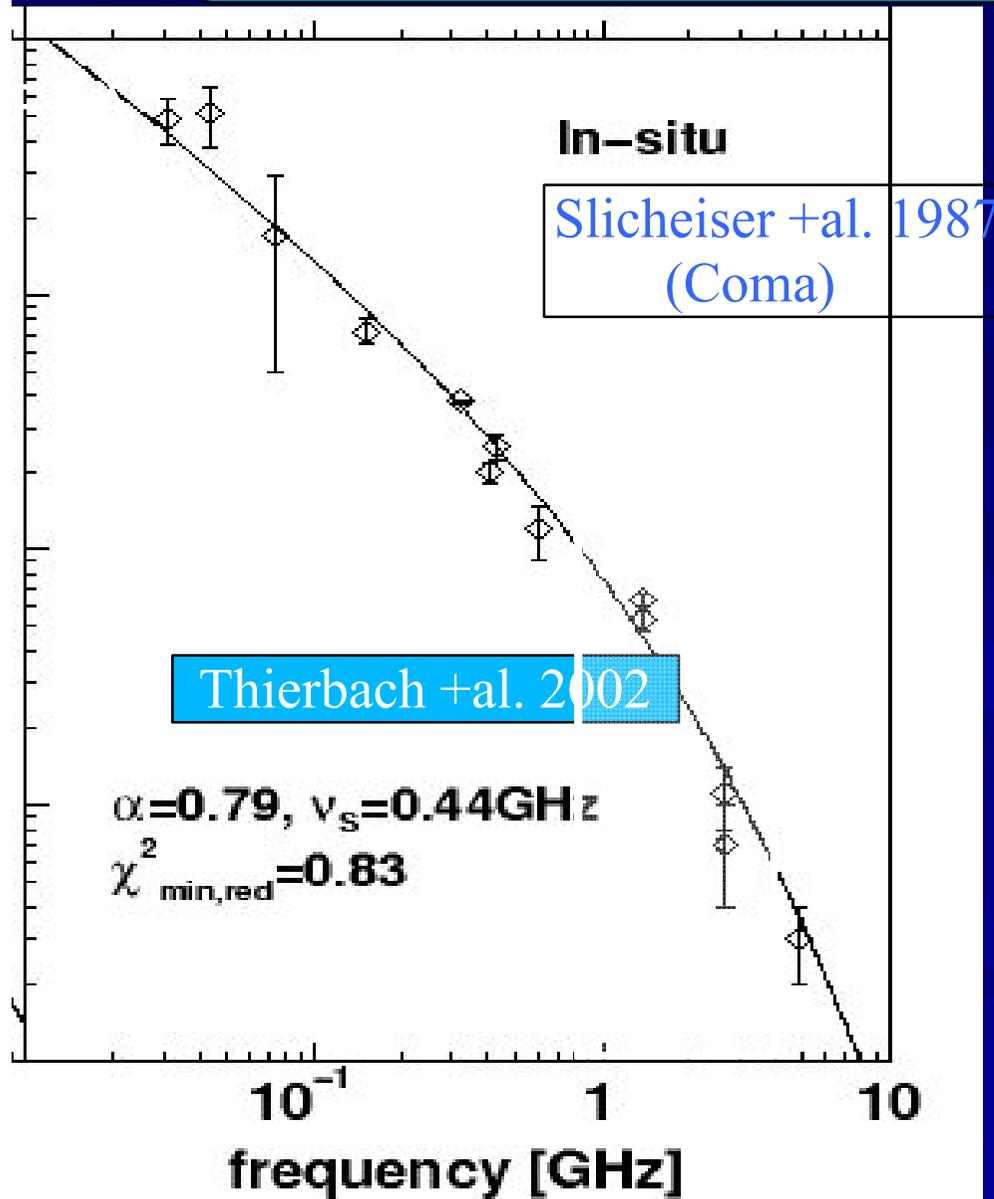


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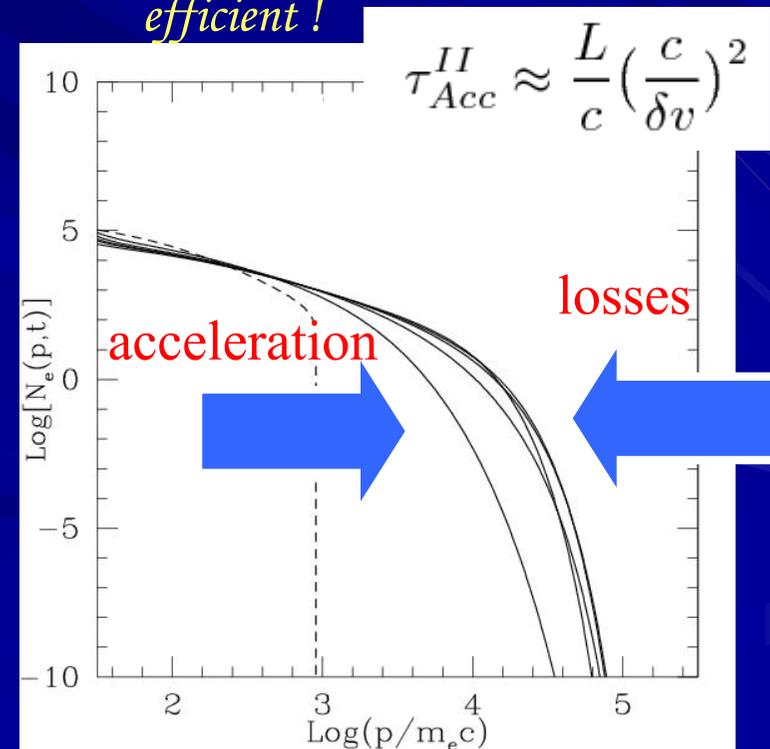


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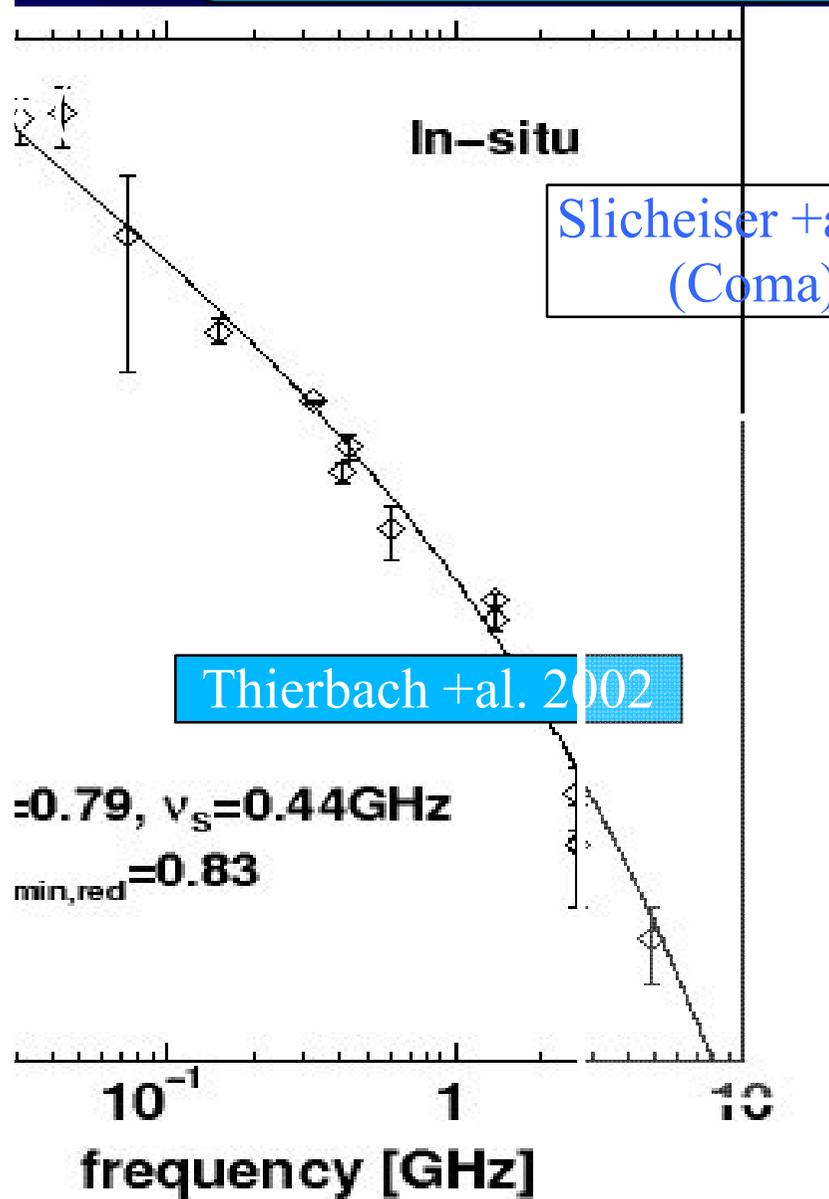


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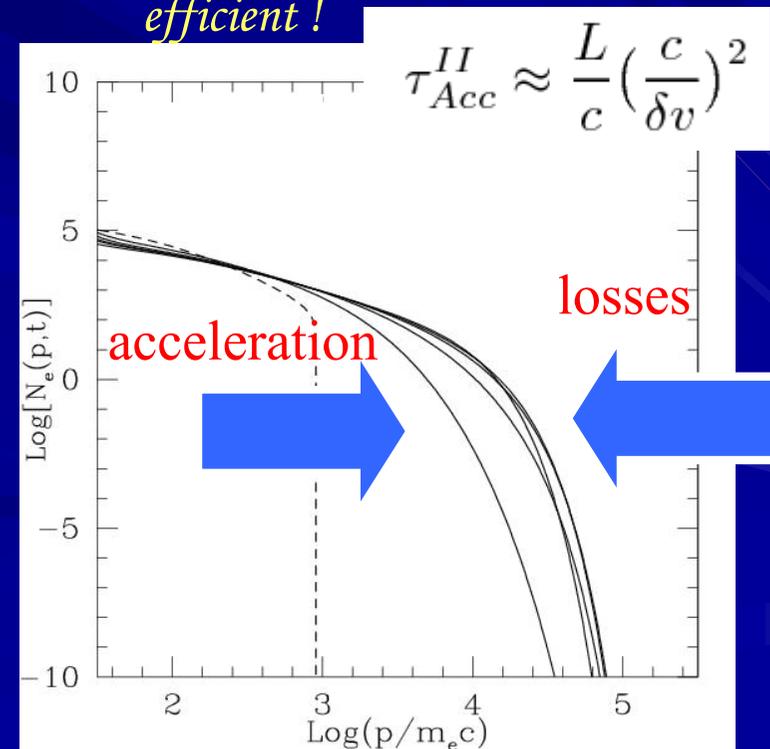


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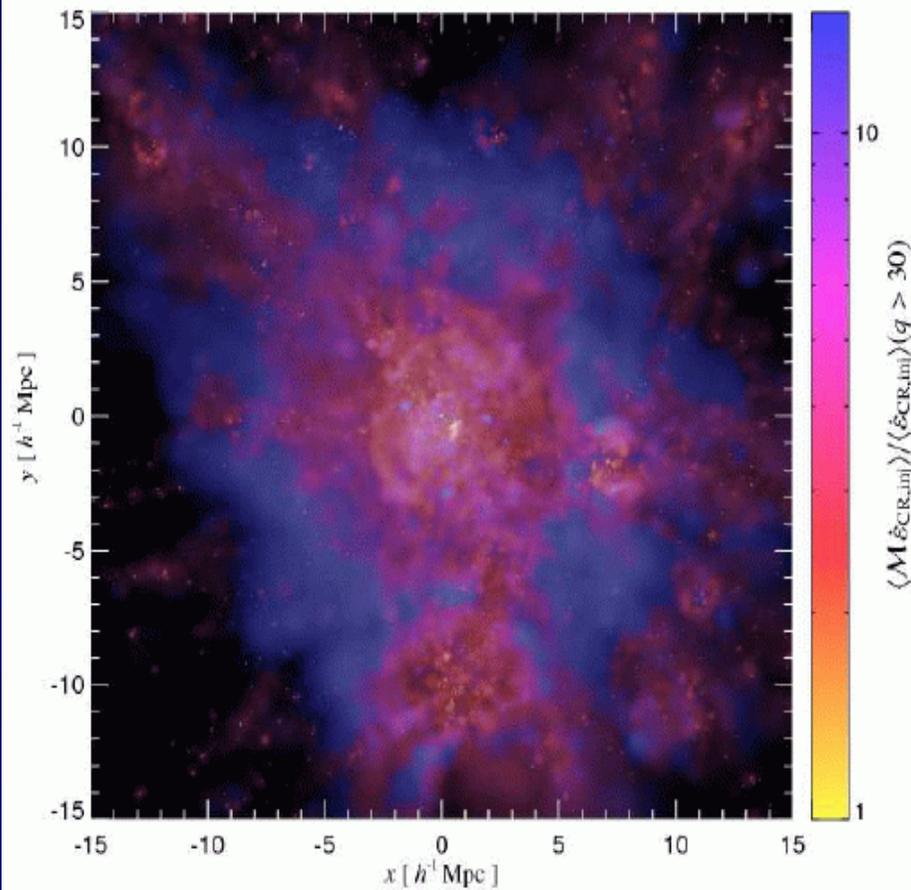
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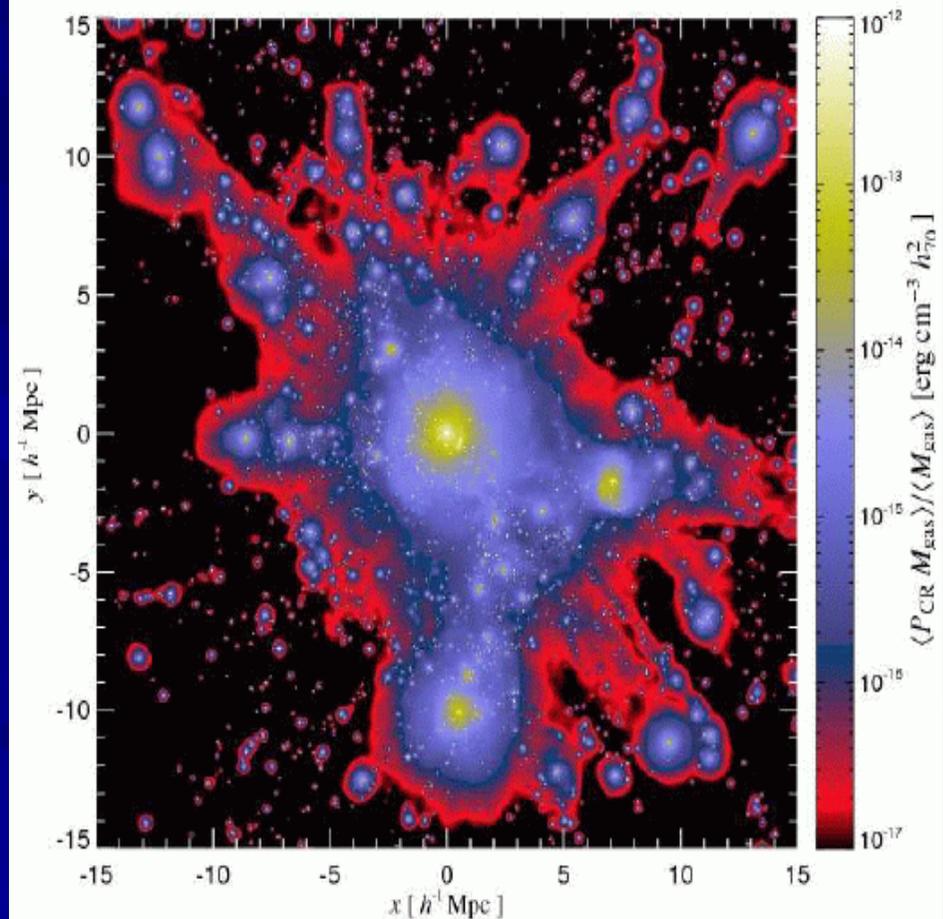
# Acceleration of CR at shocks

Pfrommer et al. 2007, 08

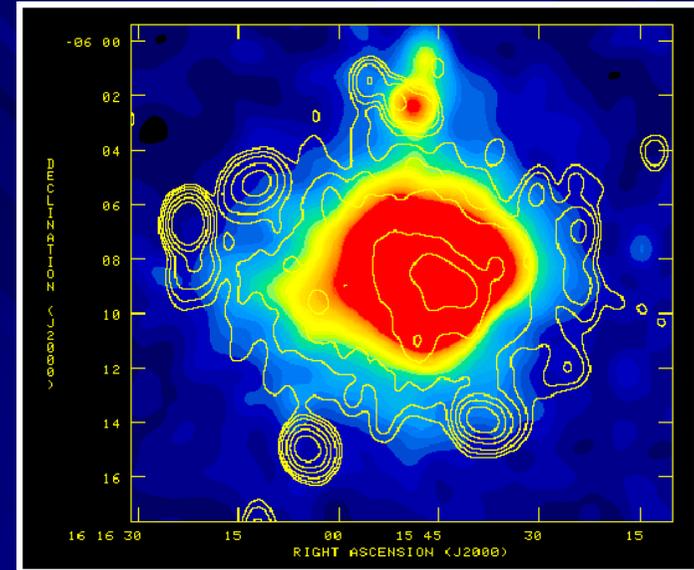
*Shock Mach numbers weighted by  $\dot{\epsilon}_{\text{CR,inj}}$ :*



*CR proton pressure:*



# Origin of the emitting electrons

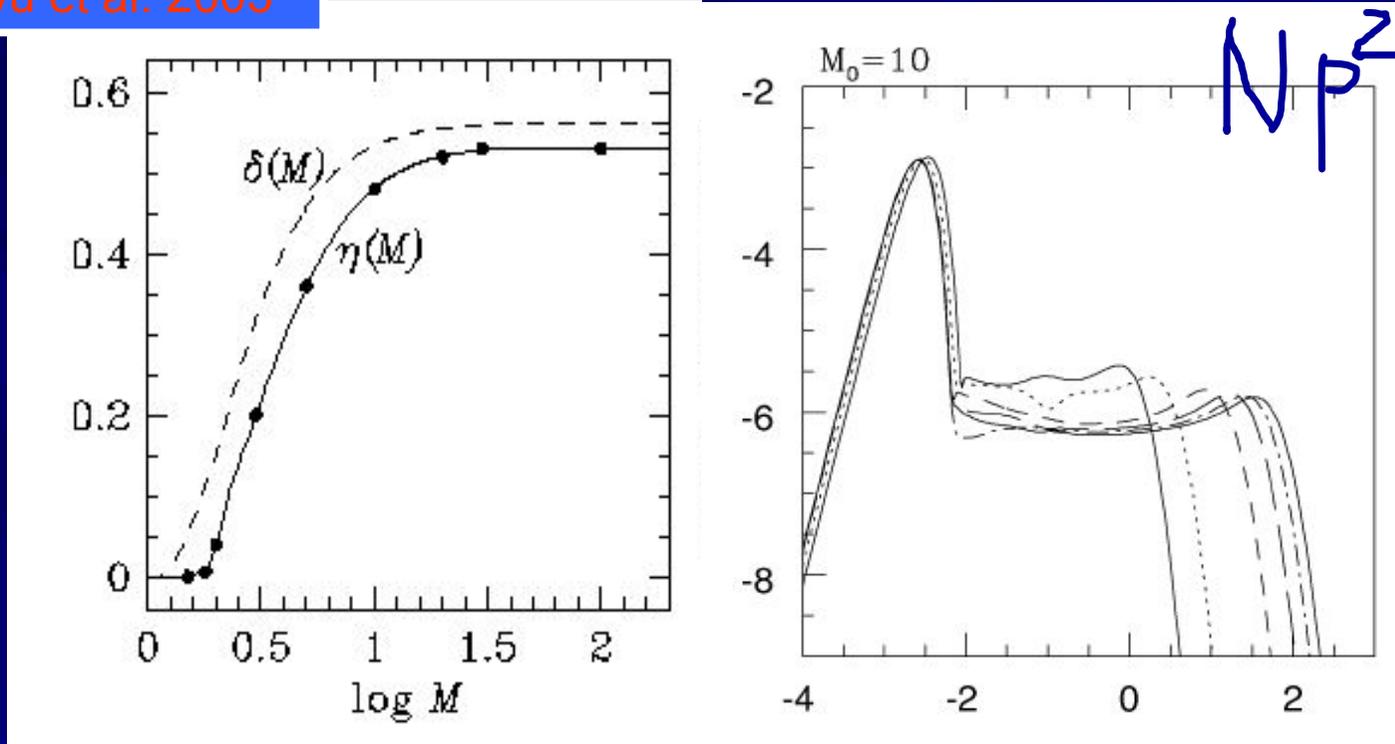


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Second possibility : *in situ re-acceleration* by MHD turbulence developed in the cluster volume during the merger events (e.g., *Brunetti et al. 2001, 2004; Petrosian 2001; Ohno et al. 2002; Fujita et al. 2003; Brunetti & Blasi 2005; Cassano & Brunetti 2005; Brunetti & Lazarian 2007; Petrosian & Bykov 2008*)

# Acceleration of CRp at shocks

Ryu et al. 2003

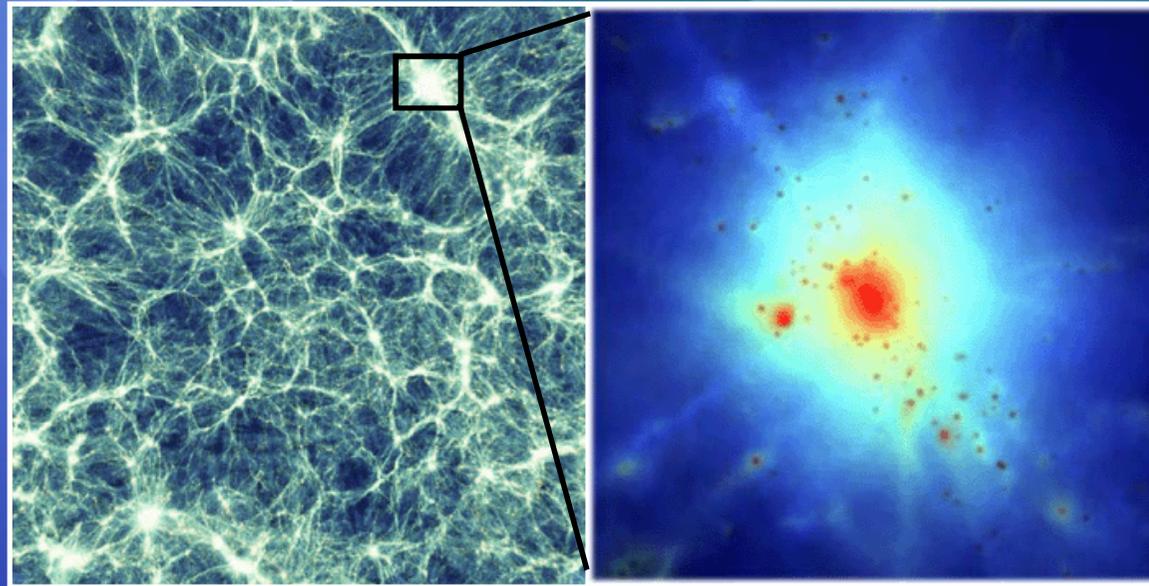


$$E_{CR} \approx \eta(M) \rho v_{sh}^3$$

From SN and our Galaxy electrons take 1-10% of the proton energy.

# Clusters of galaxies

How galaxy clusters form?

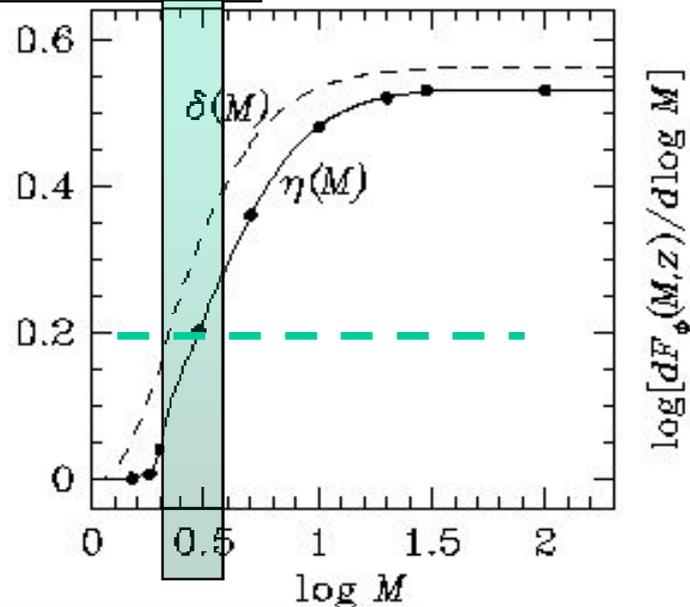


Borgani et al. 2004

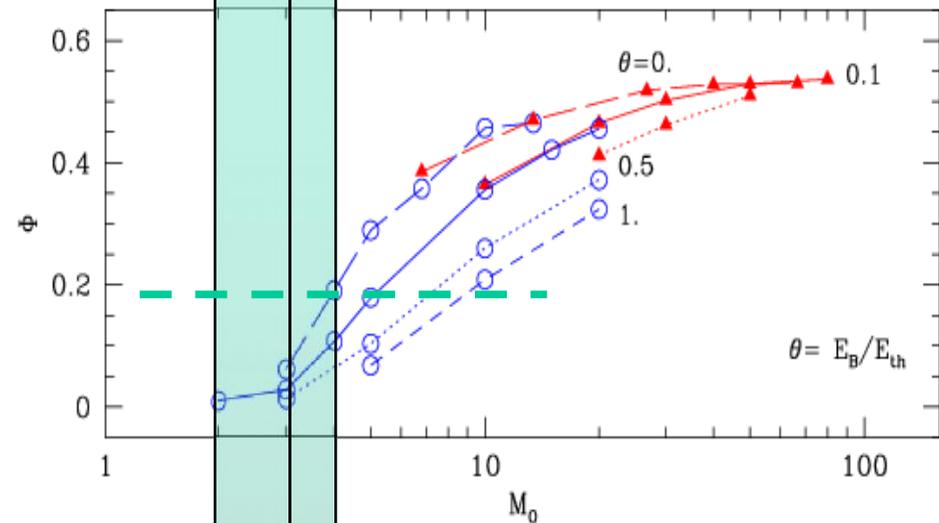
- Cosmic structures form as a result of the gravitational amplification of primordial density fluctuations.
- Clusters form by **accretion** of matter and **mergers** between sub-units at the intersection of filaments which make up the ‘cosmic web’.
- Gas falling into deep potential wells is heated to  $\sim 10^7\text{-}10^8$  K by **shocks** (and adiabatic compression)

# Acceleration of CRp at shocks

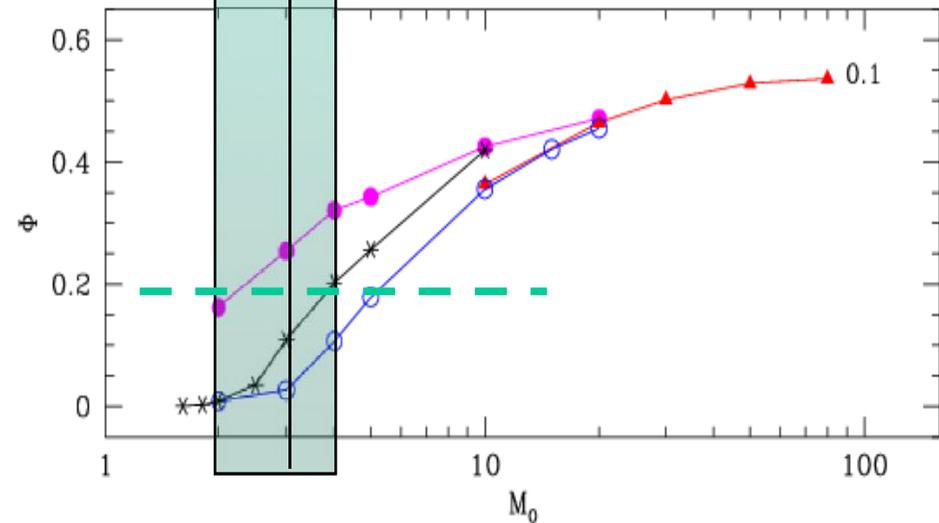
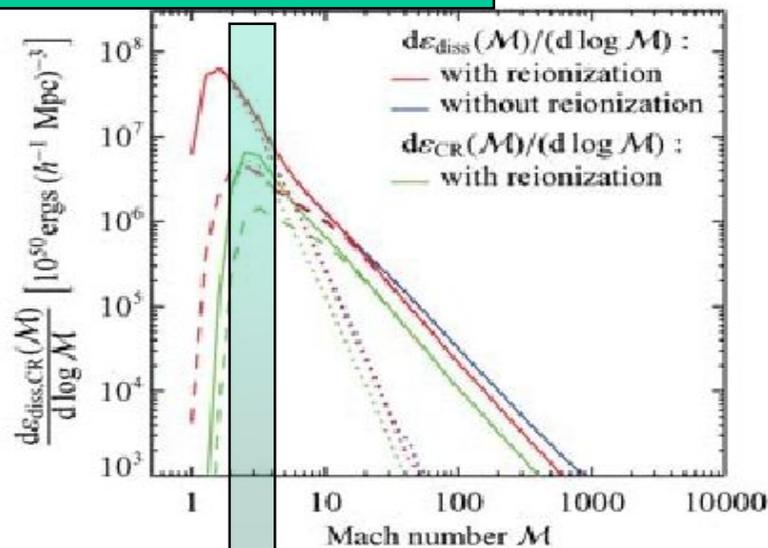
Ryu et al. 2003



Kang & Jones 2007



Pfrommer et al. 2008



## II - Conclusion

- (a) Protons are expected the dominant CR population in the IGM : they result from the accumulation of CR from the epoch of formation of galaxy clusters
- (b) Despite (a) we have only upper limits to the energy content in the form of CR protons

# Not only particle acceleration ....

**Thermal conduction and kin. viscosity in the ICM**

**(e.g., Lazarian 2006)**

**Heating of the ICM and “cooling flow” problem**

**(e.g., Fujita , Matsumoto, Weda 2004)**

**Diffusion and transport of metals in the ICM**

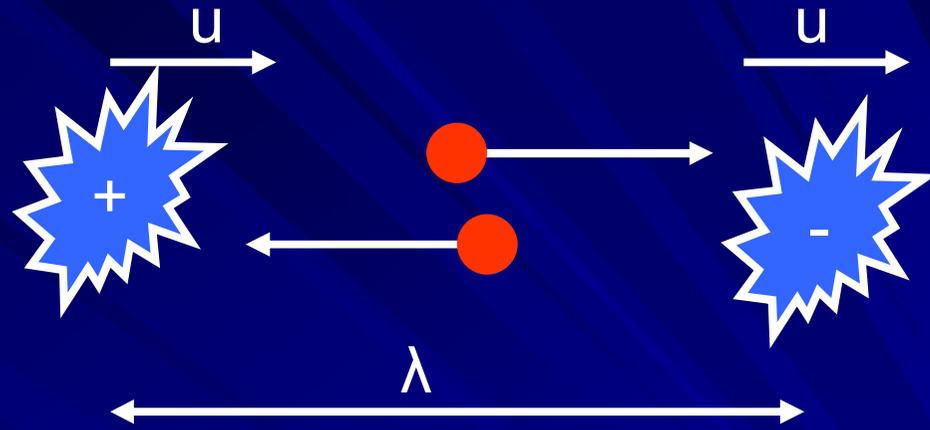
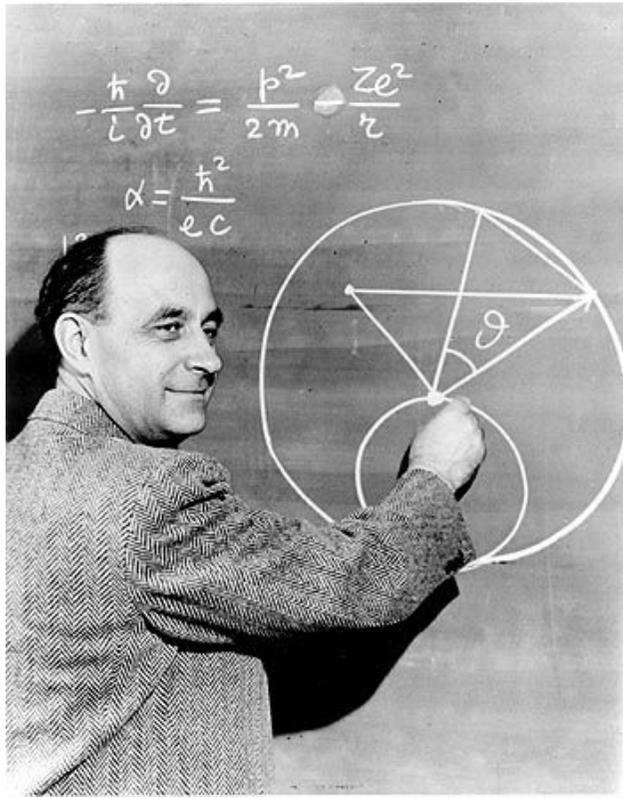
**(e.g., Voigt & Fabian 2004; Rebusco +al. 2005)**

**B-Amplification from Cosmological seed fields**

**(e.g., Dolag +al. 1999,02; Subramanian +al. 2006)**

**Diffusion and scattering of HE & UHECR in the Universe**

**(e.g., Sigl +al. 2005; Dolag +al. 2005)**



$$\Delta p_{\pm} \approx \pm 2 p \frac{u}{c}$$

$$v_{+} = \frac{u + c}{\lambda} \quad v_{-} = \frac{c - u}{\lambda}$$

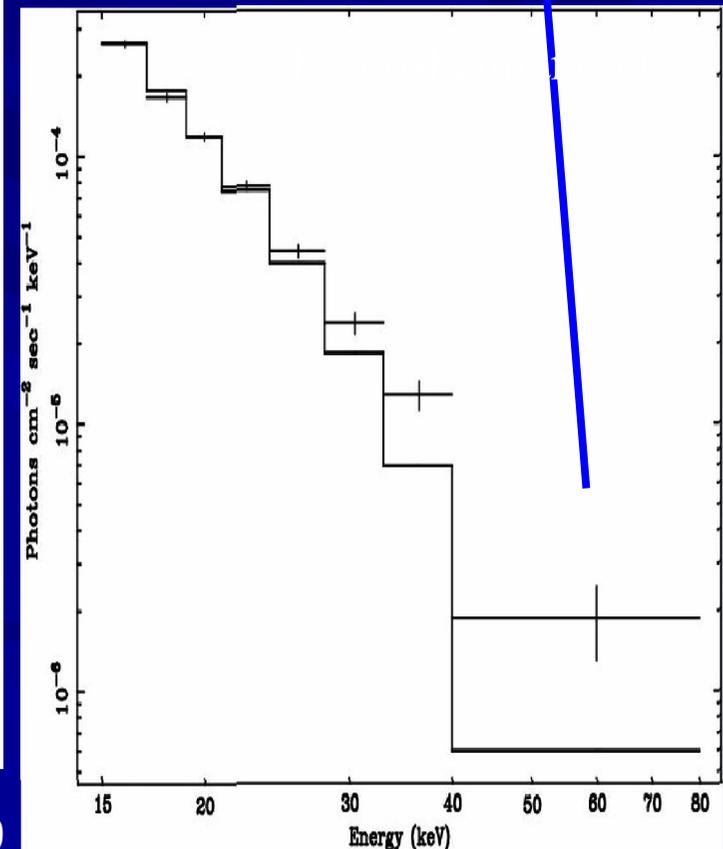
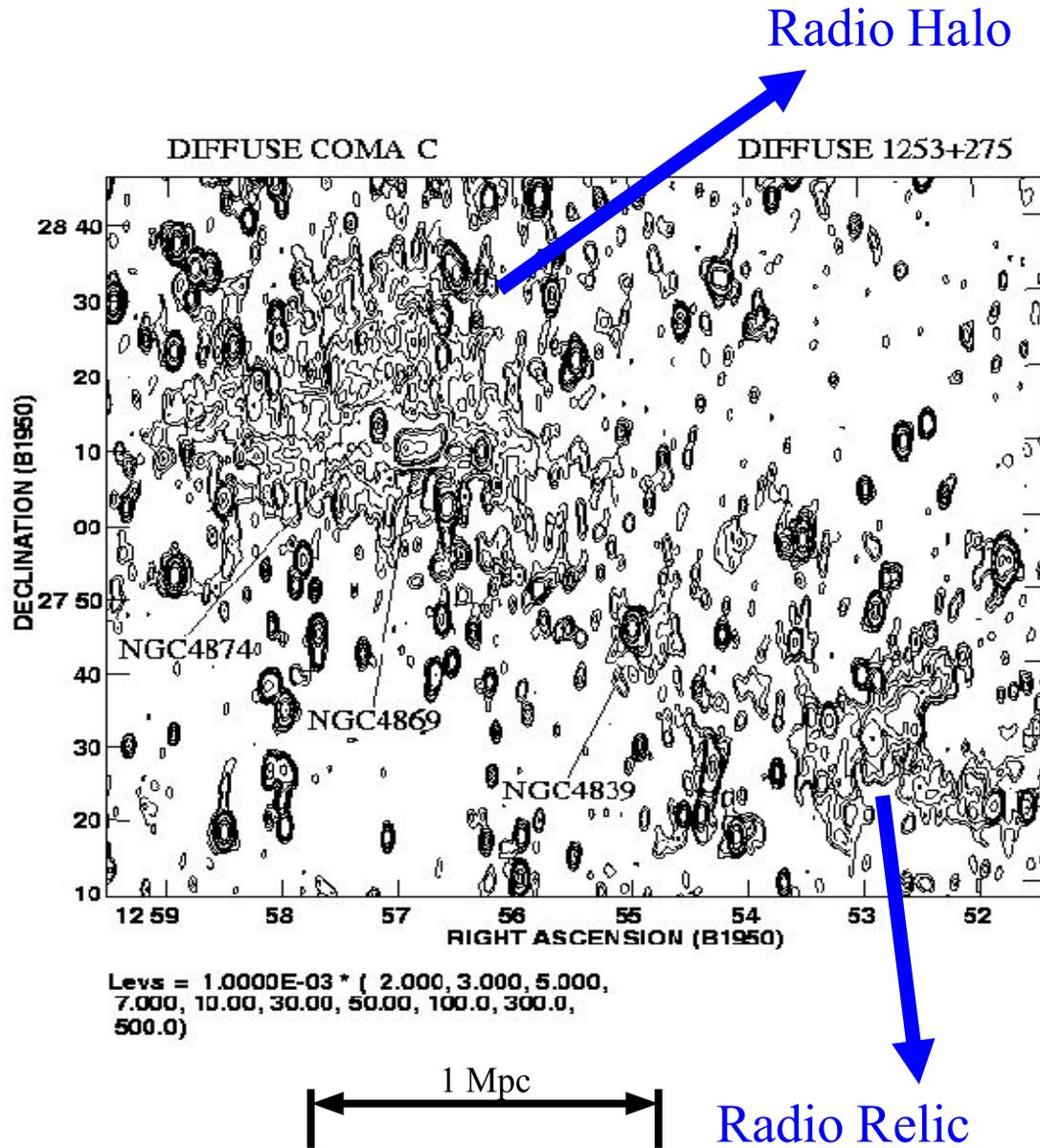
$$\left\langle \frac{\Delta p}{\Delta t} \right\rangle = v_{+} \Delta p_{+} + v_{-} \Delta p_{-} \approx 2 p \frac{u^2}{c^2} \frac{c}{\lambda}$$

$$\left\langle \frac{\Delta p}{\Delta t} \right\rangle \approx 2 p \frac{u}{c} \frac{c}{\lambda}$$

# COMA

## Hard X-ray Excess (HXR)

it may be due to IC emission from the same radio emitting electrons



Fusco-Femiano +al. 1999,04; Rephaeli +al. 1999

# CR populations in GC

- Long living population of CR protons

$$p + p \rightarrow \pi^0 + \pi^+ + \pi^- + \text{anything}$$

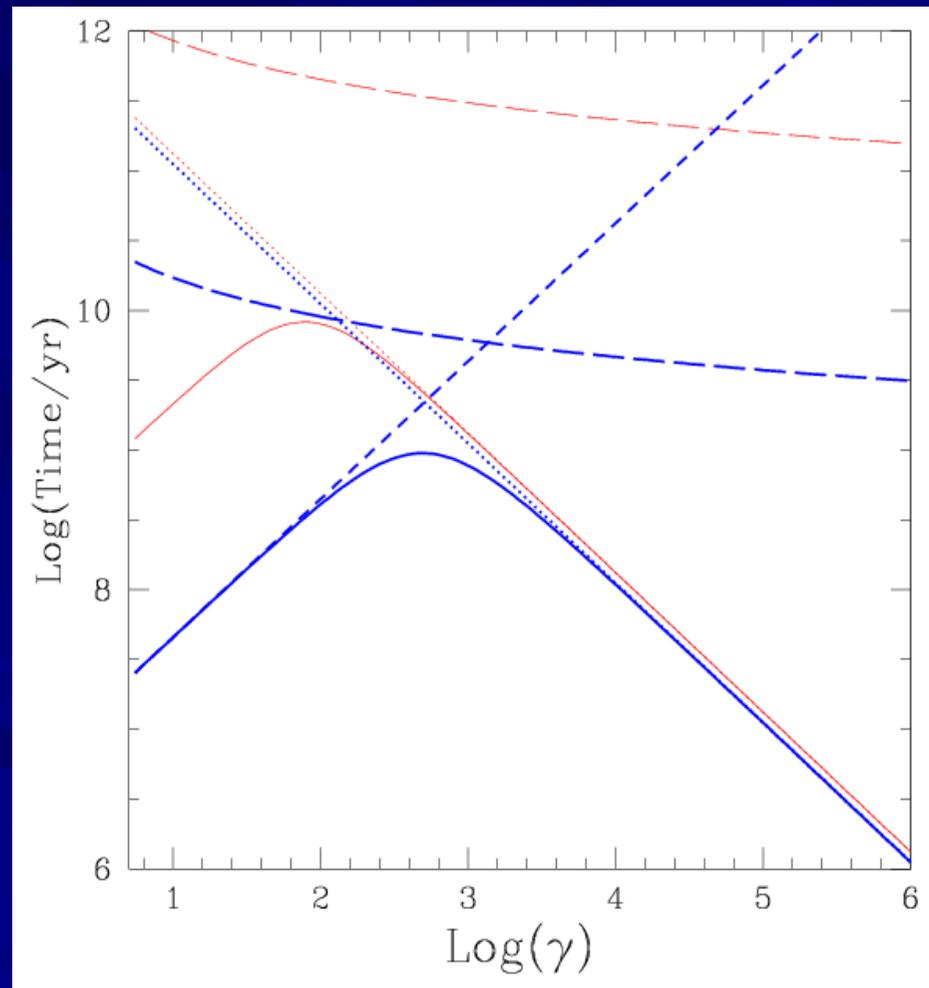
$$\pi^0 \rightarrow \gamma\gamma$$

$$\pi^\pm \rightarrow \mu + \nu_\mu \quad \mu^\pm \rightarrow e^\pm \nu_\mu \nu_e.$$

- Stationary (continuous injection) population of CR (secondary) electrons
- Transient population of CR electrons ( $< 1$  Gyr)

# Physics of CR Leptons

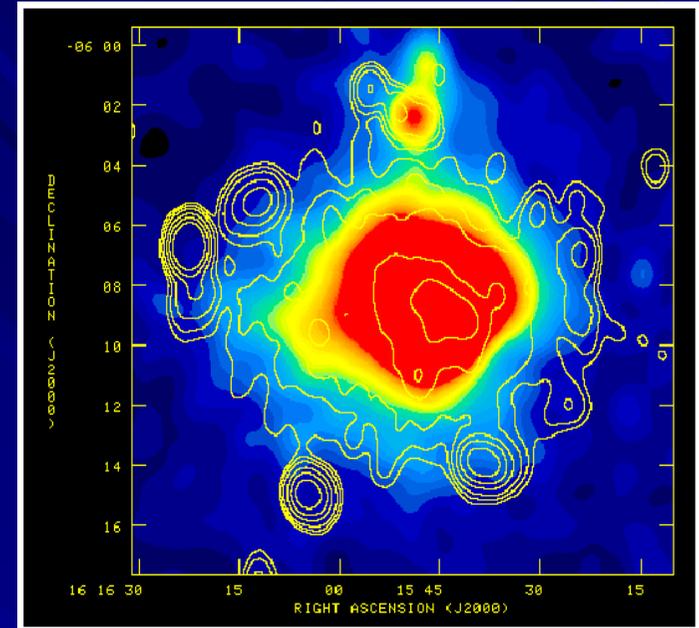
$$(dE/dt) \sim \mathbf{E} / \mathbf{Time} \sim m_e c^2 b$$



# *Diffuse Radio Emission & origin of emitting electrons*

(G.Brunetti, T.Venturi, S.Giacintucci, R.Cassano, D.Dallacasa, G.Setti, R.Athreya, N.Kassim, W.Lane, K.Dolag, S.Bardelli, B.Cotton, P.Mazzotta, M.Markevitch)

GMRT

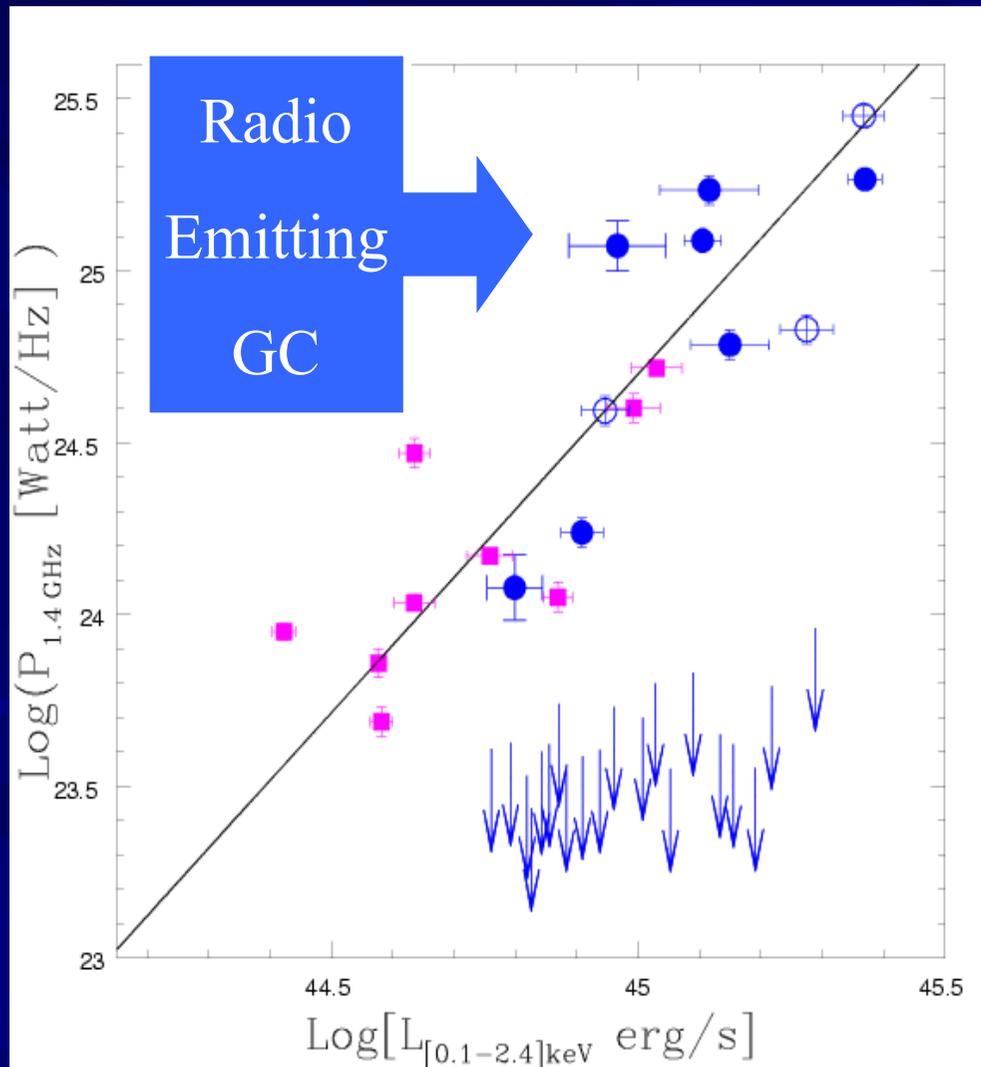


Sample of  
50 massive GC  $z=0.2-0.4$   
(REFLEX + eBCS)

Similar  $z$   
Similar X-luminosities

# Radio- Statistical properties of GC

Brunetti +al. 2007



➤ RH are not common

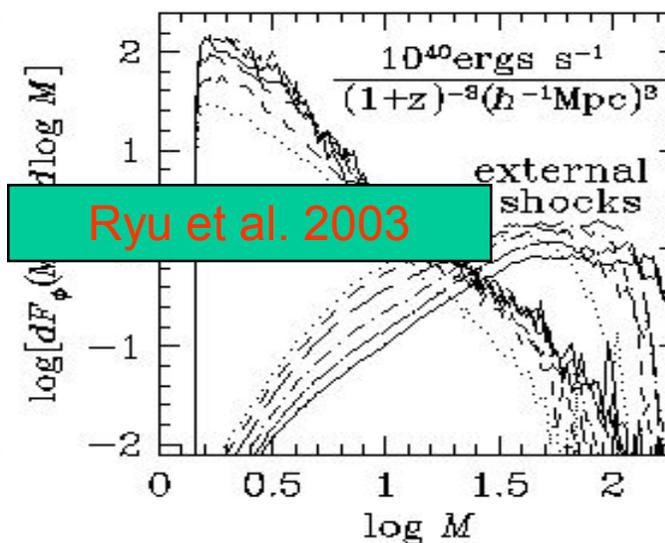
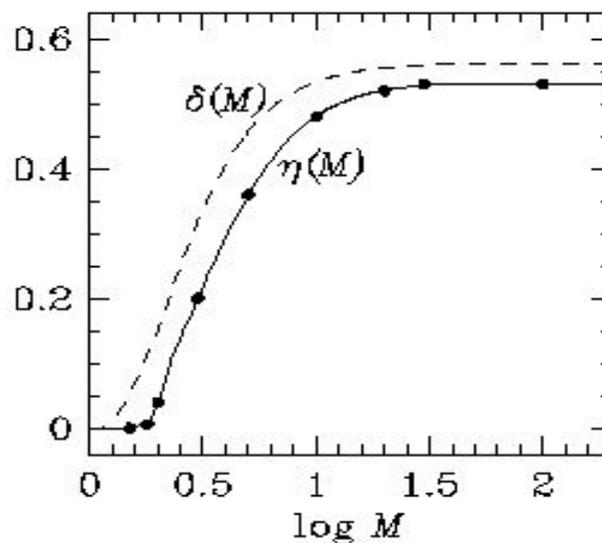
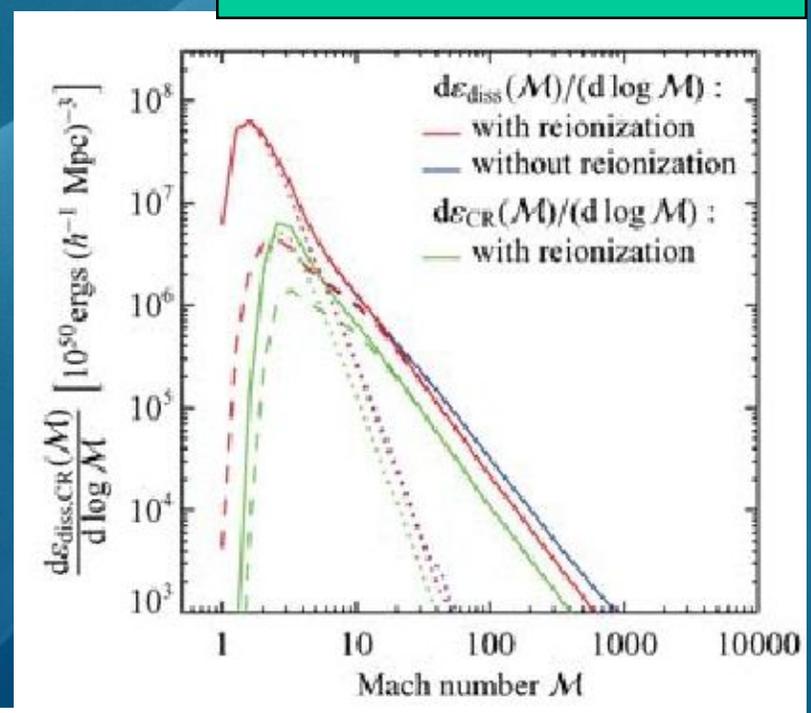
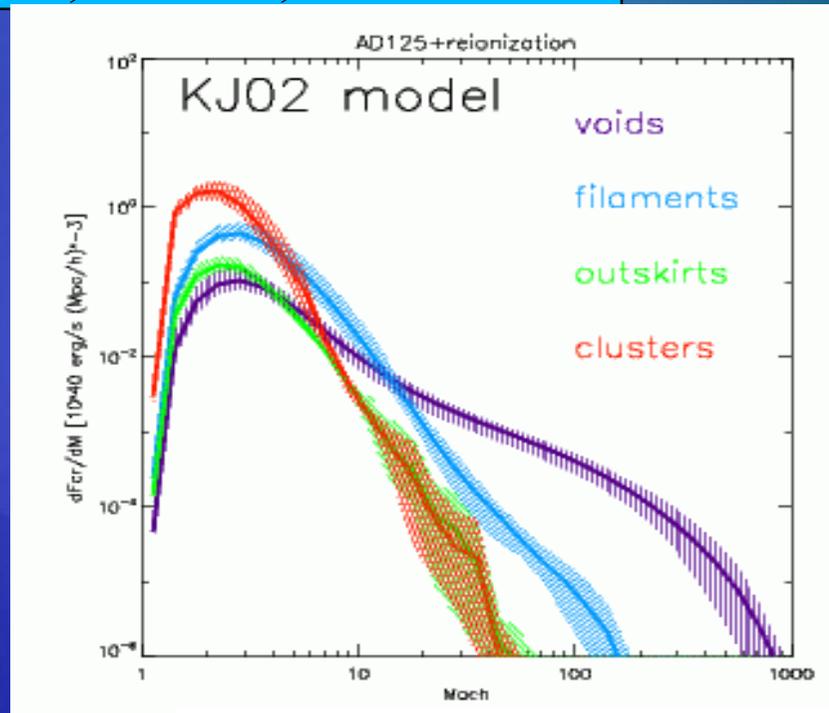
➤ Bi-modality of GC

← Radio  
Quiet  
GC

# Shocks in Galaxy Clusters (I)

Vazza, Brunetti, Gheller 2008

Pfrommer et al. 2008

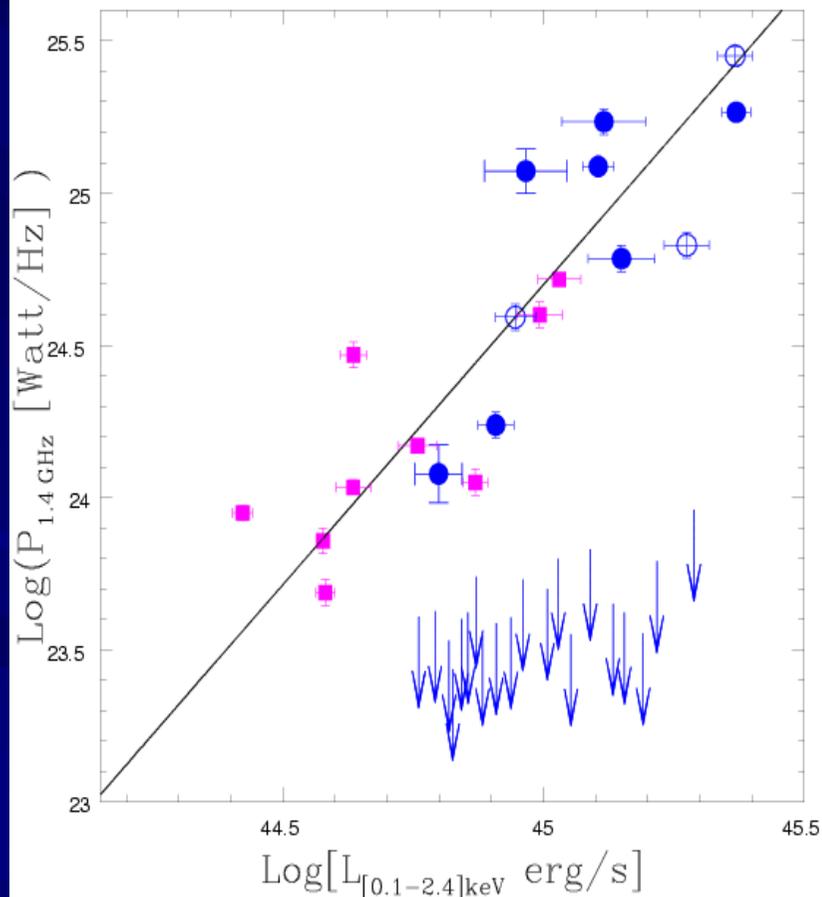


Ryu et al. 2003

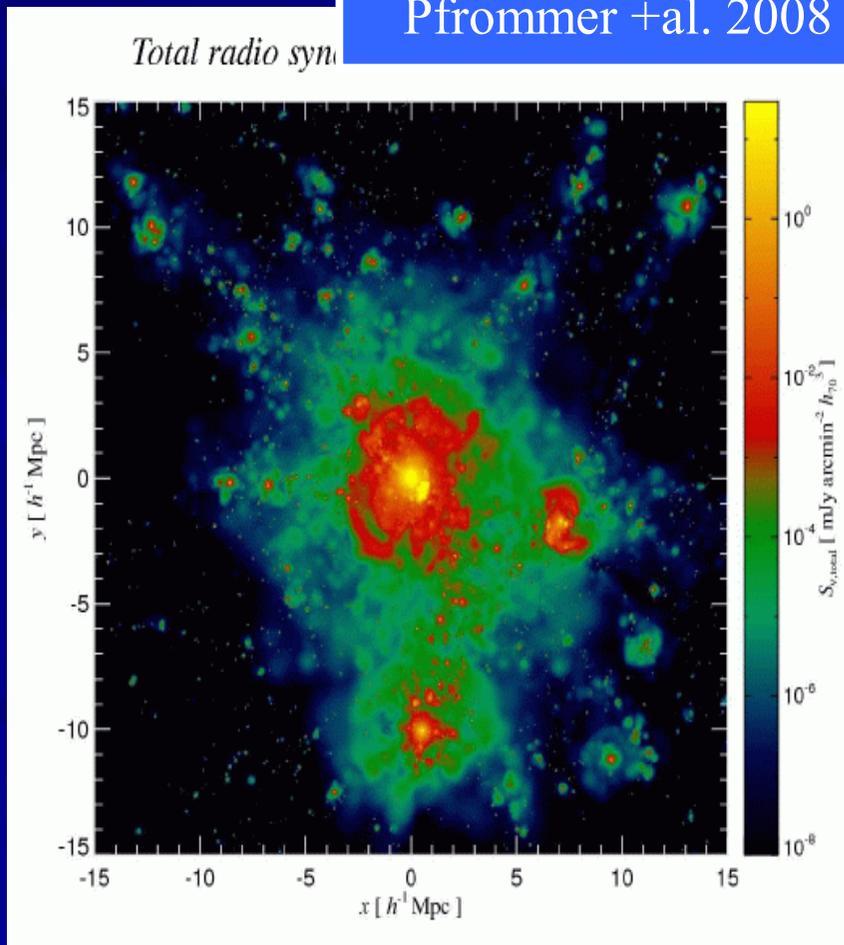
# Radio- Statistical properties of GC

Disagreement with  
shock+secondary models

Brunetti +al. 2007



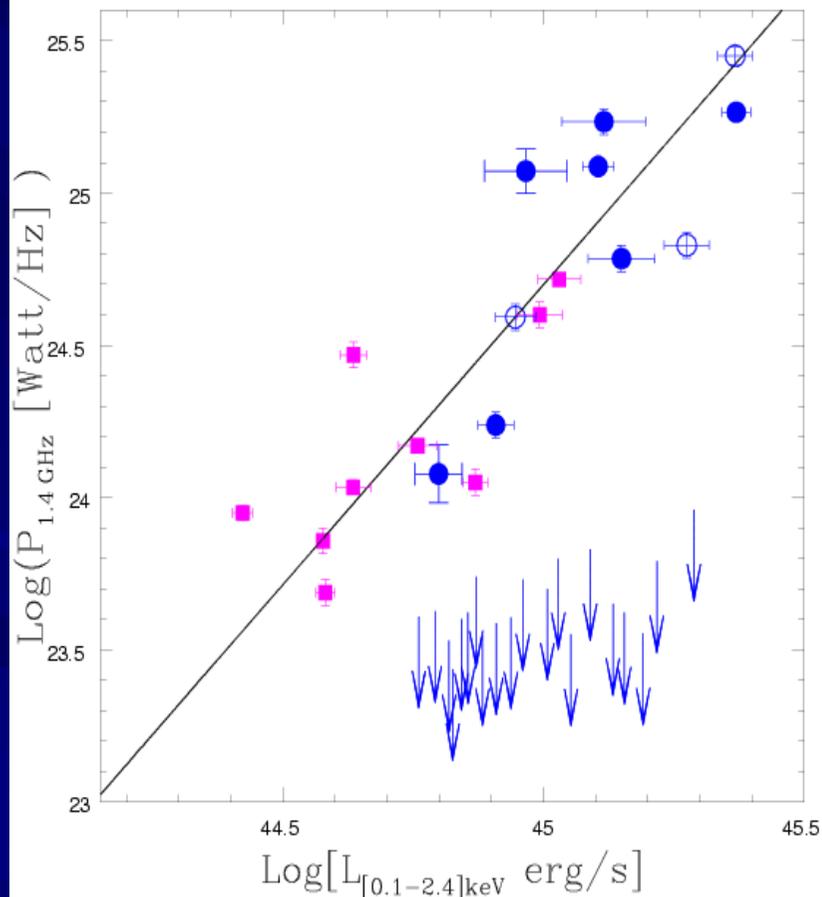
Pfrommer +al. 2008



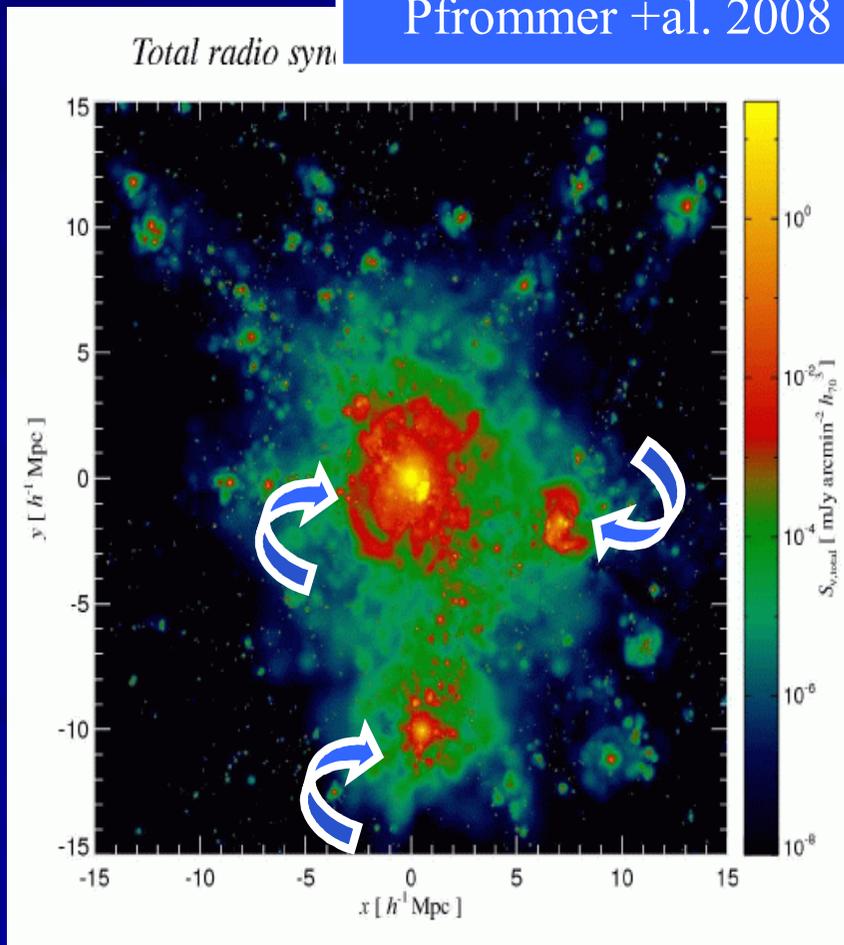
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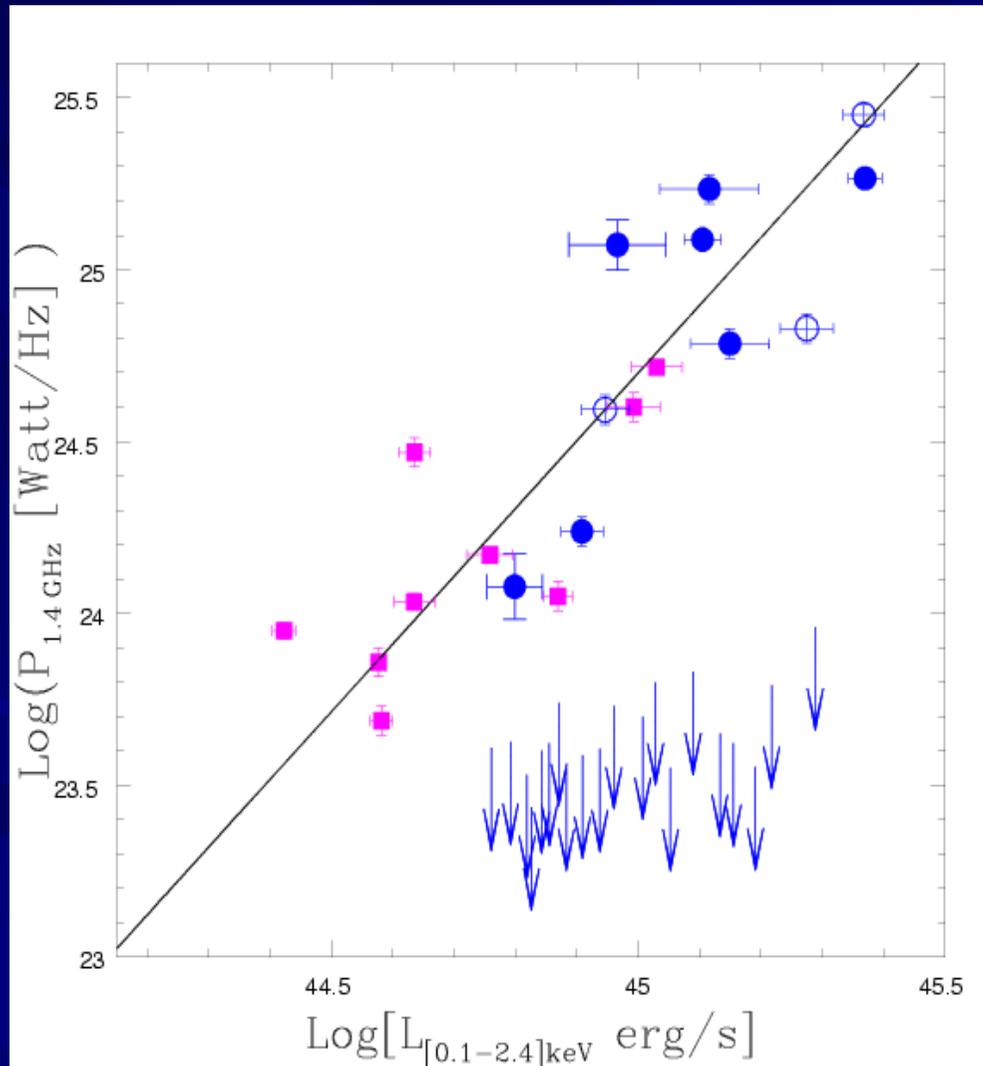


Pfrommer +al. 2008



# Radio- Statistical properties of GC

Brunetti +al. 2007



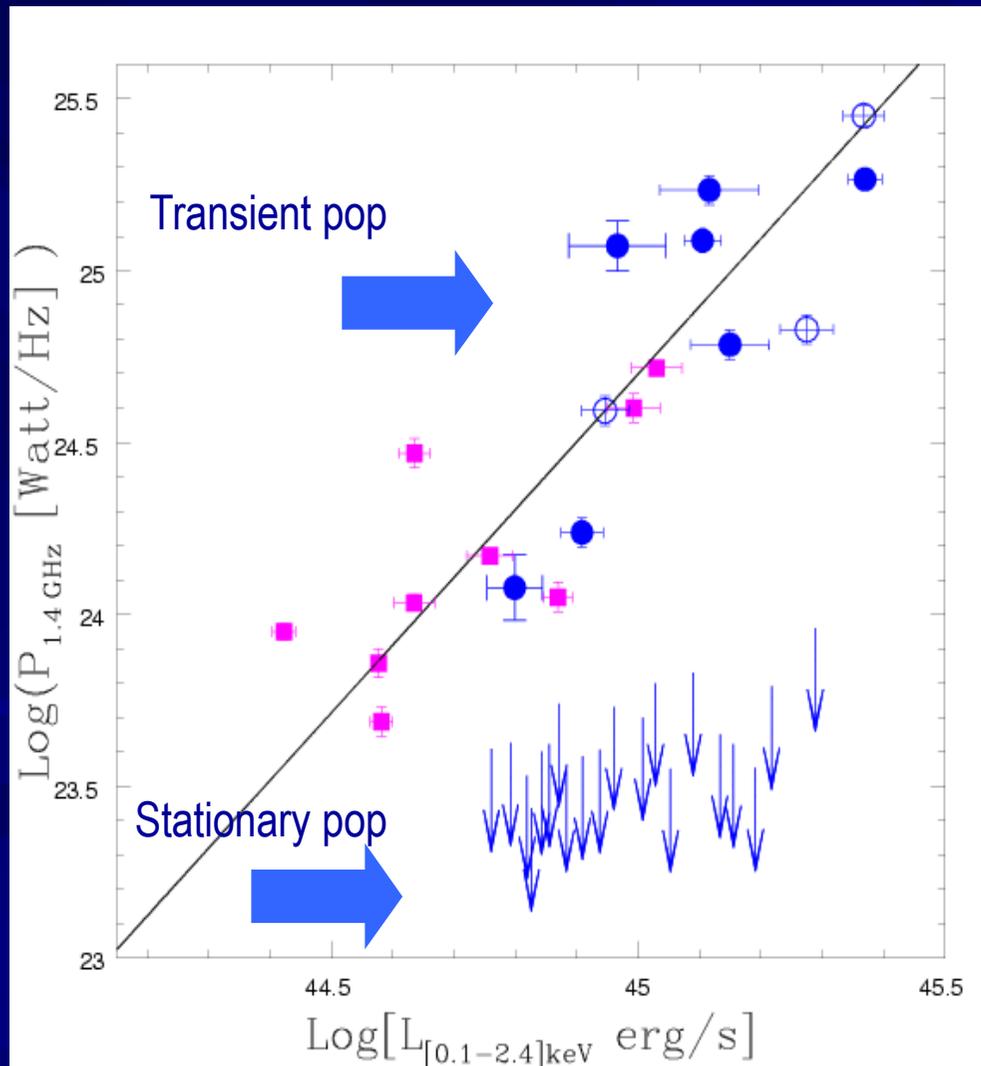
➤ RH are not common

➤ Bi-modality of GC

$\gamma \approx 10^4 e^\pm$  are not  
common in GC  
(on-off mechanism)

# Radio- Statistical properties of GC

Brunetti +al. 2007

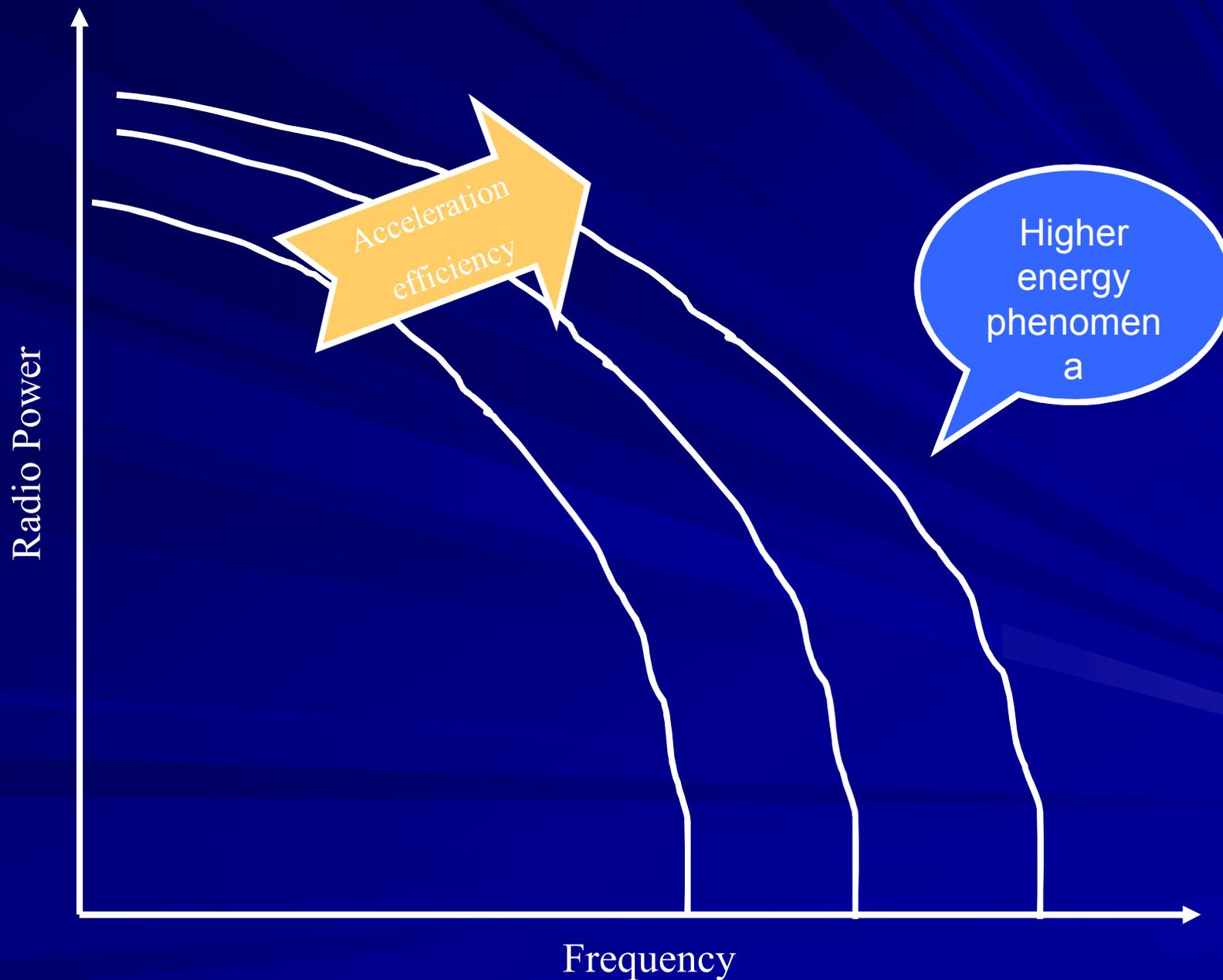


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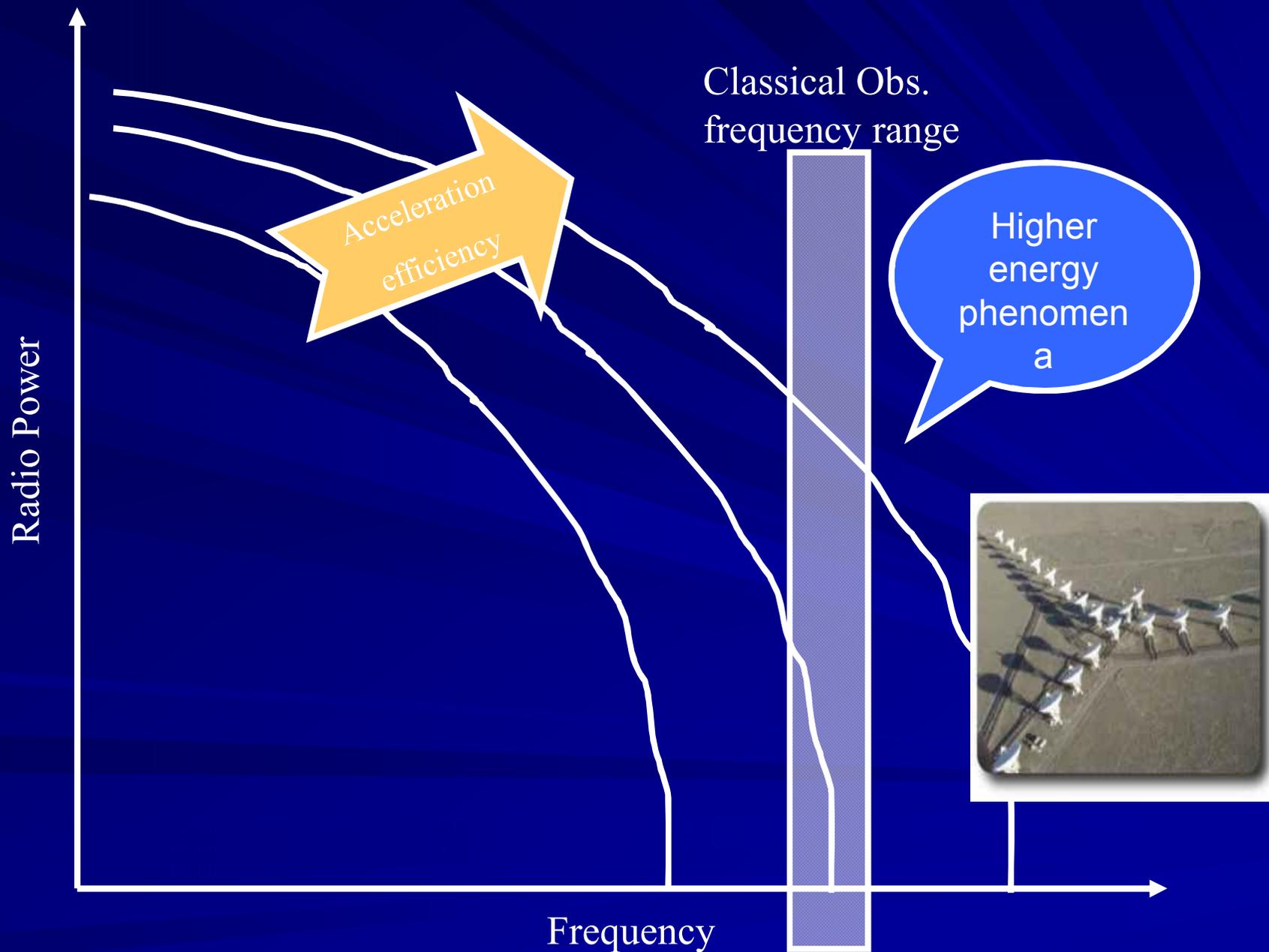
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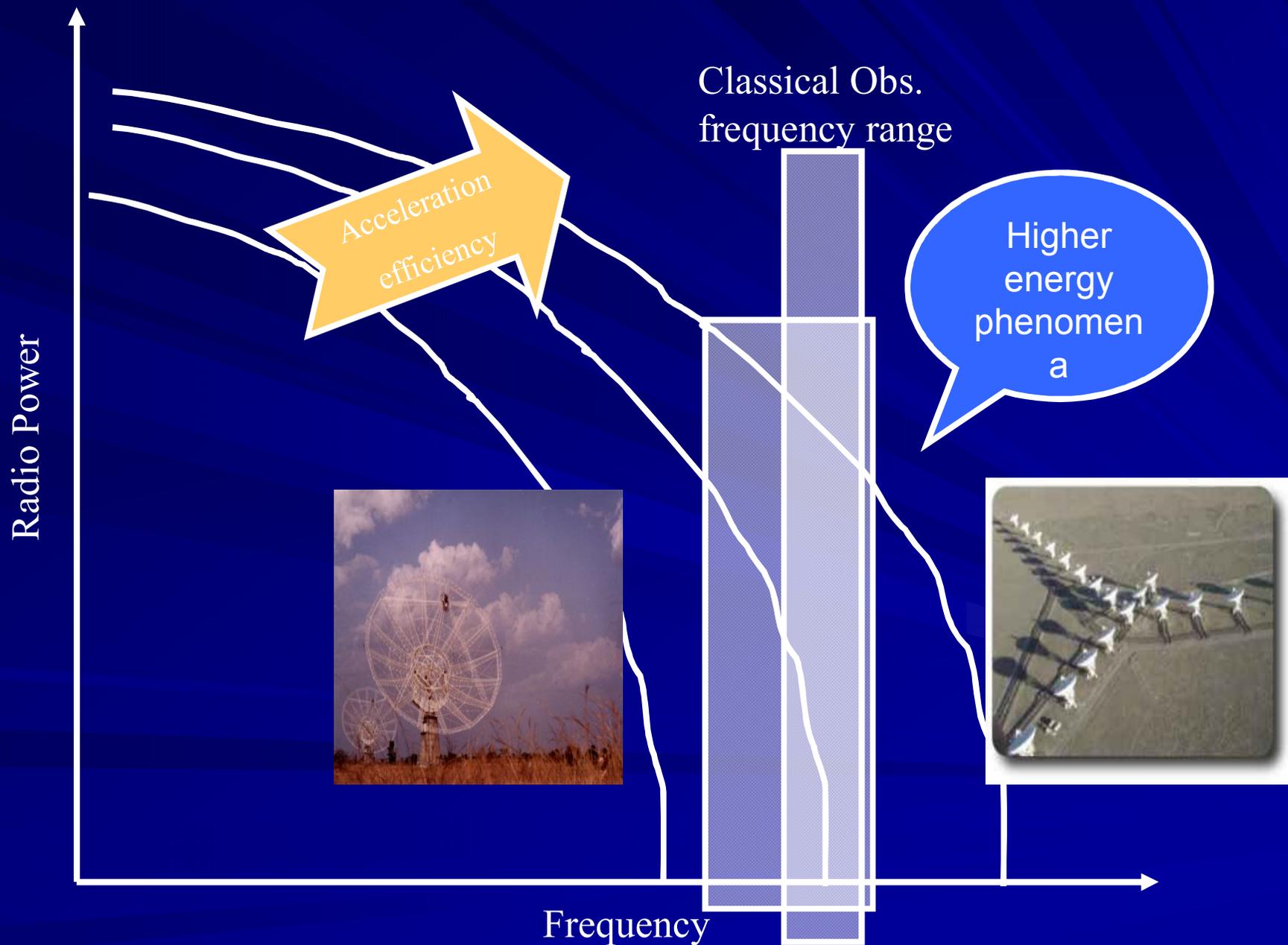
# Request: Extending the frequency range



# Request: Extending the frequency range



# Request: Extending the frequency range

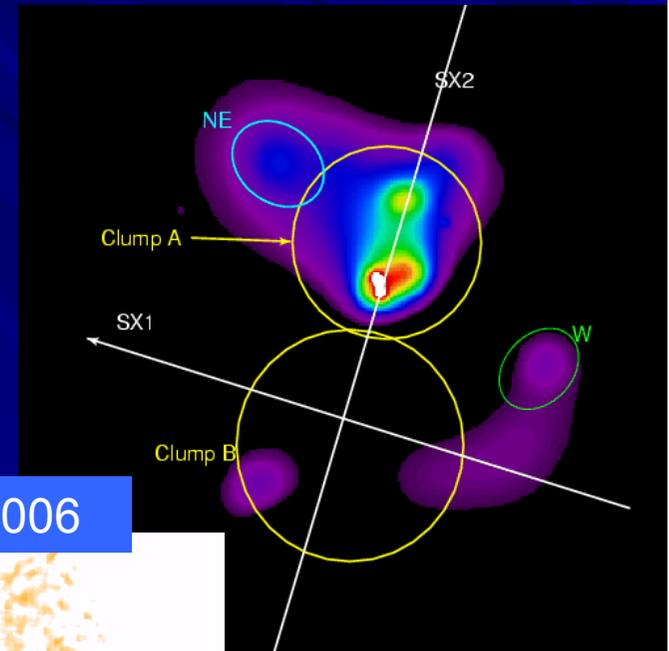


# Abell 521: a big surprise !

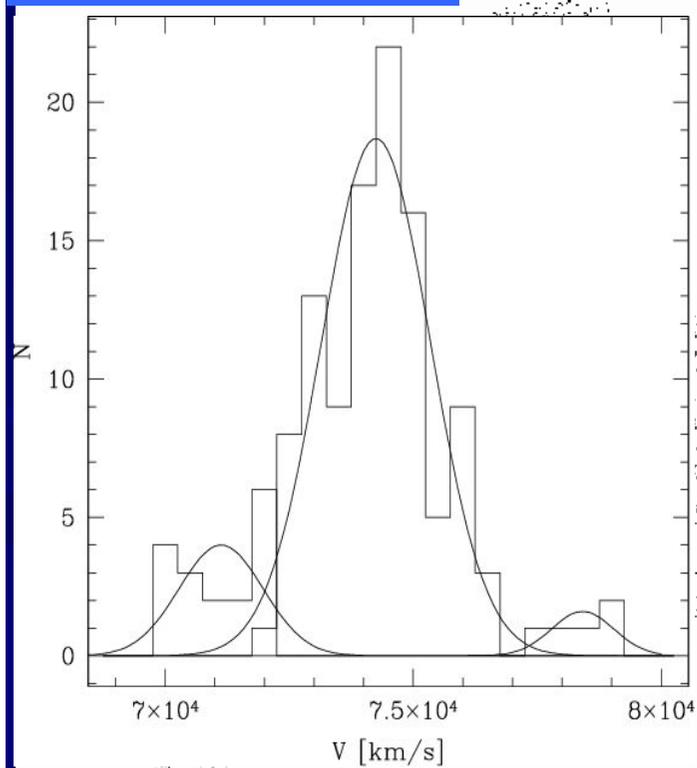
$z=0.247$

$L_x[0.1-2.4]=8.2 \cdot 10^{44}$  erg/s

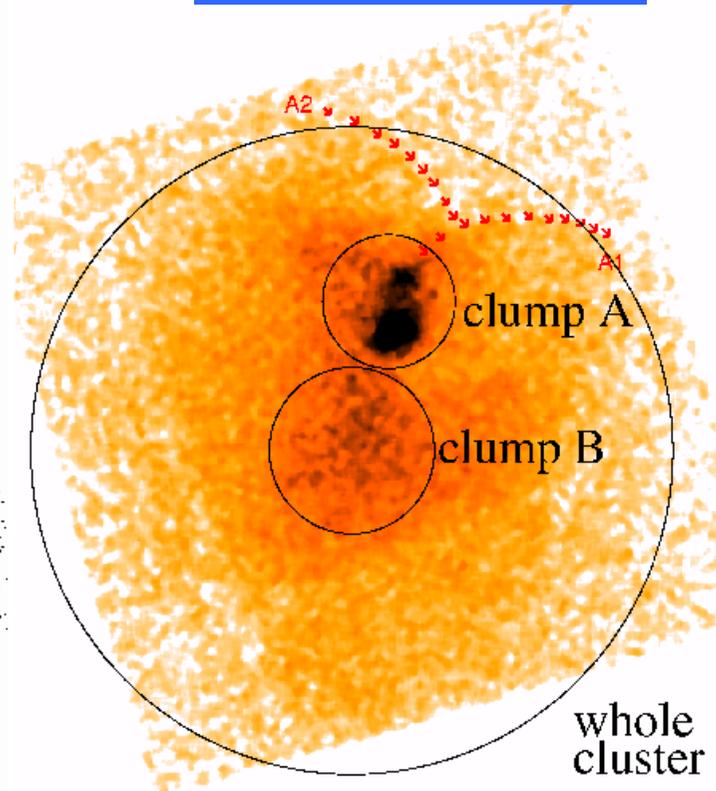
$M \approx 2 \cdot 10^{15}$  Msun



Ferrari +al. 2003

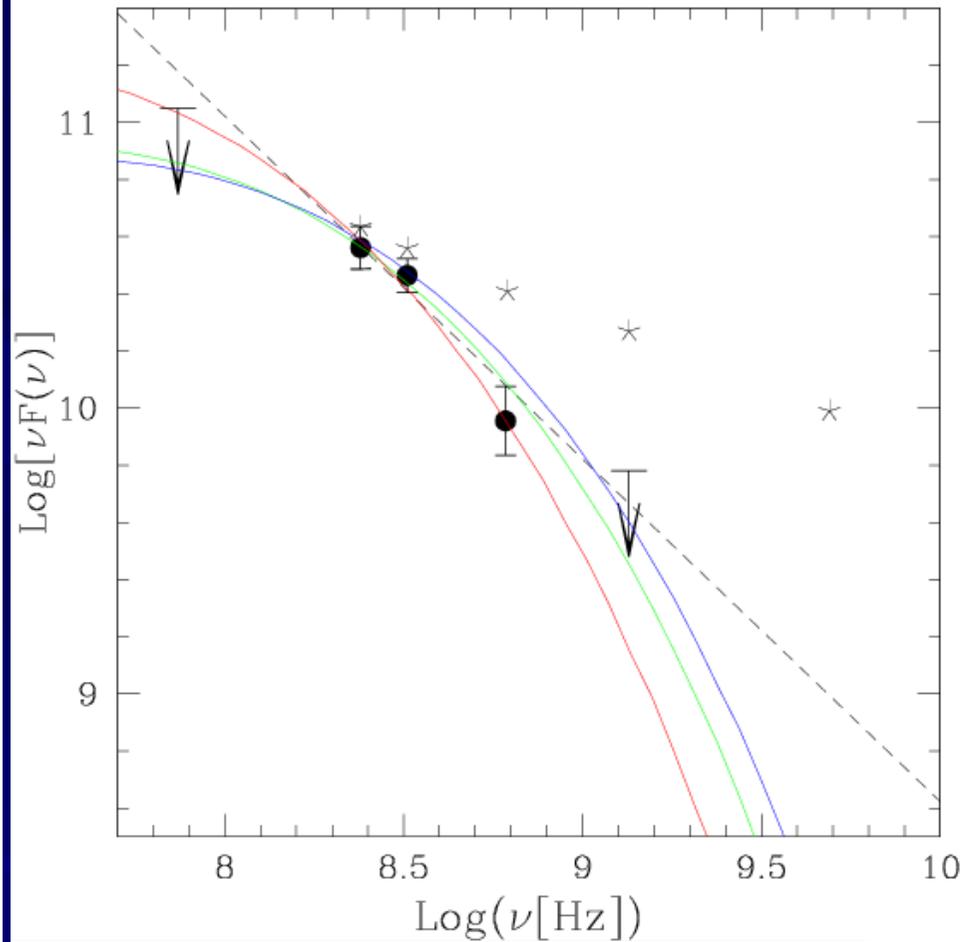


Ferrari +al. 2006

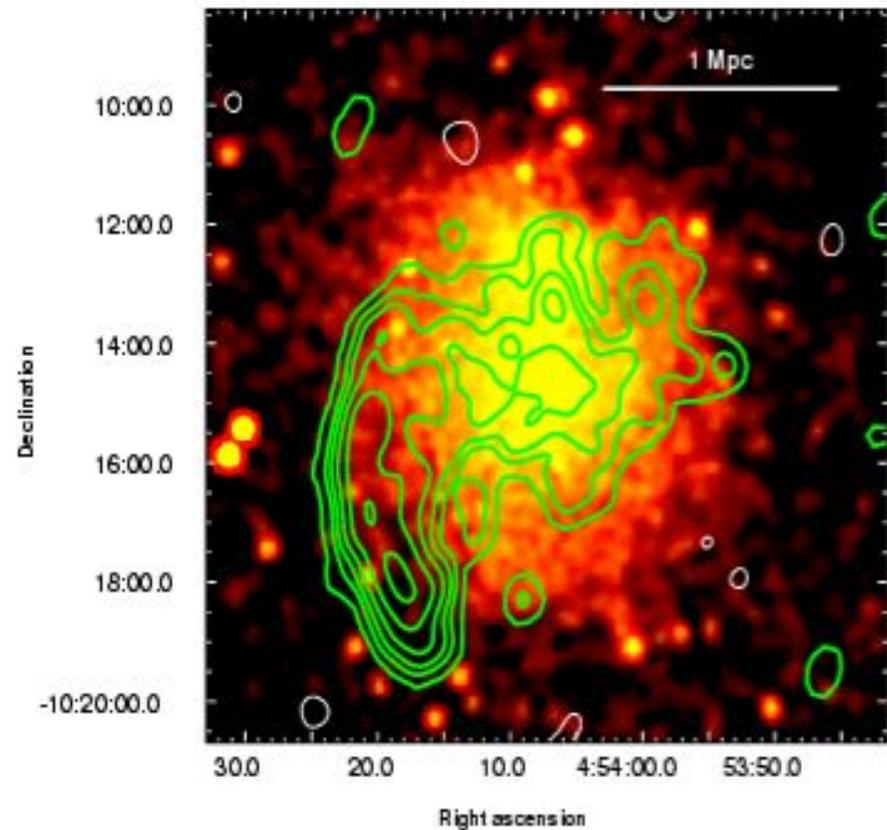


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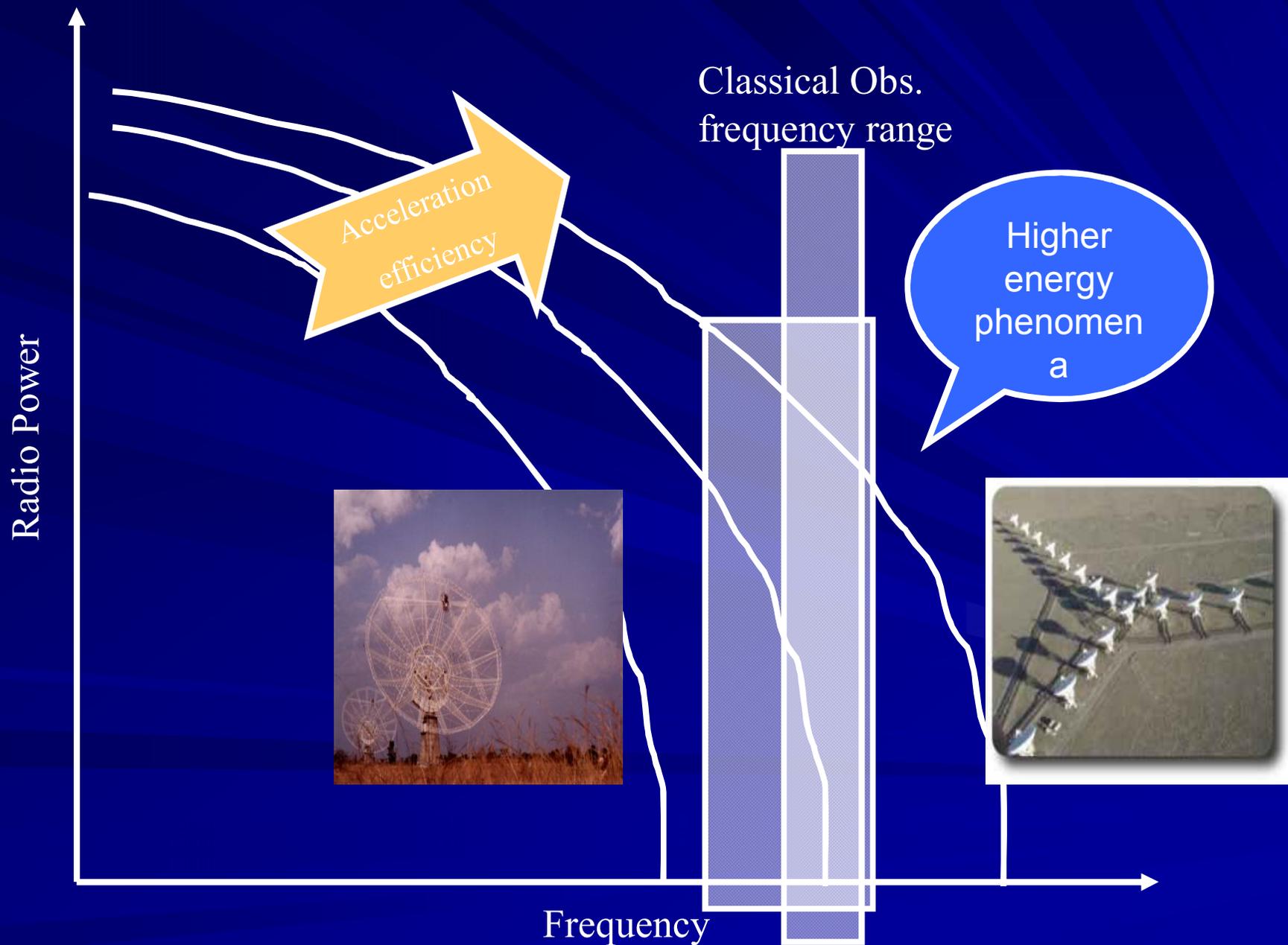
The first low frequency  
Radio Halo !



The first Radio Halo  
with ultra steep spectrum

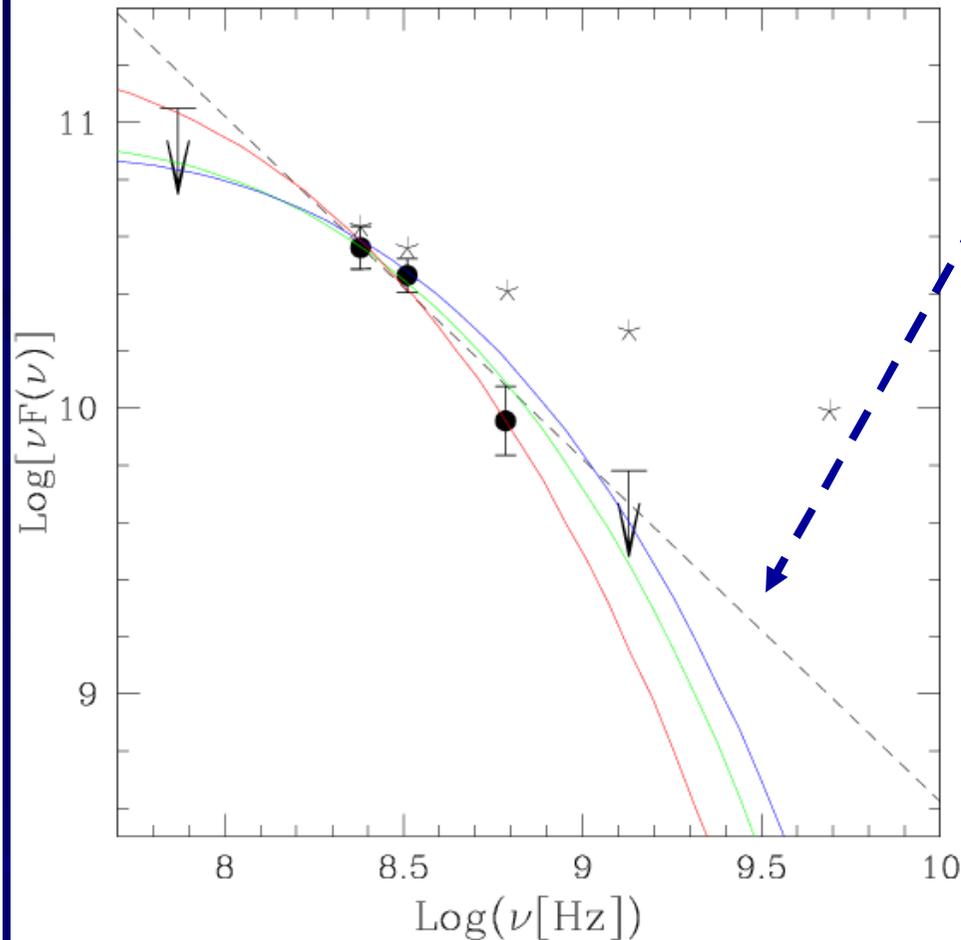


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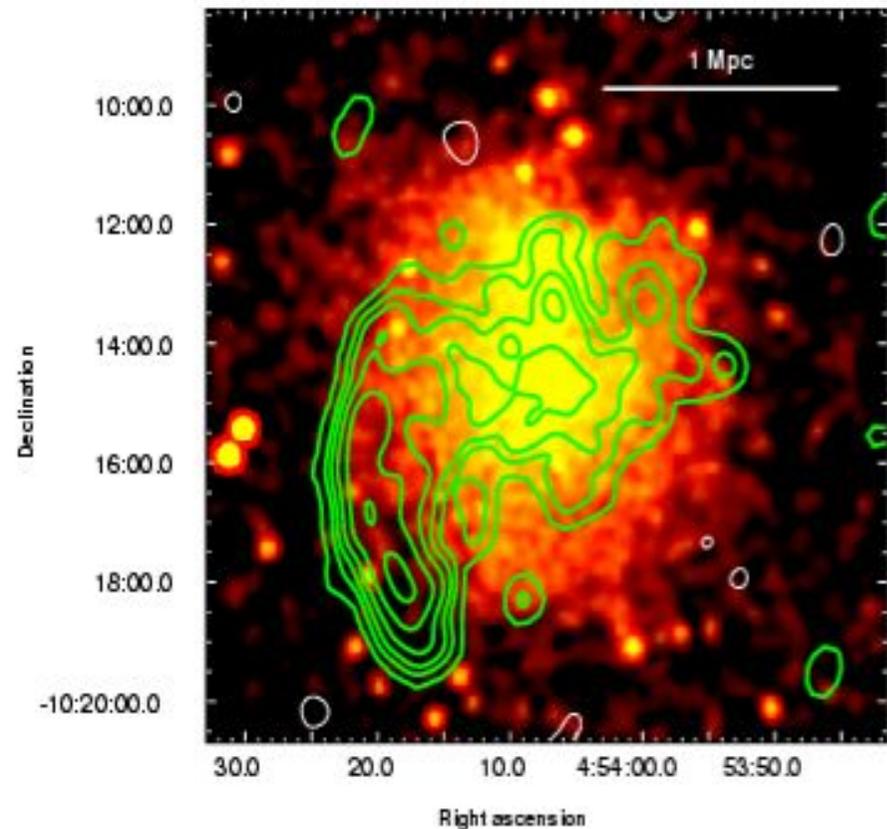


# Abell 521: a big surprise !

Secondary models require energy in CR protons larger than the cluster thermal energy

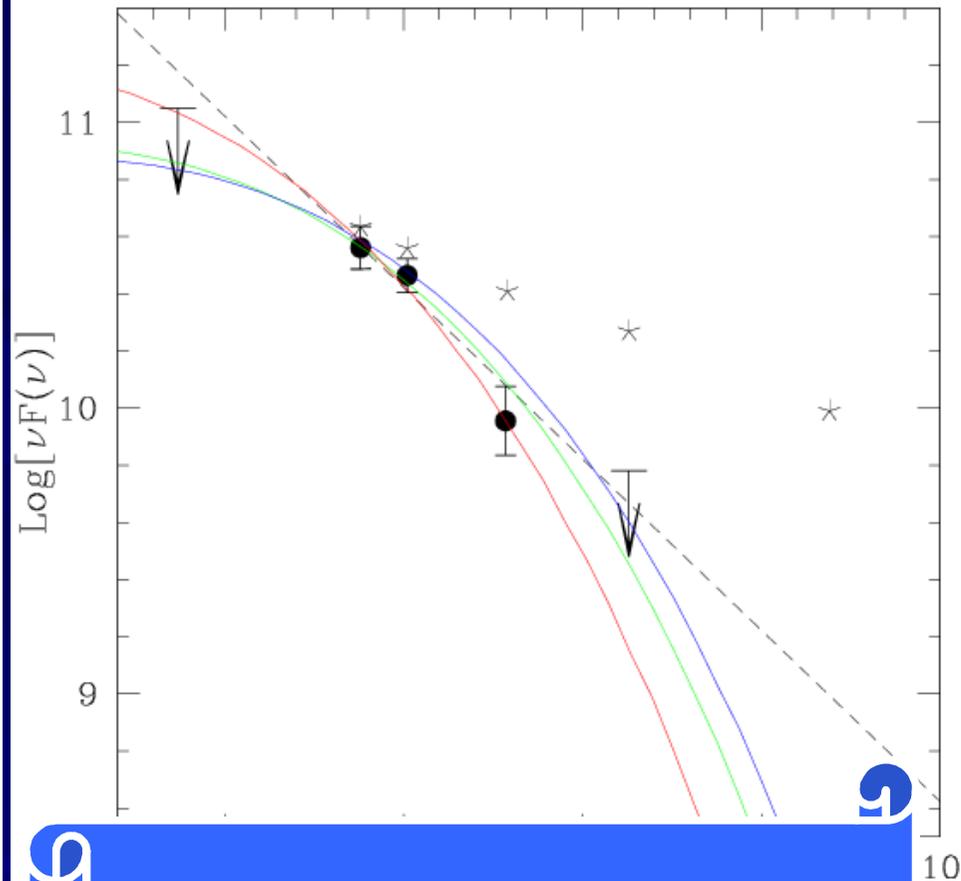


The first Radio Halo with ultra steep spectrum

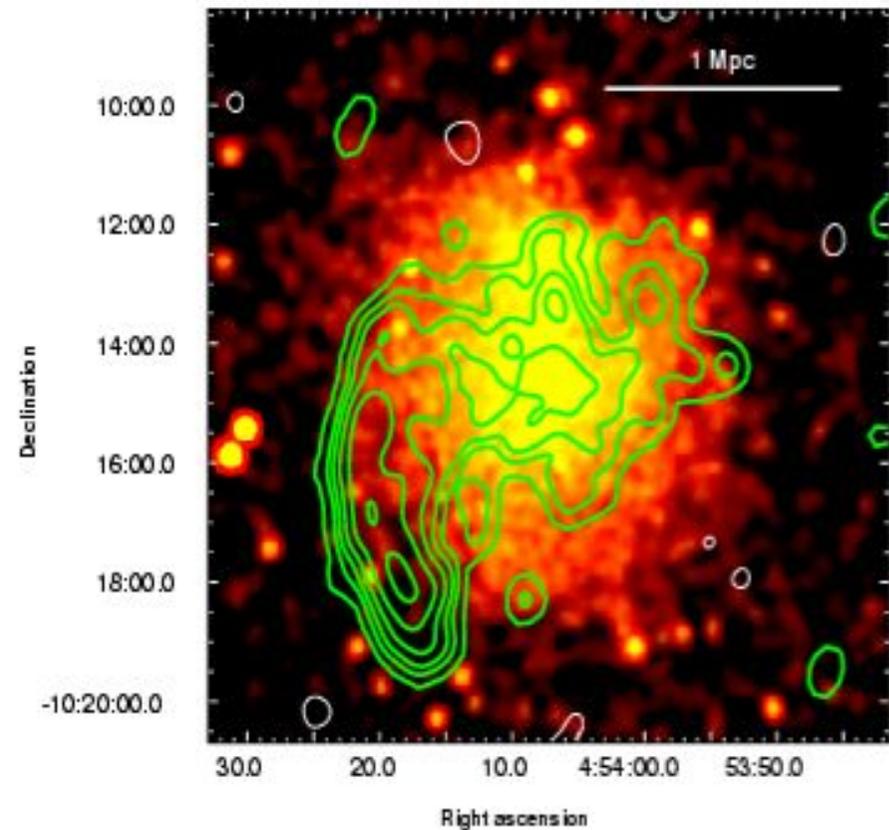


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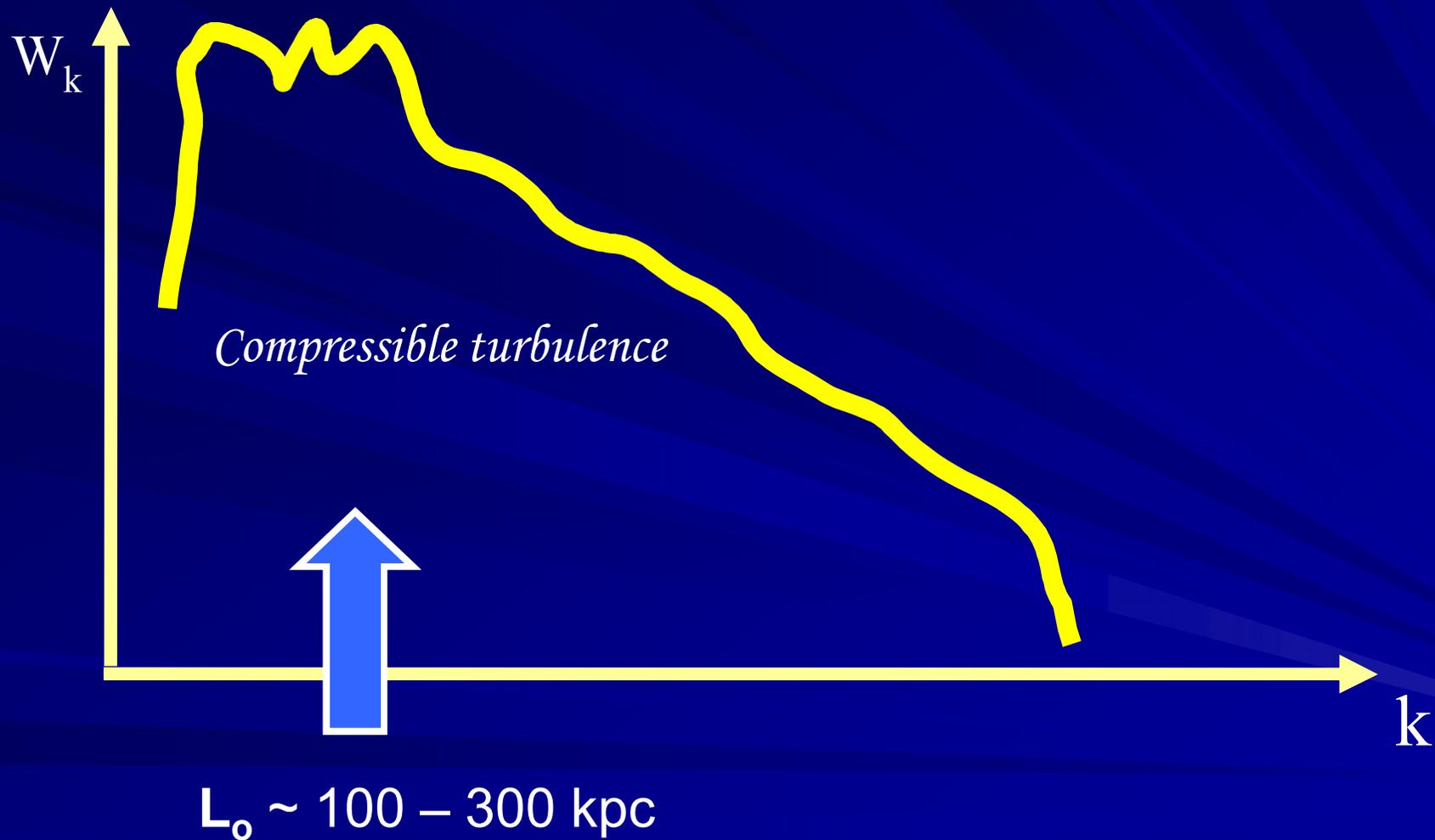


The most striking evidence that turbulence accelerates particles in the IGM



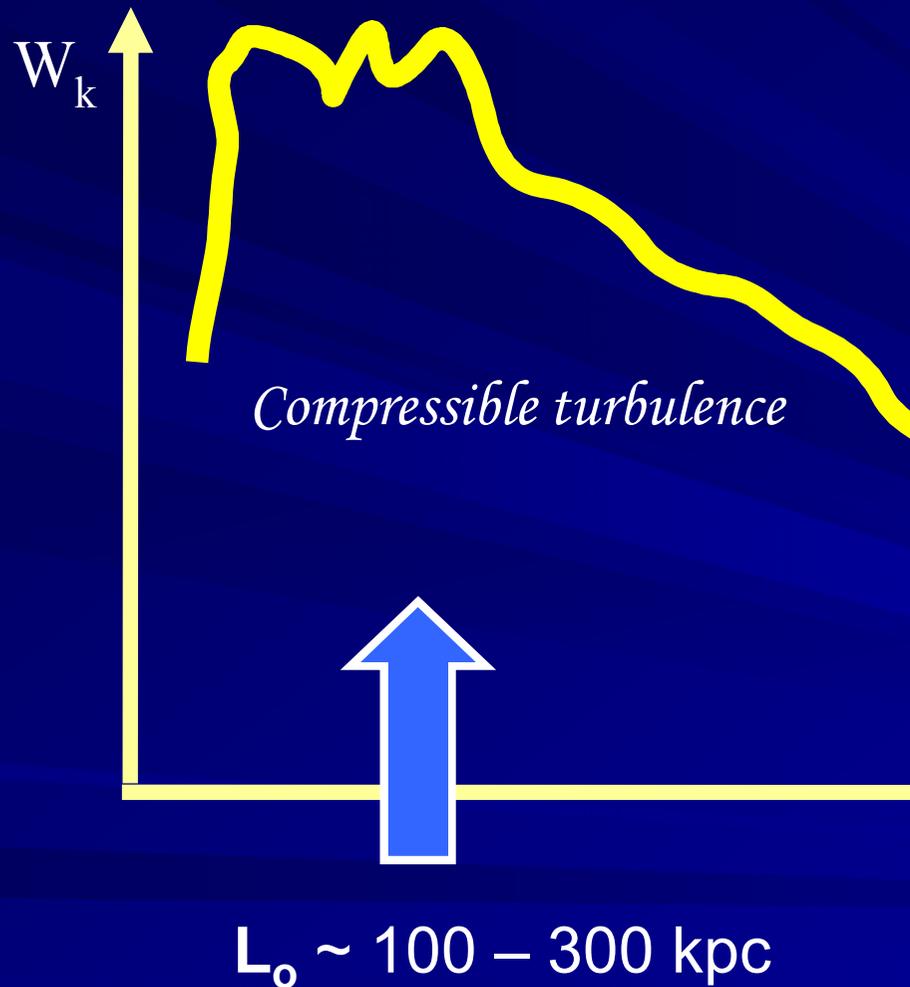
# Basics of turbulence in the ICM

Brunetti & Lazarian 2007



# Basics of turbulence in the ICM

Brunetti & Lazarian 2007



$$L_0 \sim 100 - 300 \text{ kpc}$$

$$V_0 \sim 500 - 1000 \text{ km/s}$$

$$c_s \sim 1200 - 1800 \text{ km/s}$$

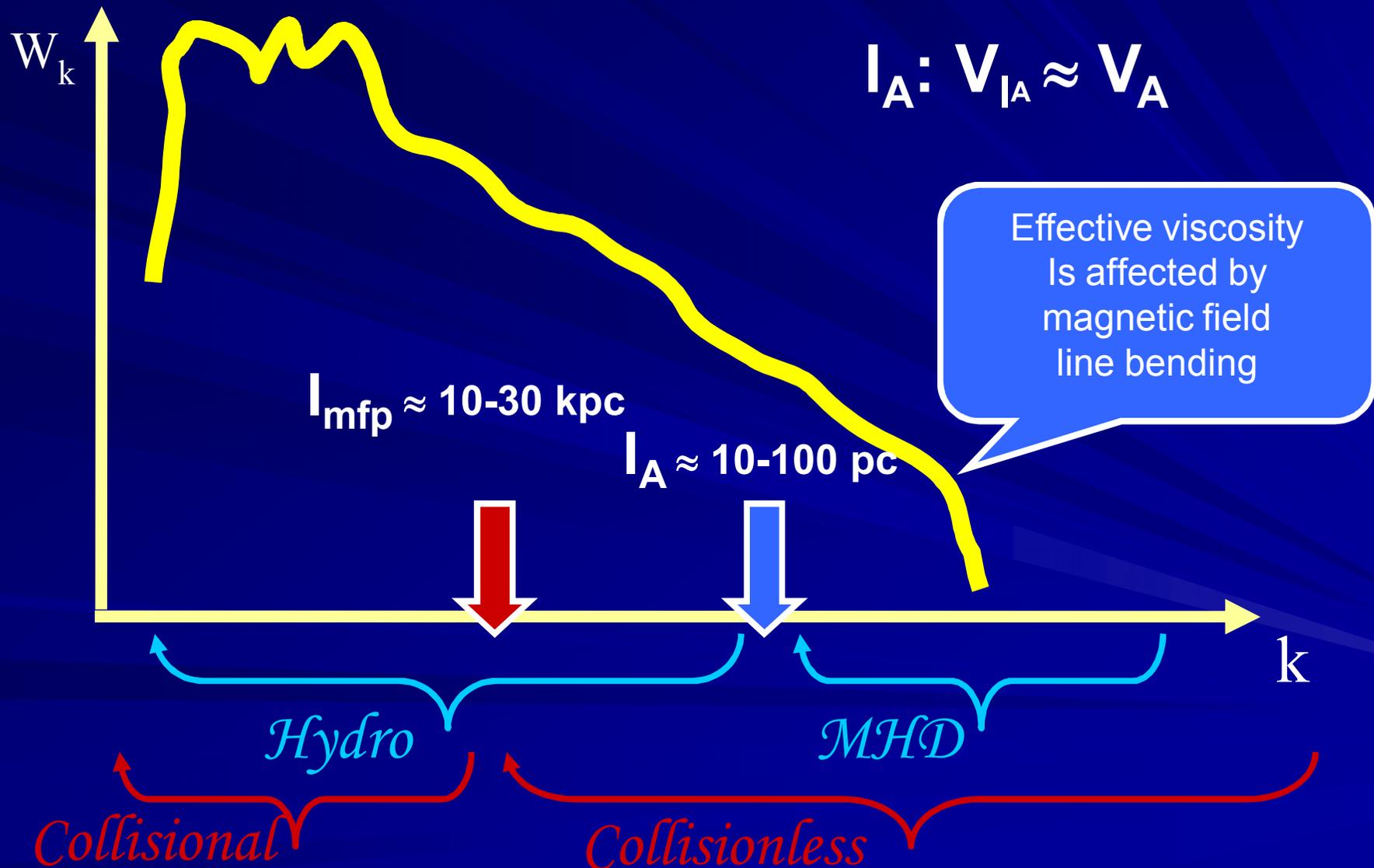
$$V_A \sim 30 - 100 \text{ km/s}$$

*Sub-sonic Turbulence*

*Super-Alfvénic Turbulence*

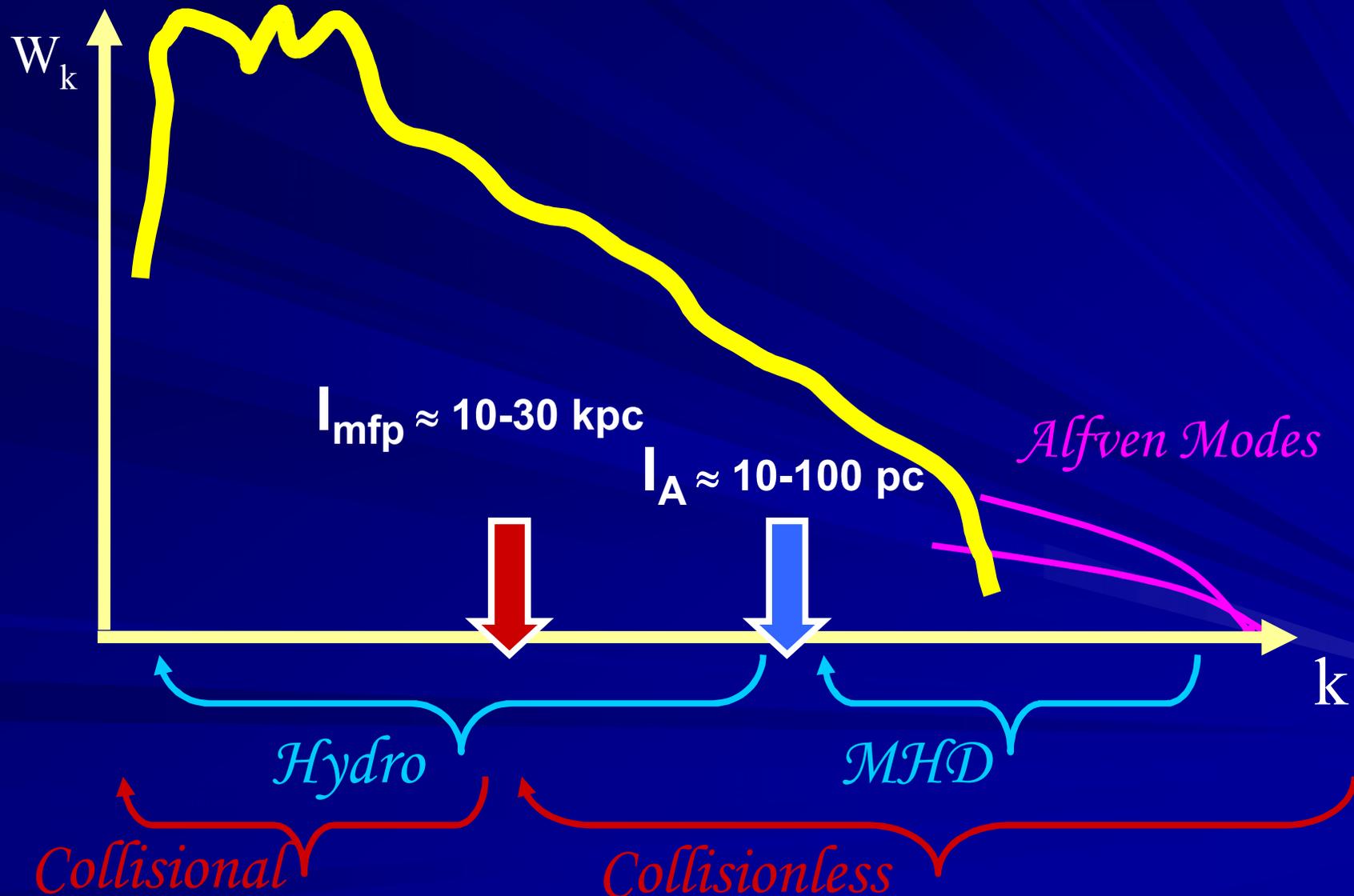
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Brunetti & Lazarian 2007



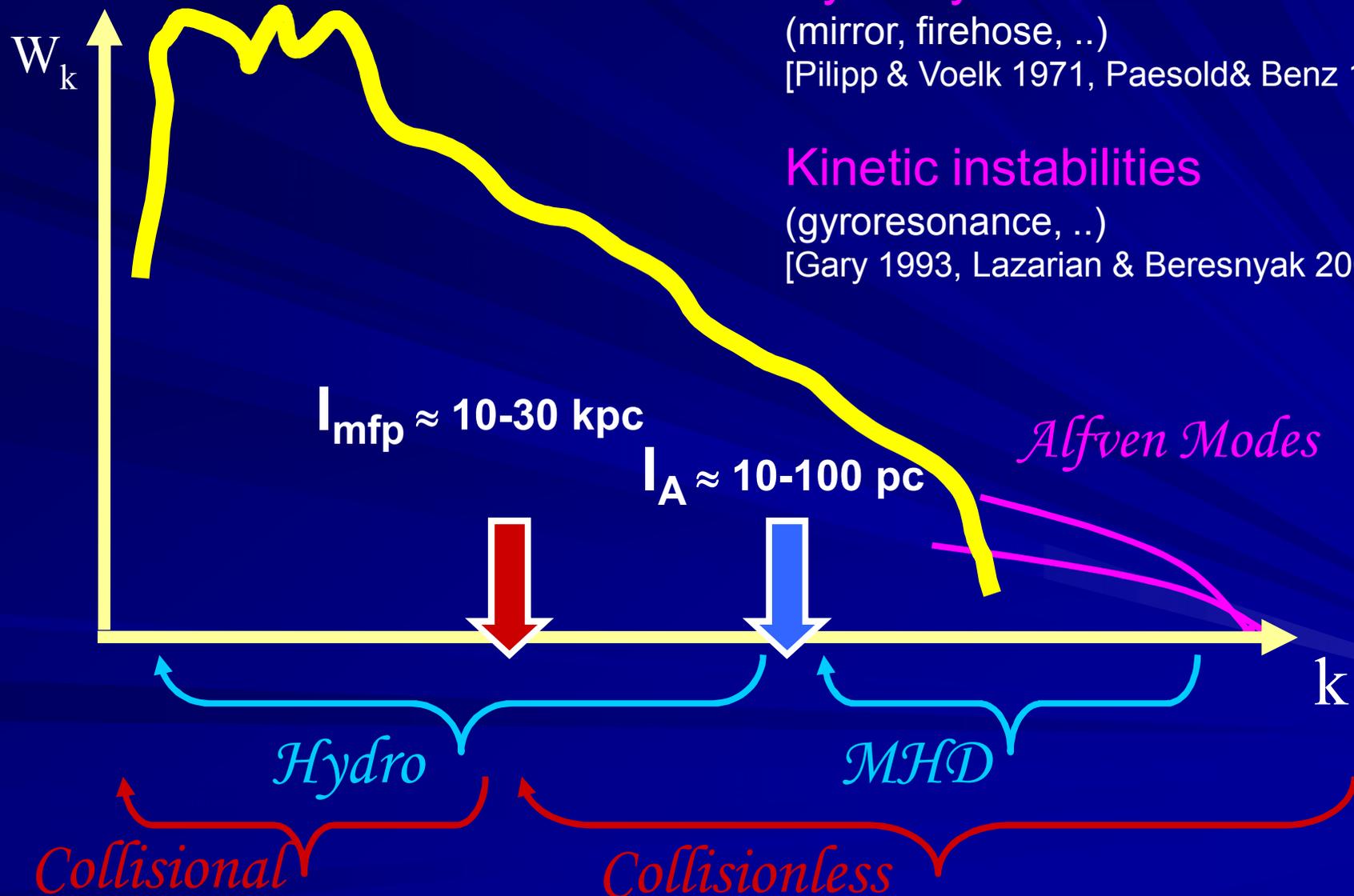
# Basics of turbulence in the ICM

Brunetti & Lazarian 2007



# Basics of turbulence in the ICM

Brunetti & Lazarian 2007



Hydrodynamic instabilities

(mirror, firehose, ..)

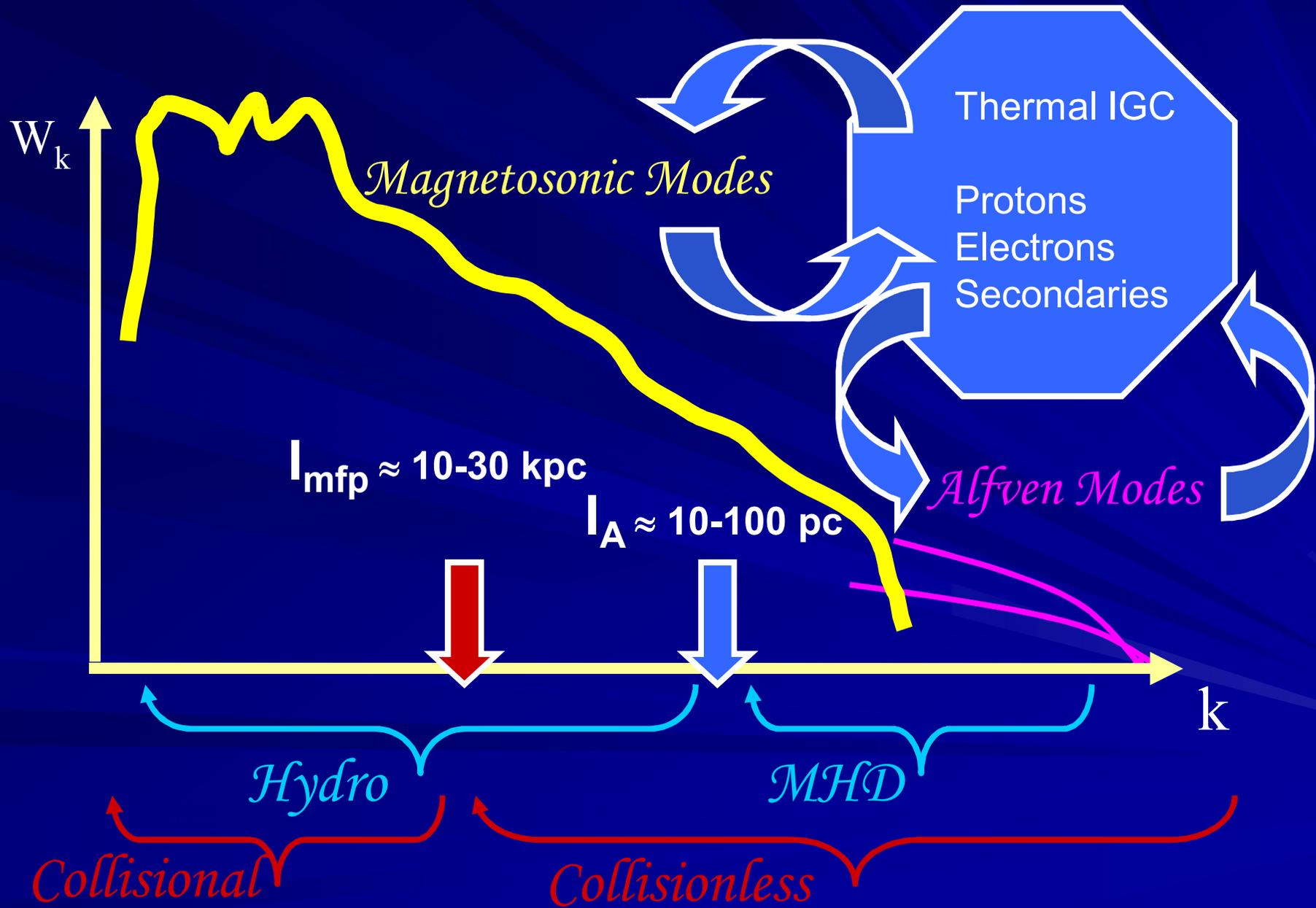
[Pilipp & Voelk 1971, Paesold & Benz 1999]

Kinetic instabilities

(gyroresonance, ..)

[Gary 1993, Lazarian & Beresnyak 2006]

# Basics of turbulence in the ICM



# Alfvenic: results

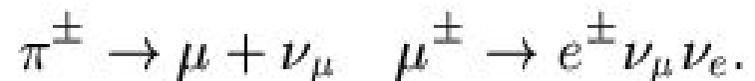
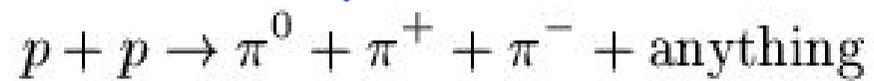
$n_{th}, T, B_o, N_p(p,0)$

$I(k)$

# Alfvenic: results

$n_{th}, T, B_0, N_p(p,0)$

$I(k)$

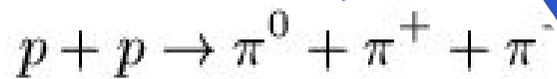


# Alfvenic: results

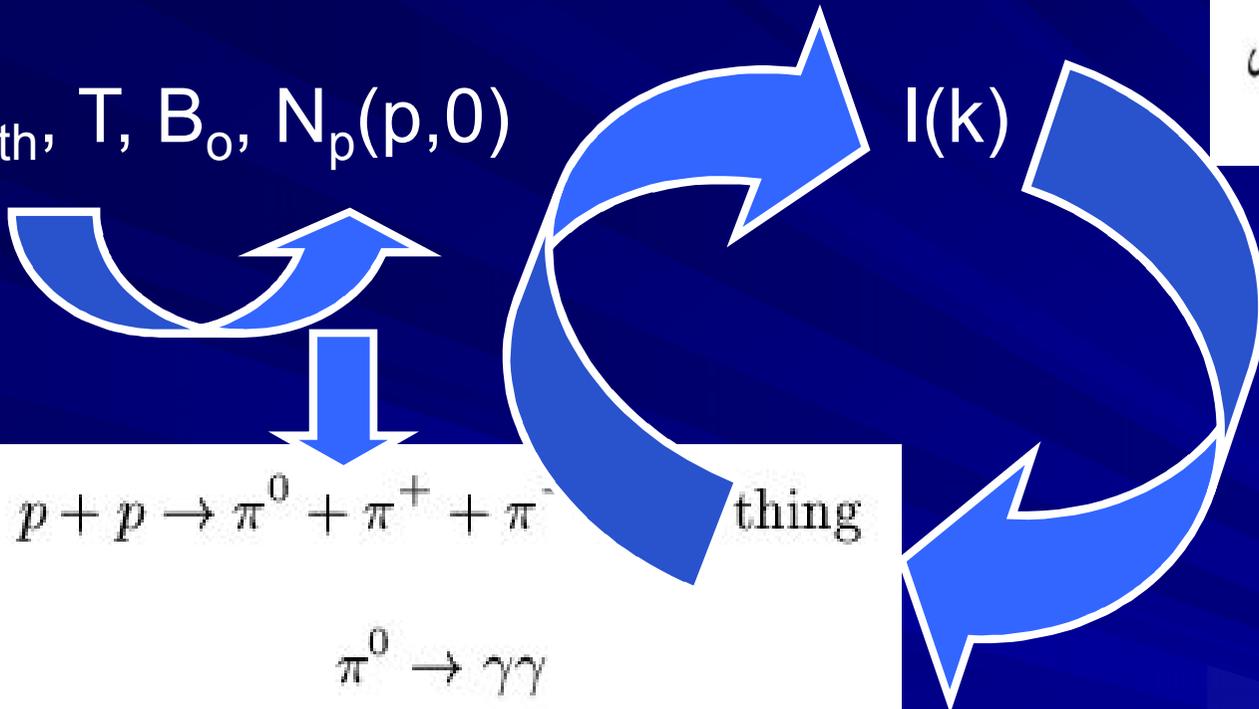
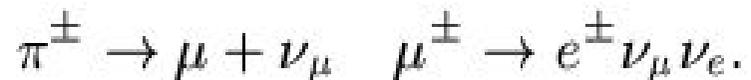
$n_{th}, T, B_o, N_p(p,0)$

$I(k)$

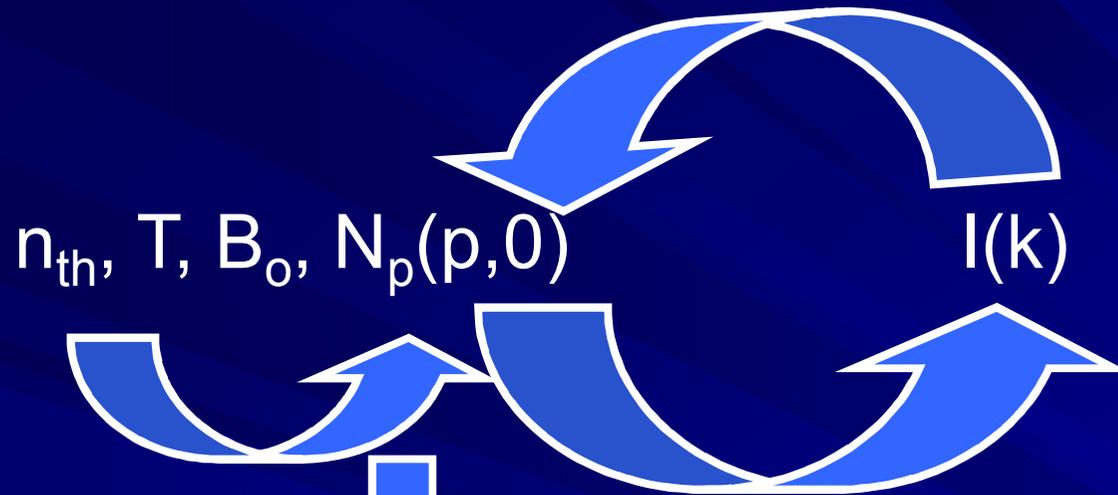
$$\omega - k_{\parallel} v_{\parallel} - n \frac{\Omega_o}{\gamma} = 0$$



thing



# Alfvenic: results



$$\omega - k_{\parallel} v_{\parallel} - n \frac{\Omega_o}{\gamma} = 0$$

$$p + p \rightarrow \pi^0 + \pi^+ + \pi^- + \text{anything}$$

$$\pi^0 \rightarrow \gamma\gamma$$

$$\pi^{\pm} \rightarrow \mu + \nu_{\mu} \quad \mu^{\pm} \rightarrow e^{\pm} \nu_{\mu} \nu_e.$$

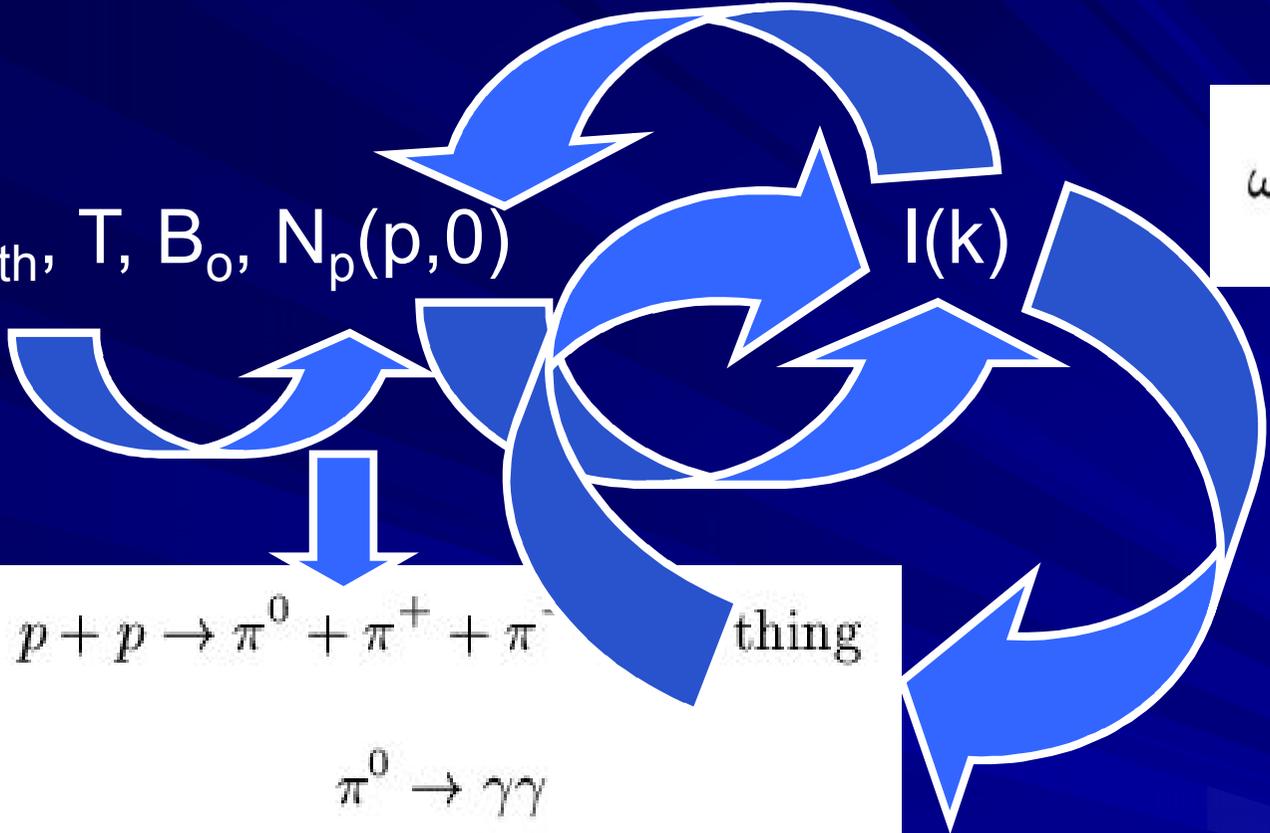
# Alfvenic: results

$n_{th}, T, B_o, N_p(p,0)$

$I(k)$

$$\omega - k_{\parallel} v_{\parallel} - n \frac{\Omega_o}{\gamma} = 0$$

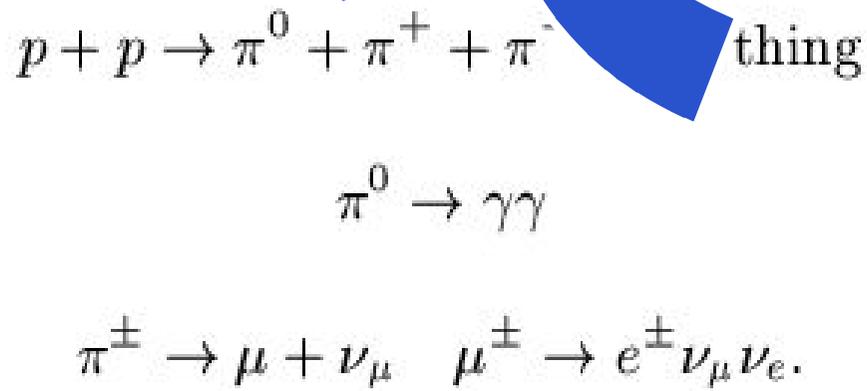
$p + p \rightarrow \pi^0 + \pi^+ + \pi^-$  thing  
 $\pi^0 \rightarrow \gamma\gamma$   
 $\pi^{\pm} \rightarrow \mu + \nu_{\mu} \quad \mu^{\pm} \rightarrow e^{\pm} \nu_{\mu} \nu_e.$



# Alfvenic: results

$n_{th}, T, B_0, N_p(p,0)$

$I(k)$

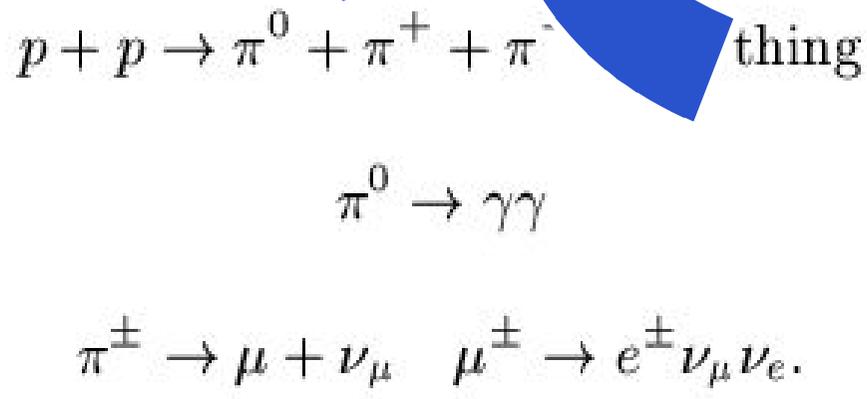


$N_p(p,t), N_{e^\pm}(p,t), W(k,t), Q_{e^\pm}(p,t), Q_\pi(p,t)$

# Alfvenic: results

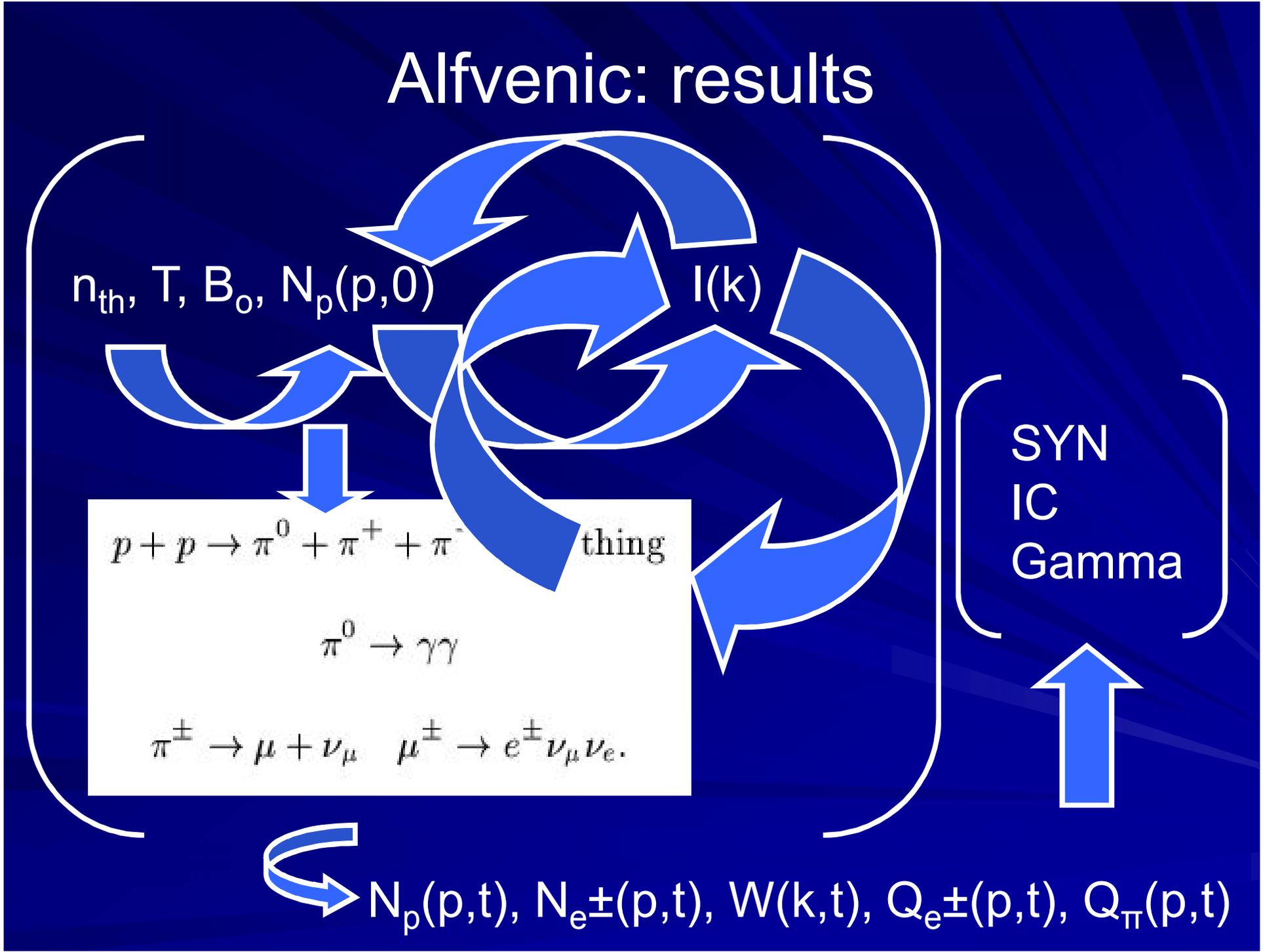
$n_{th}, T, B_0, N_p(p,0)$

$I(k)$



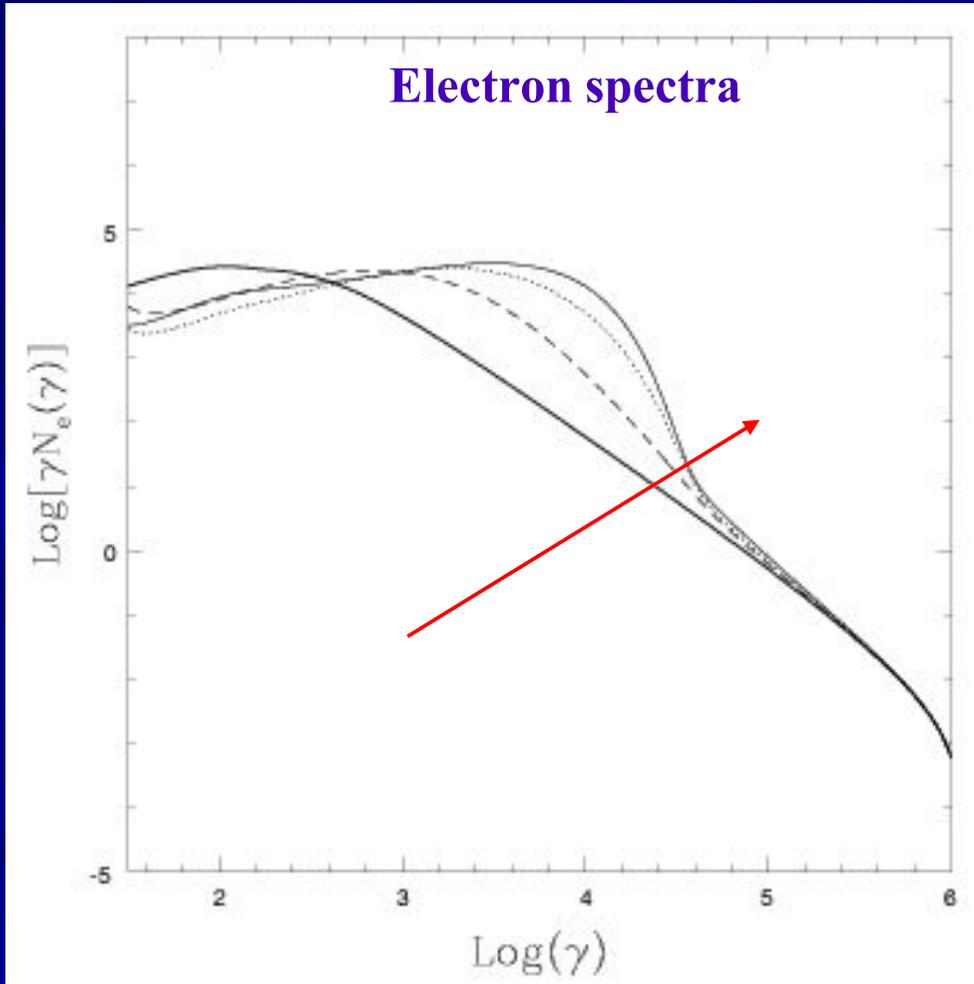
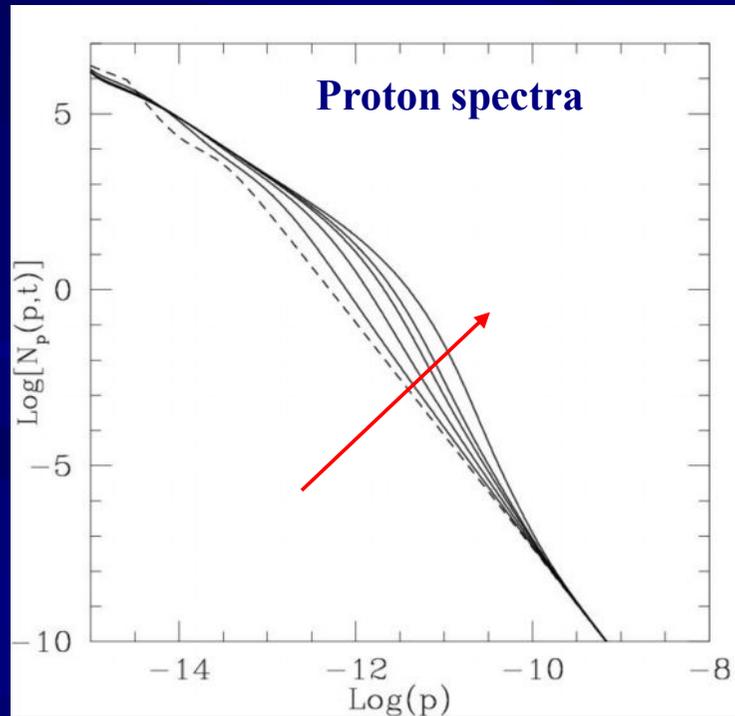
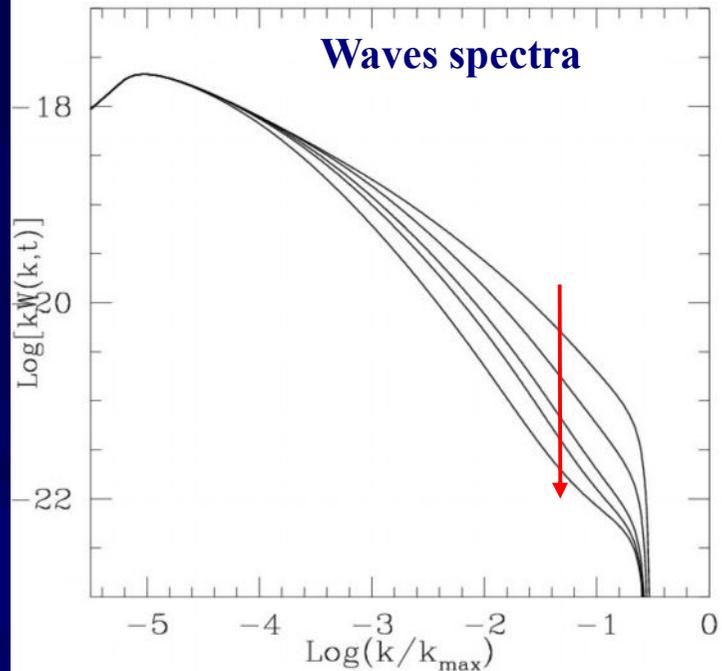
SYN  
 IC  
 Gamma

$N_p(p,t), N_{e^\pm}(p,t), W(k,t), Q_{e^\pm}(p,t), Q_\pi(p,t)$



# Full Alfven-Wave--Particle Coupling

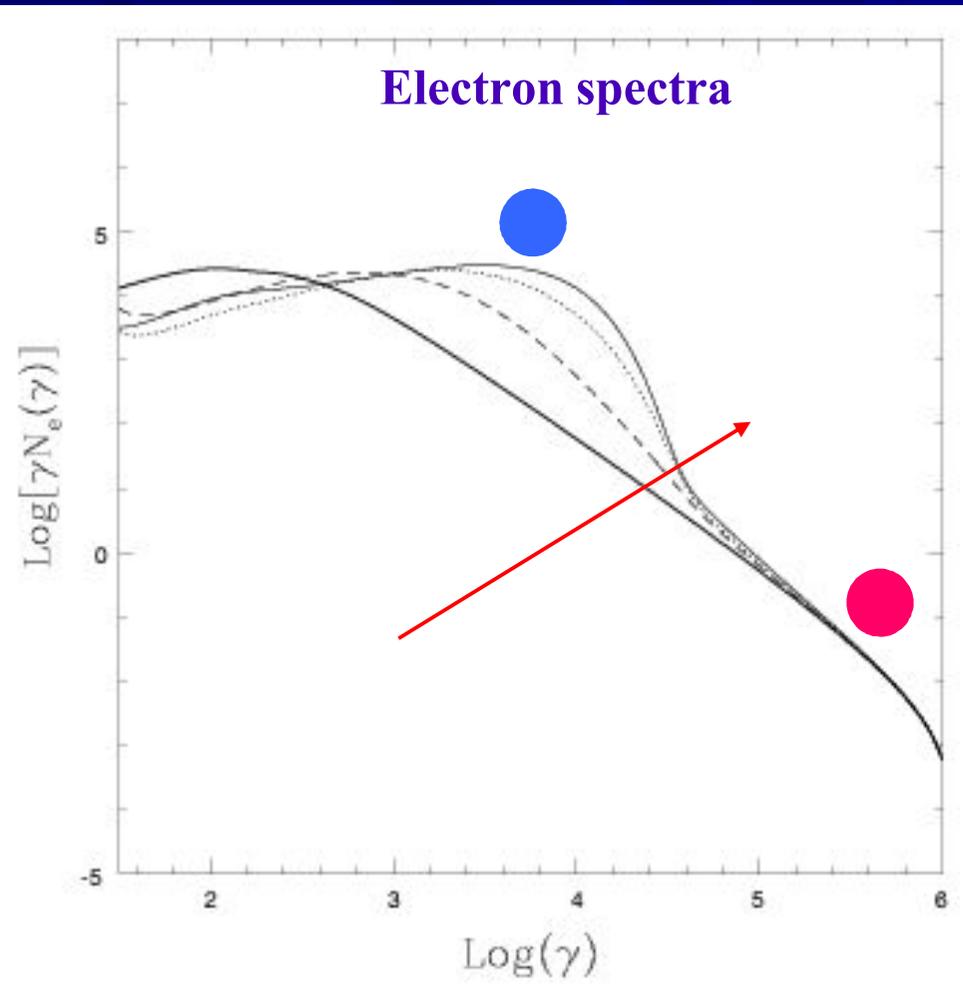
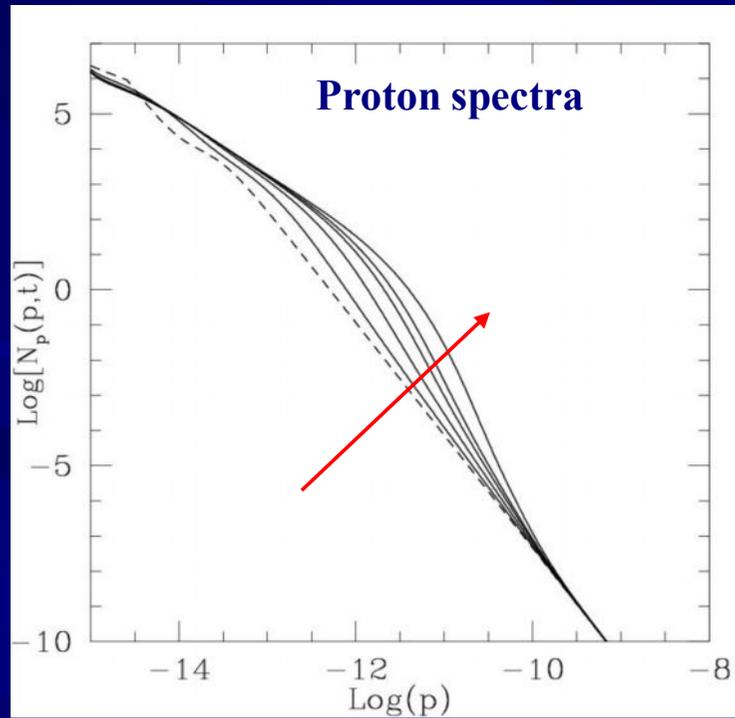
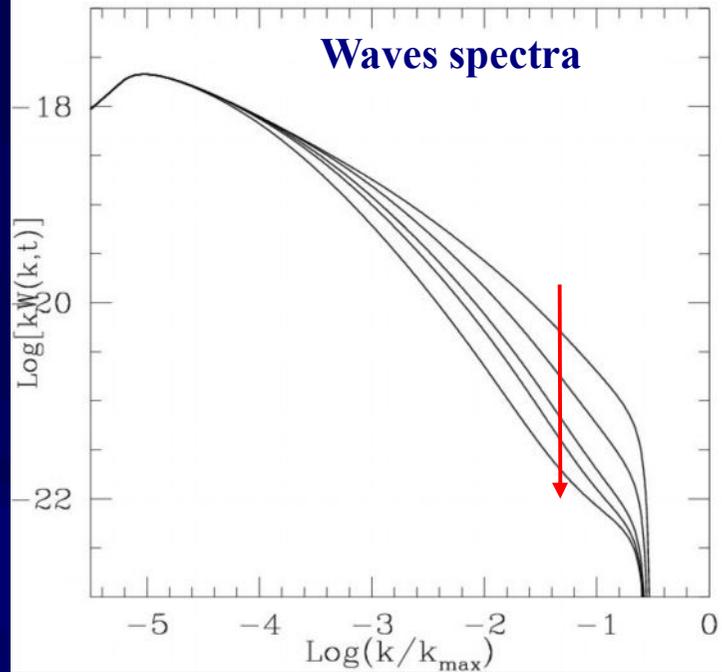
(Brunetti +al. 2004; Brunetti & Blasi 2005)



Waves + Protons + Secondaries

# Full Alfven-Wave--Particle Coupling

(Brunetti +al. 2004; Brunetti & Blasi 2005)

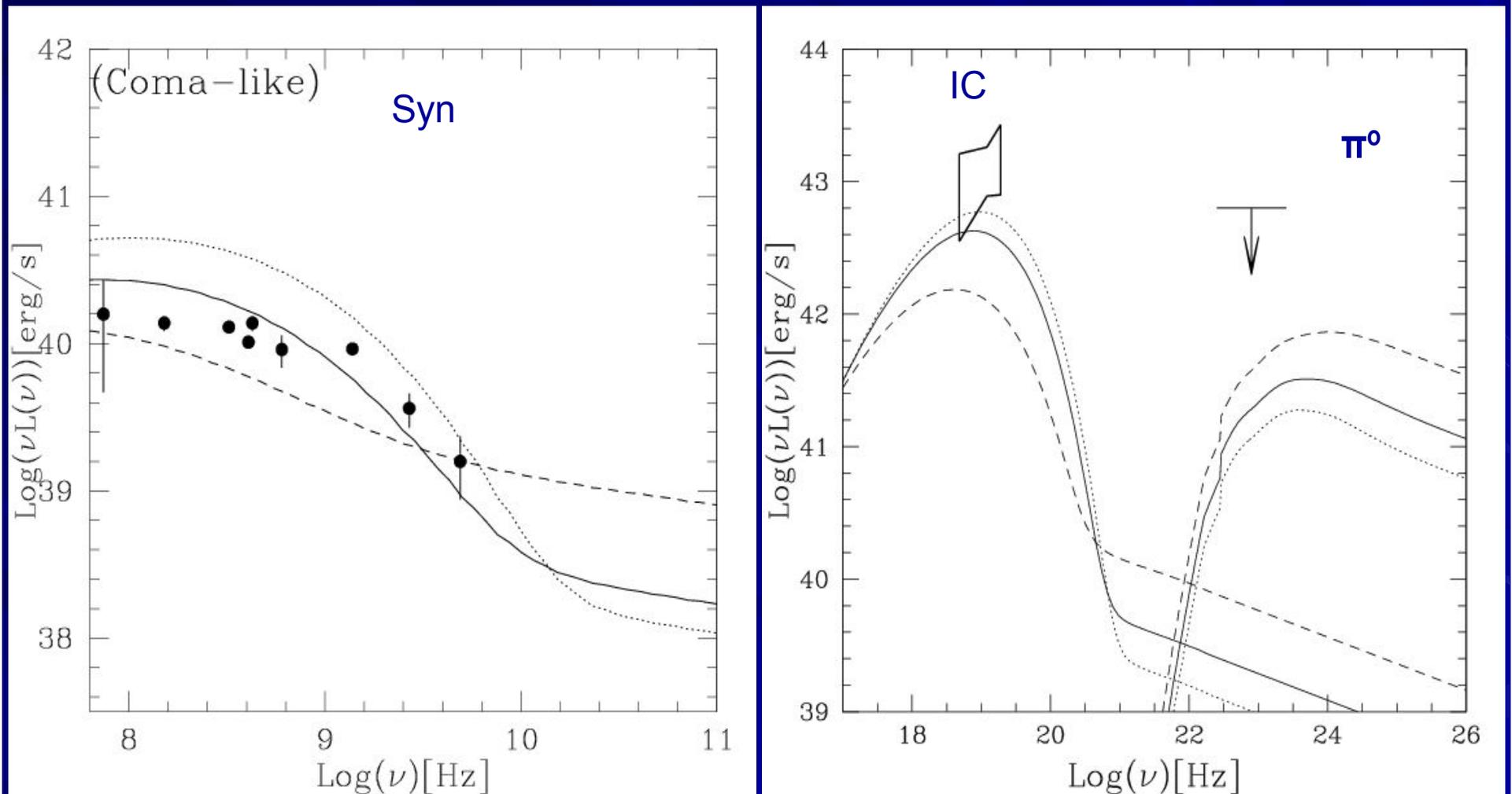


Waves + Protons + Secondaries

# Alfvenic: results

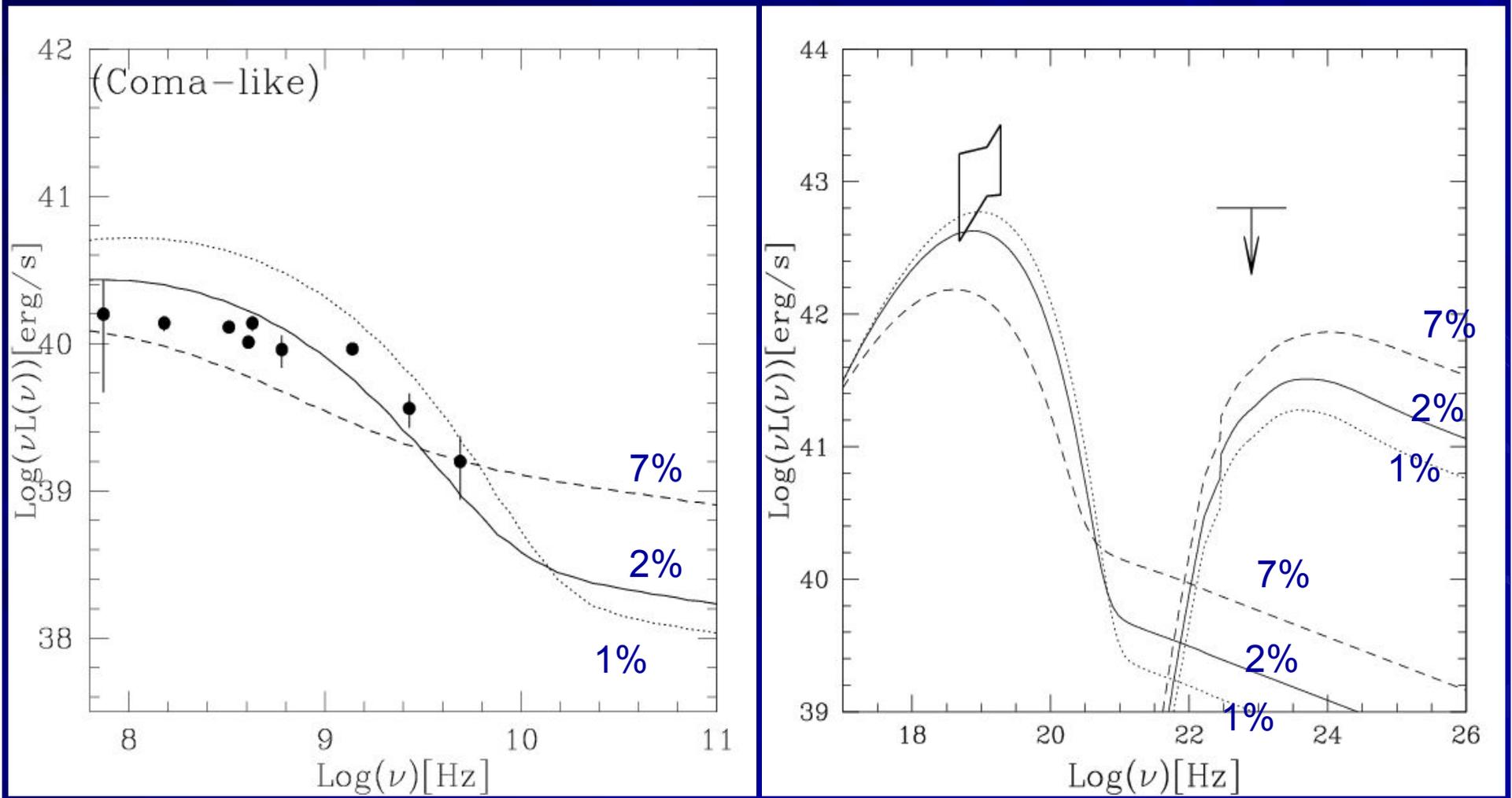
Brunetti, Blasi, Gabici, Cassano, in prep

Toy Model:  $\beta$ -profile,  $B_0 \approx A n_{\text{th}}^{2/3}$ ,  $B_0(0) = 1.5 \mu\text{G}$ ,  $W_{\text{CR}} \approx f W_{\text{th}}$ ,  $P_A \approx Q n_{\text{th}}^{5/6}$



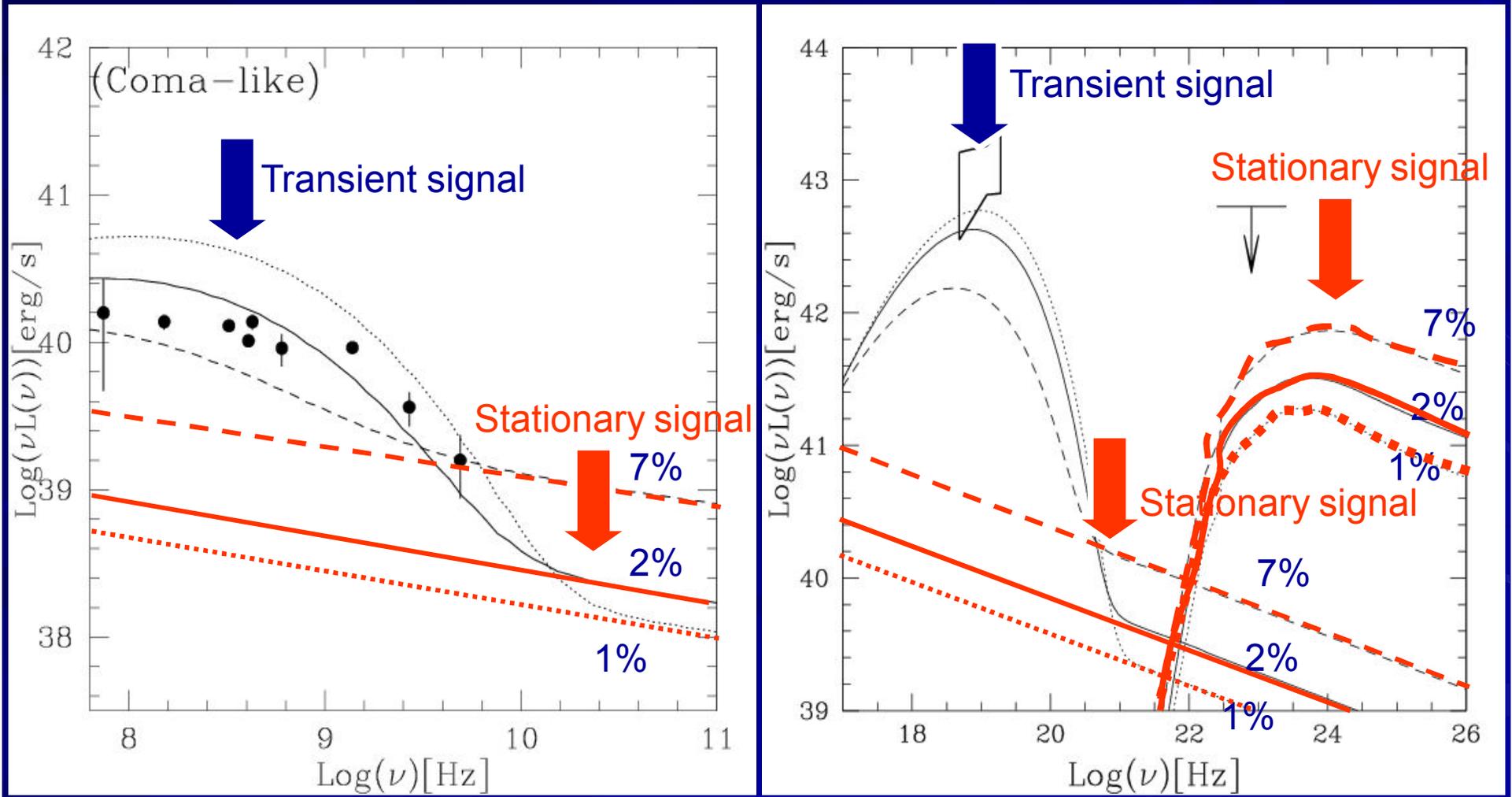
# Alfvenic: results

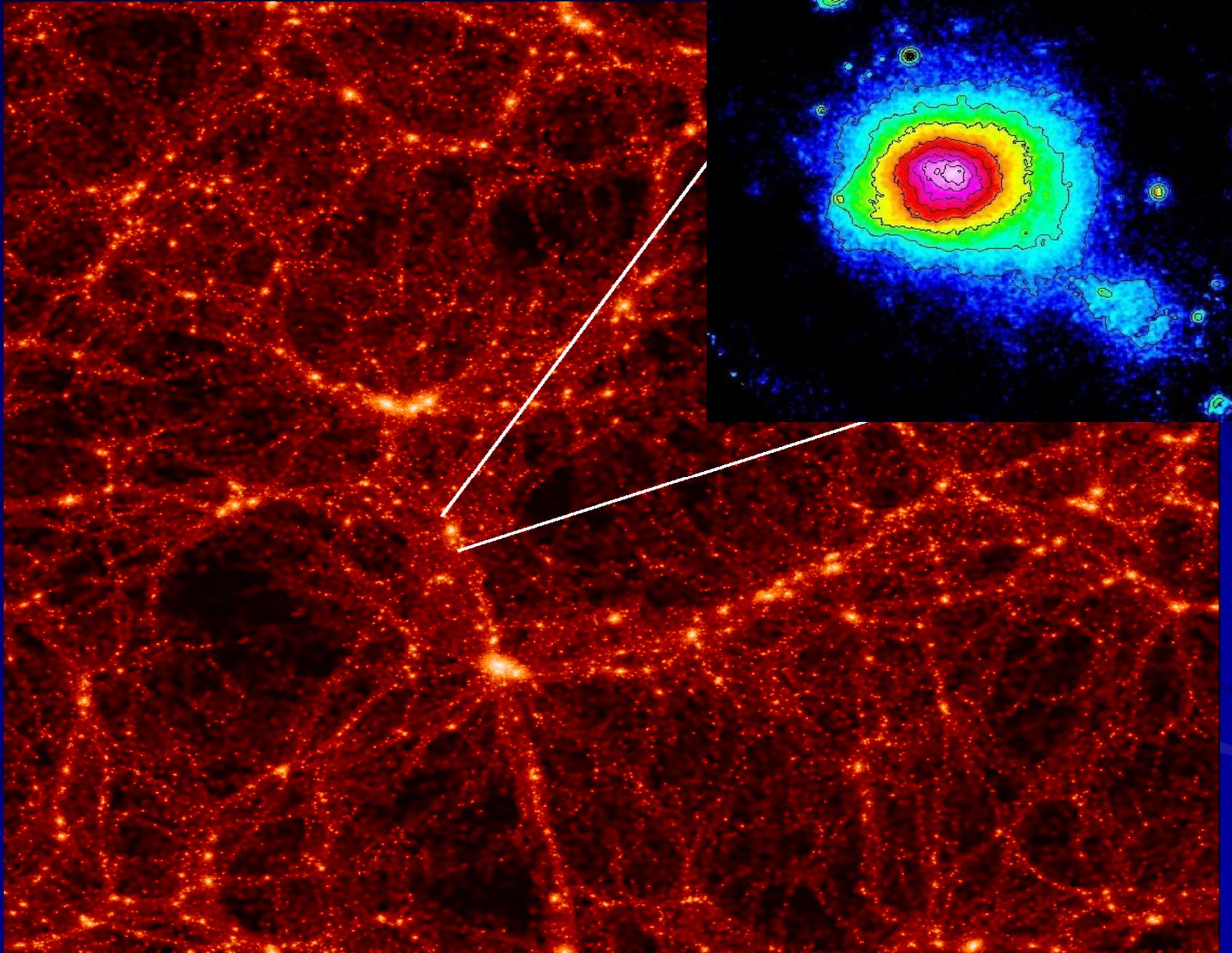
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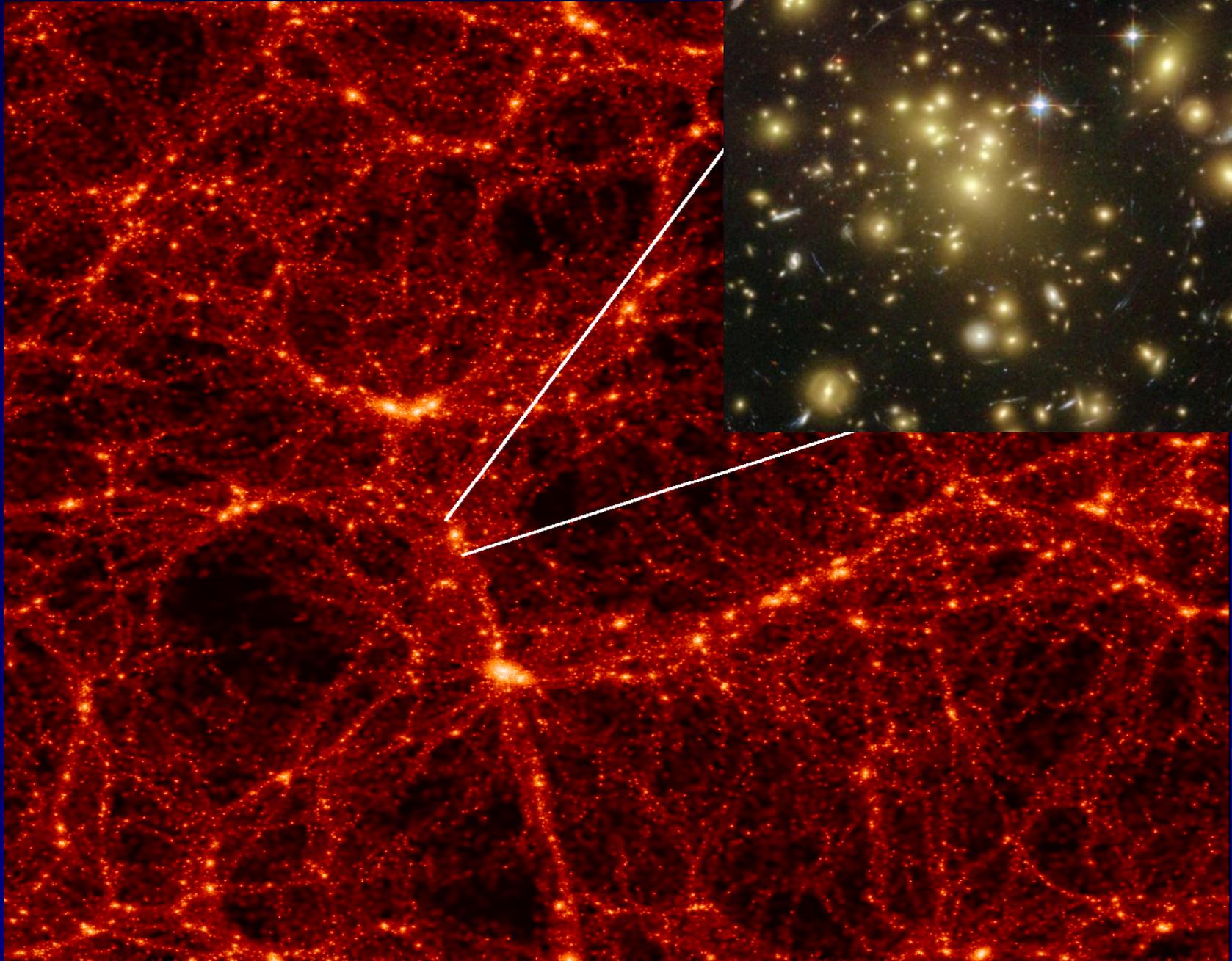


# Alfvenic: results

Toy Model:  $\beta$ -profile,  $B_0 \approx A n_{th}^{2/3}$ ,  $B_0(0)=1.5\mu\text{G}$ ,  $W_{CR} \approx f W_{th}$ ,  $P_A \approx Q n_{th}^{5/6}$

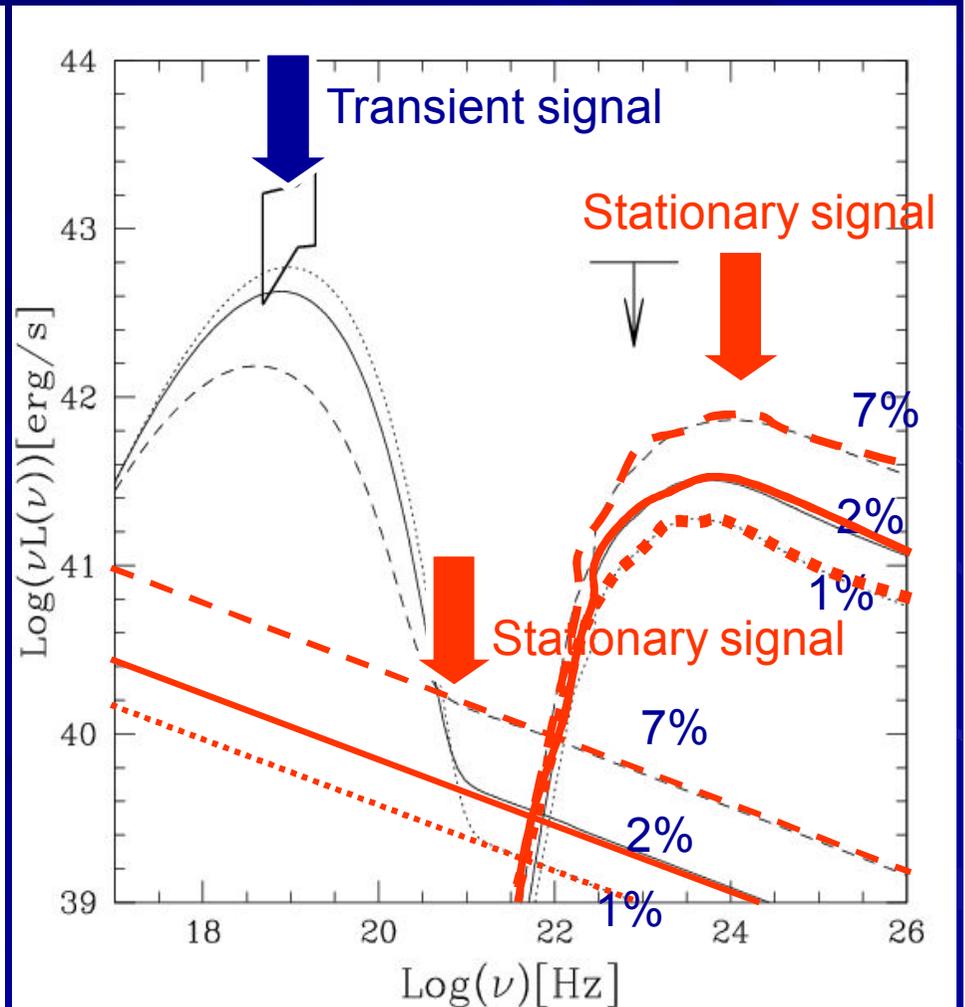
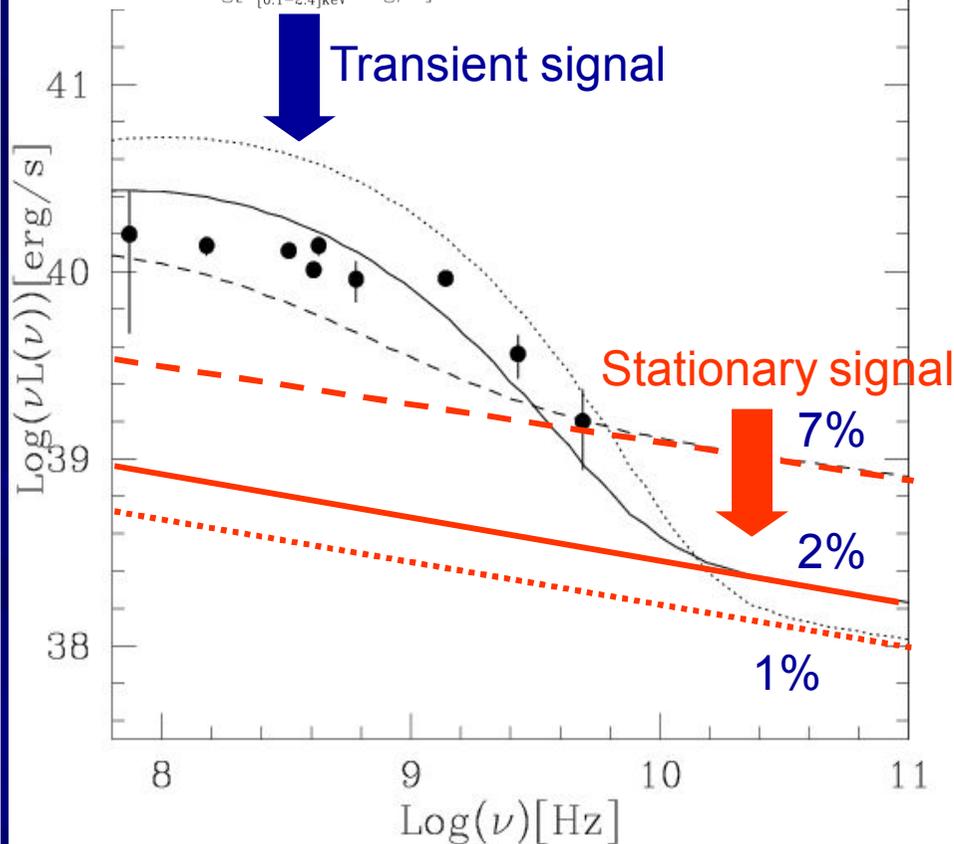
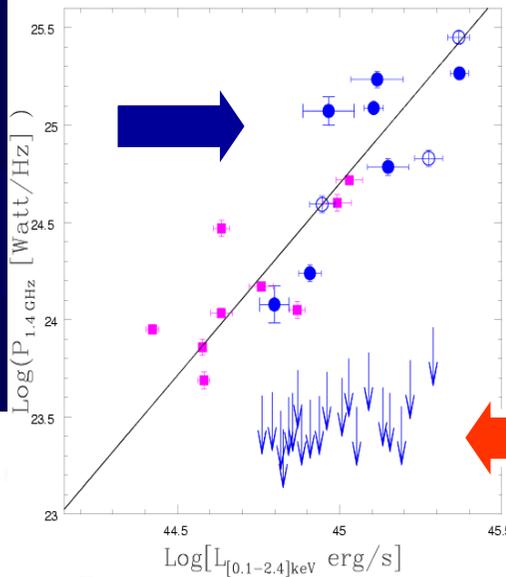






# Alfvenic: results

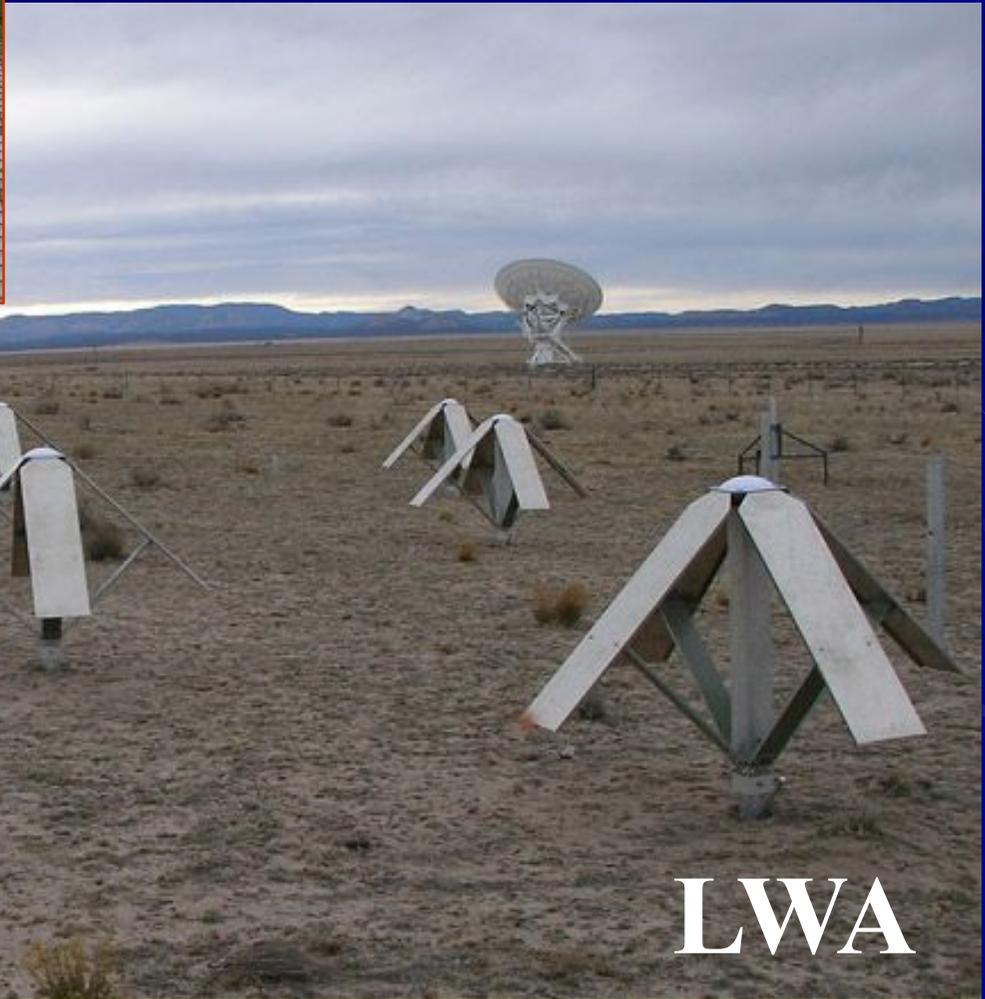
$$e, B_0 \approx A n_{\text{th}}^{2/3}, B_0(0) = 1.5 \mu\text{G}, W_{\text{CR}} \approx f W_{\text{th}}, P_A \approx Q n_{\text{th}}^{5/6}$$



**LOFAR**

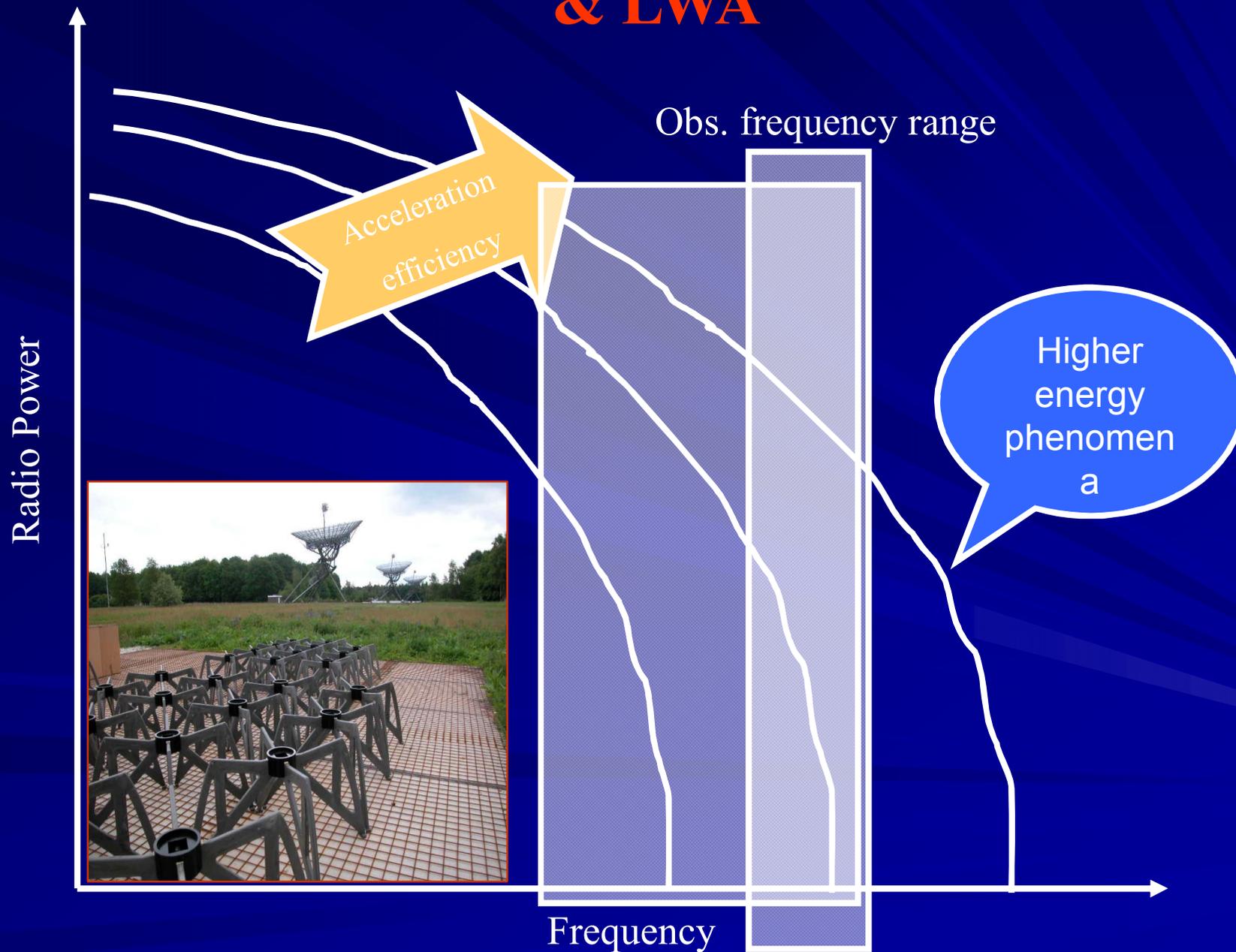


*FUTURE*



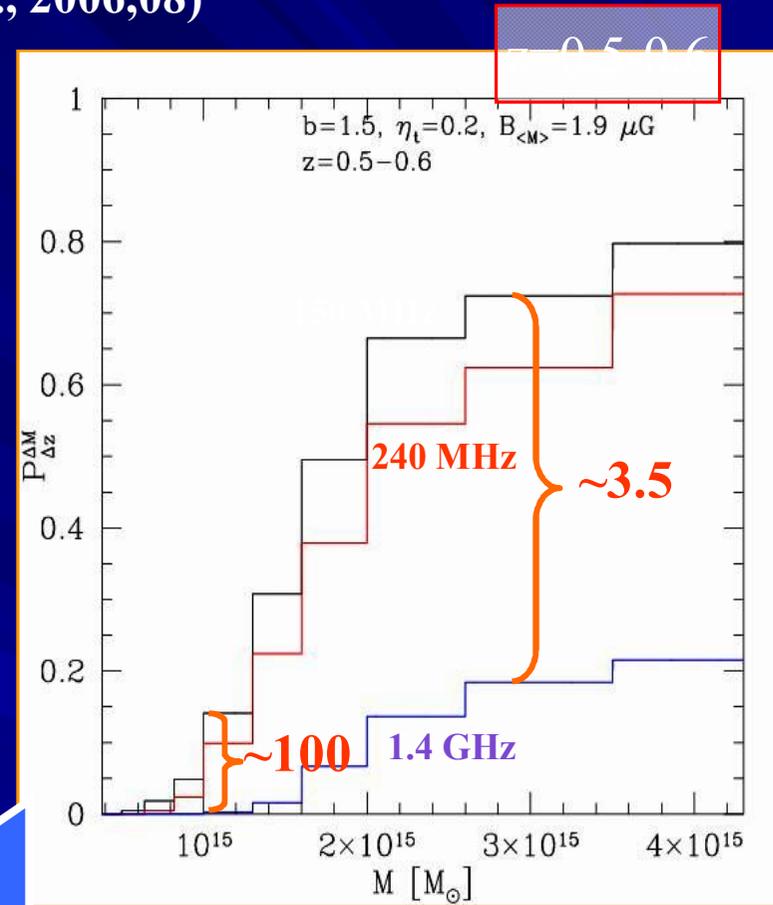
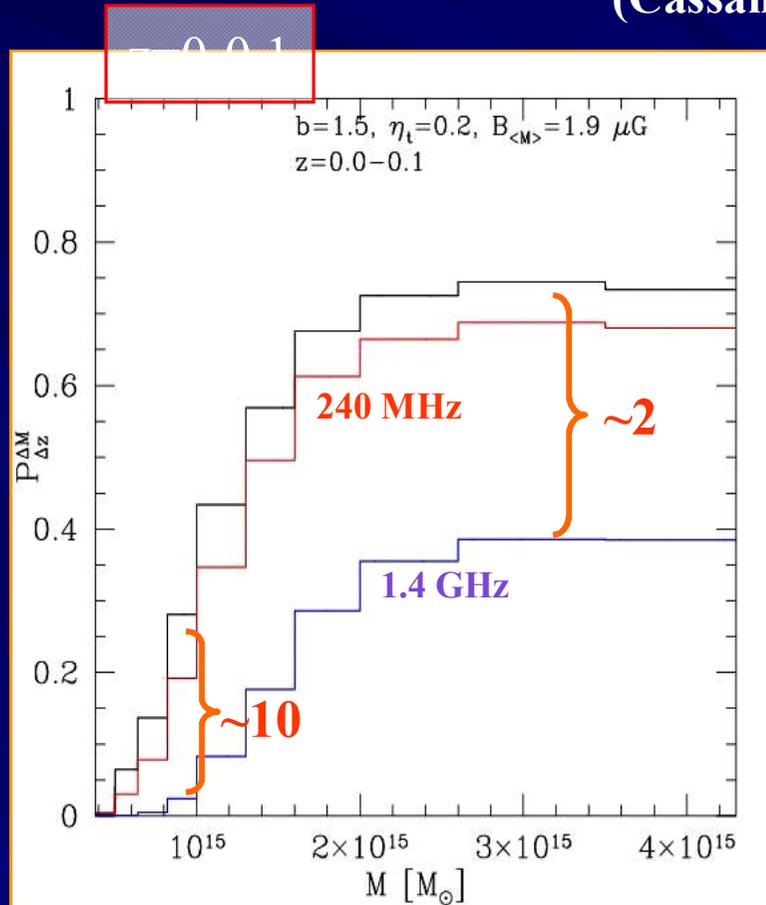
**LWA**

# LOW freq observations: LOFAR & LWA



# Fraction of GC with RHs at lower frequencies

(Cassano et al., 2006,08)



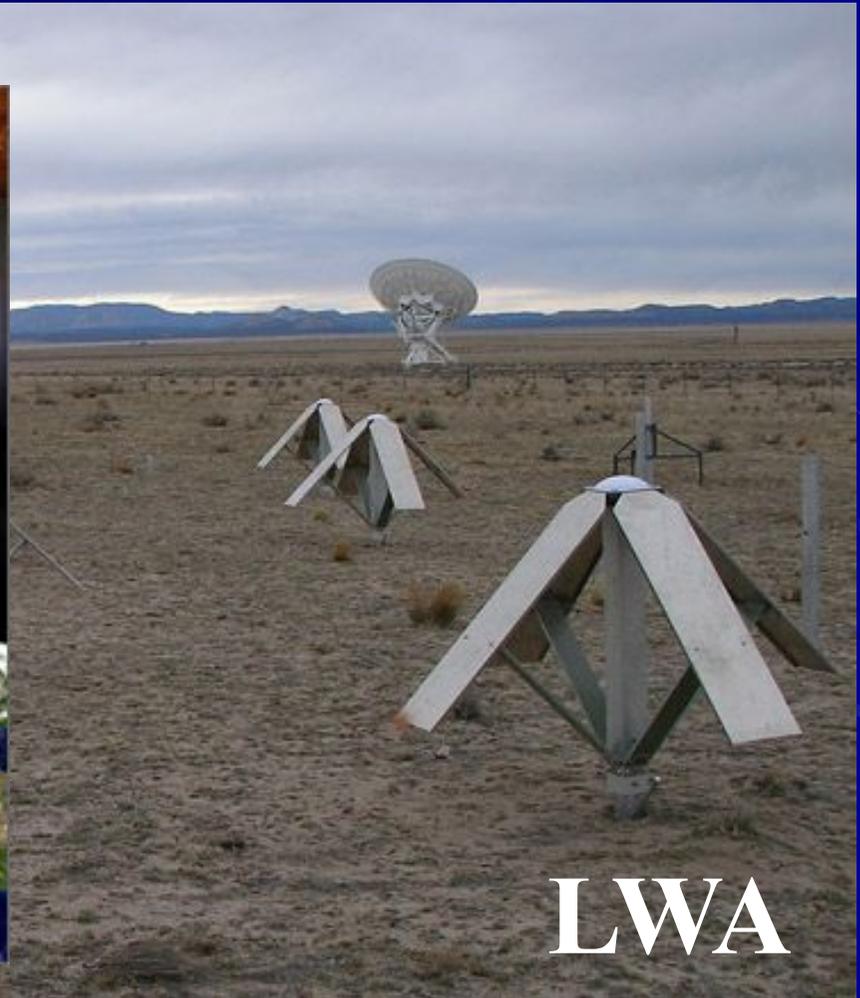
Expectation : Ultra-Steep-Spectrum Radio Halos

**LOFAR**



*FUTURE*

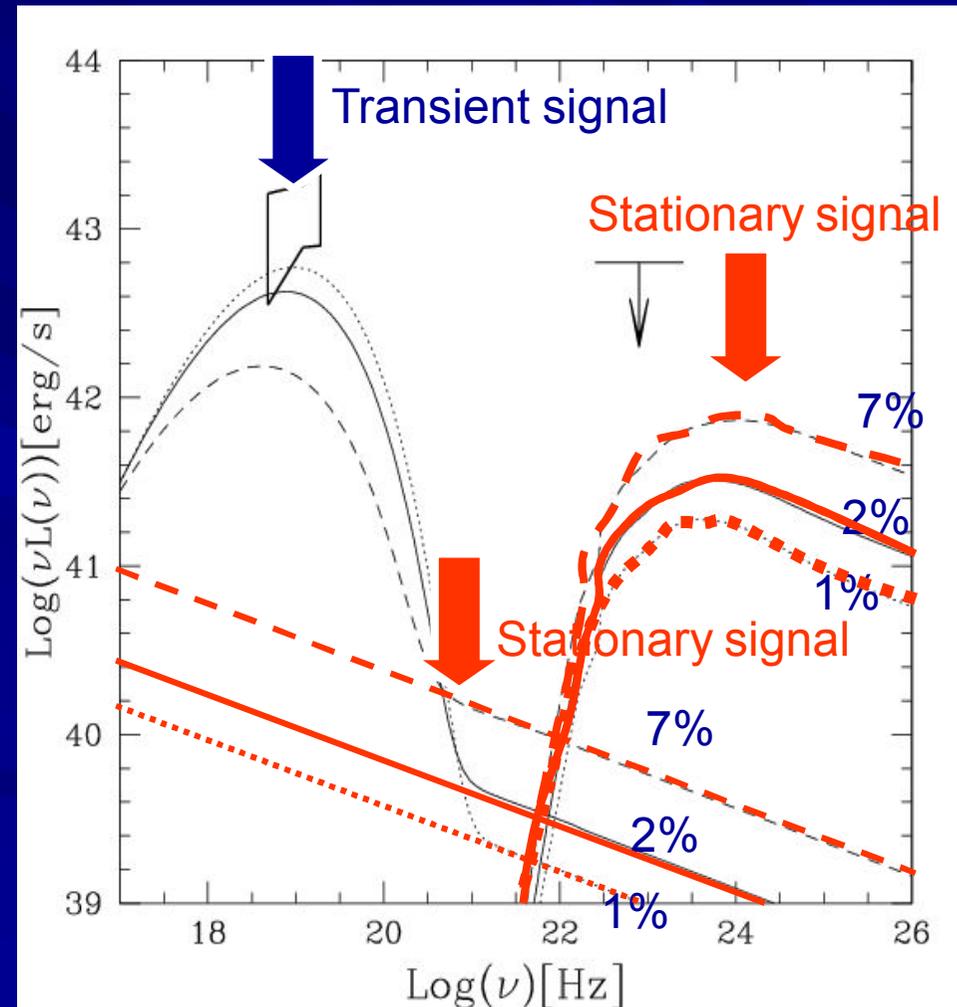
**Glast**



**LWA**

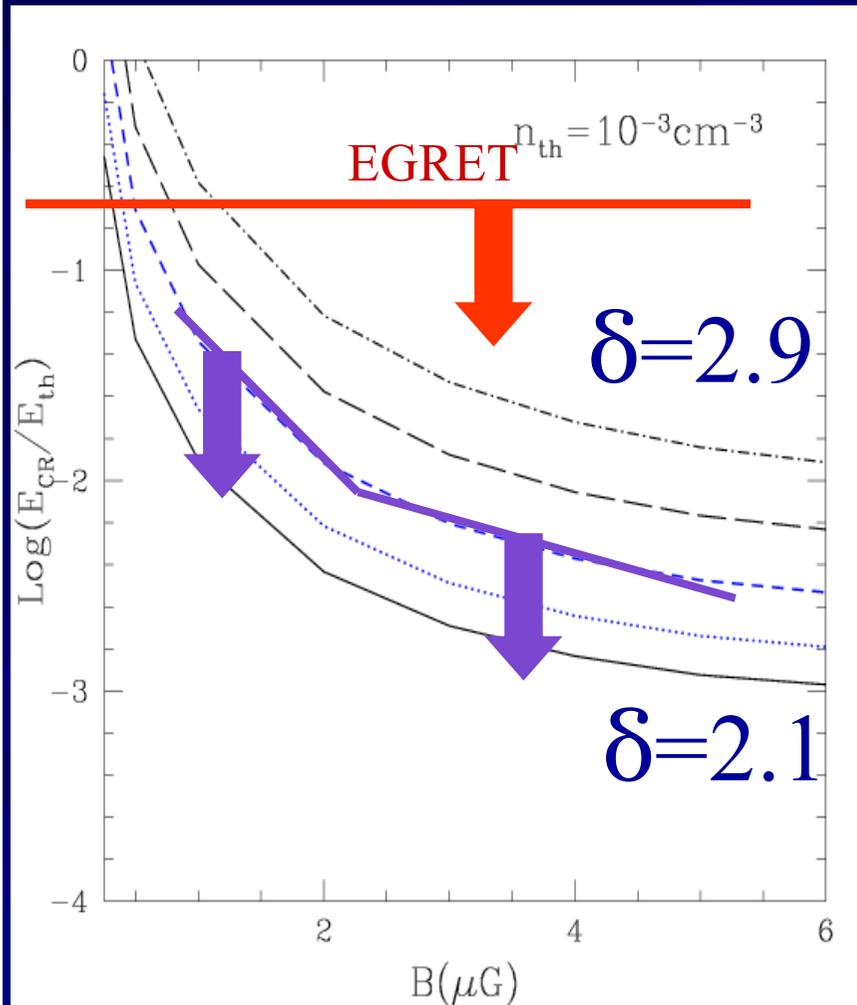
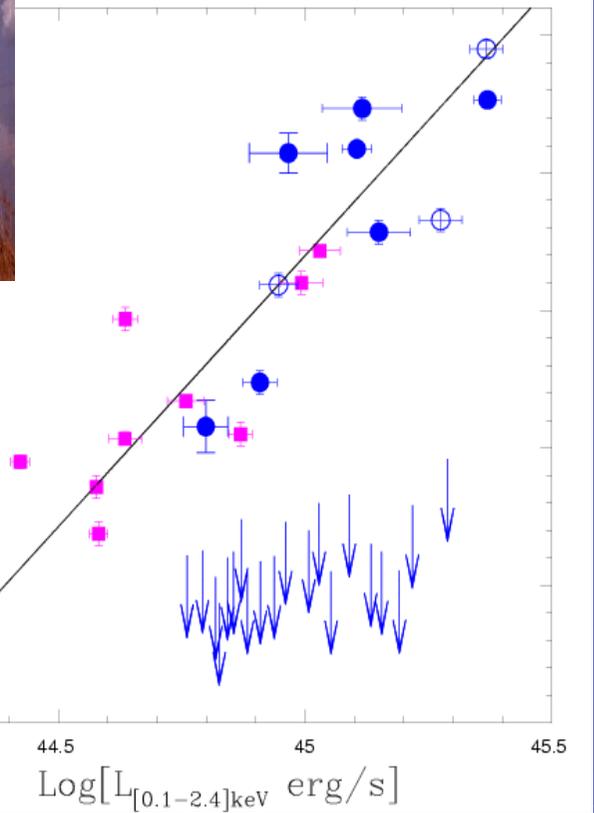
# Alfvenic: results

The gamma ray signal yields a direct estimate of CR protons



# .. limits on CR protons

Brunetti +al. 2007

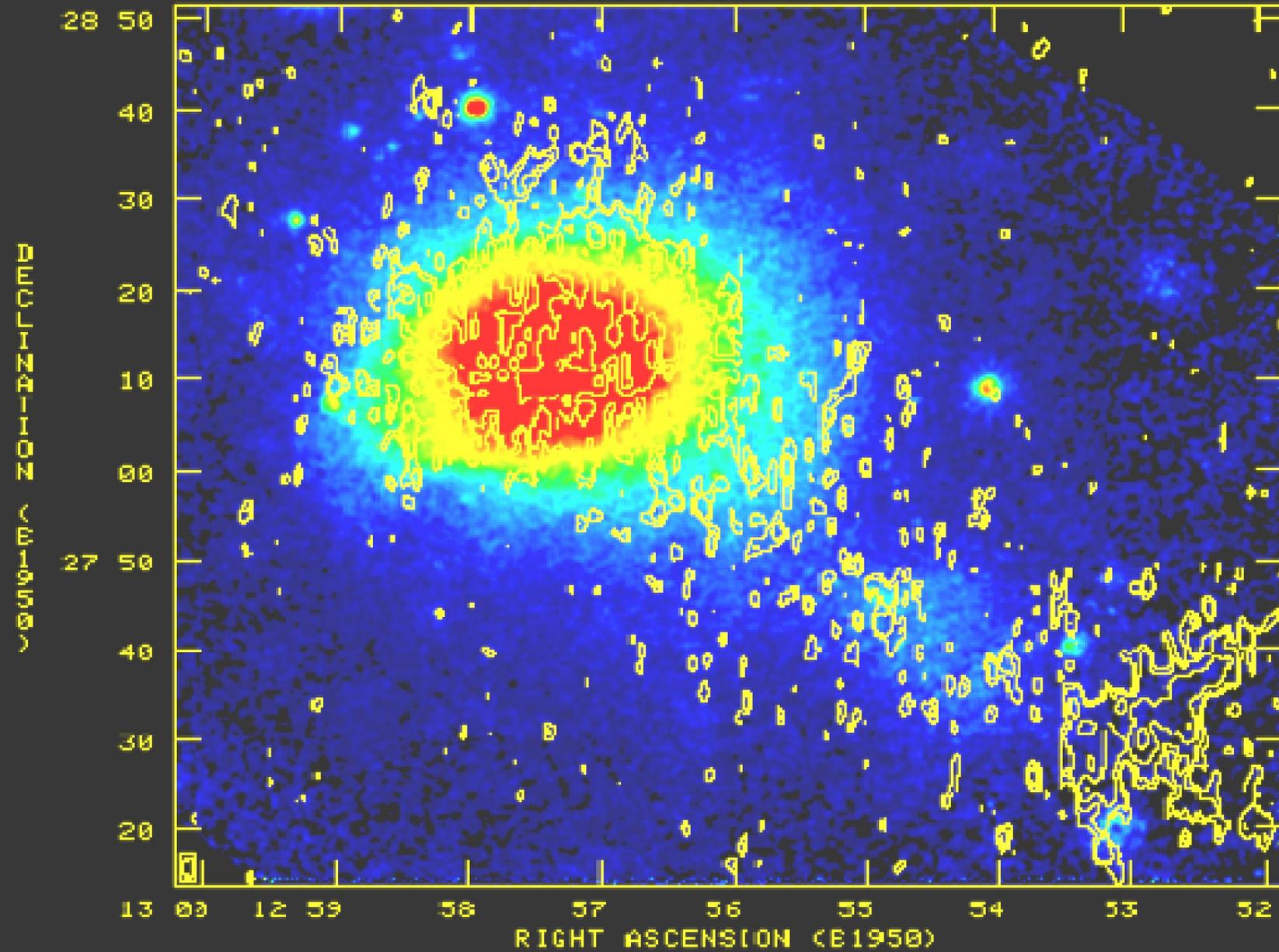


Synchrotron emission from secondaries should be smaller than upper limits .

limit on :  $B$  ,  $E_{CRp}$  ,  $\delta$

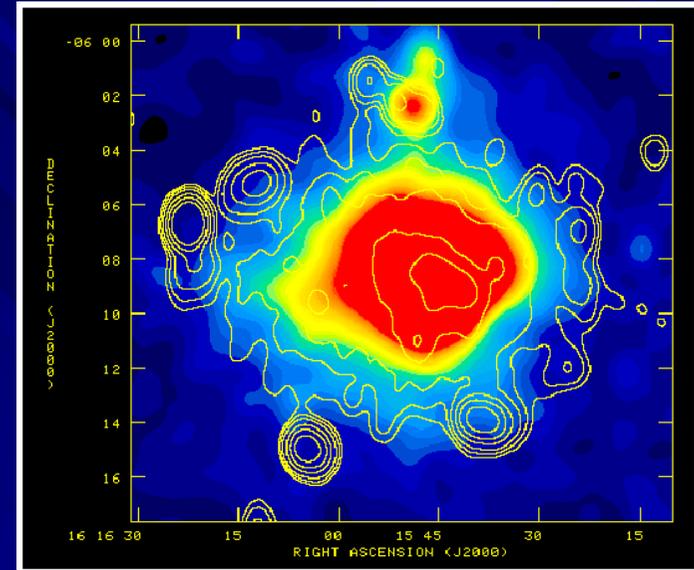


# Coma Cluster



Feretti +al.1998

# Origin of the emitting electrons

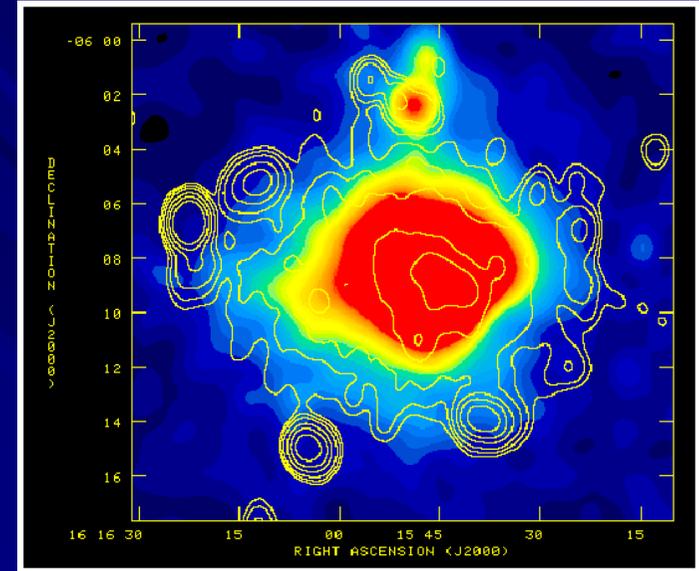
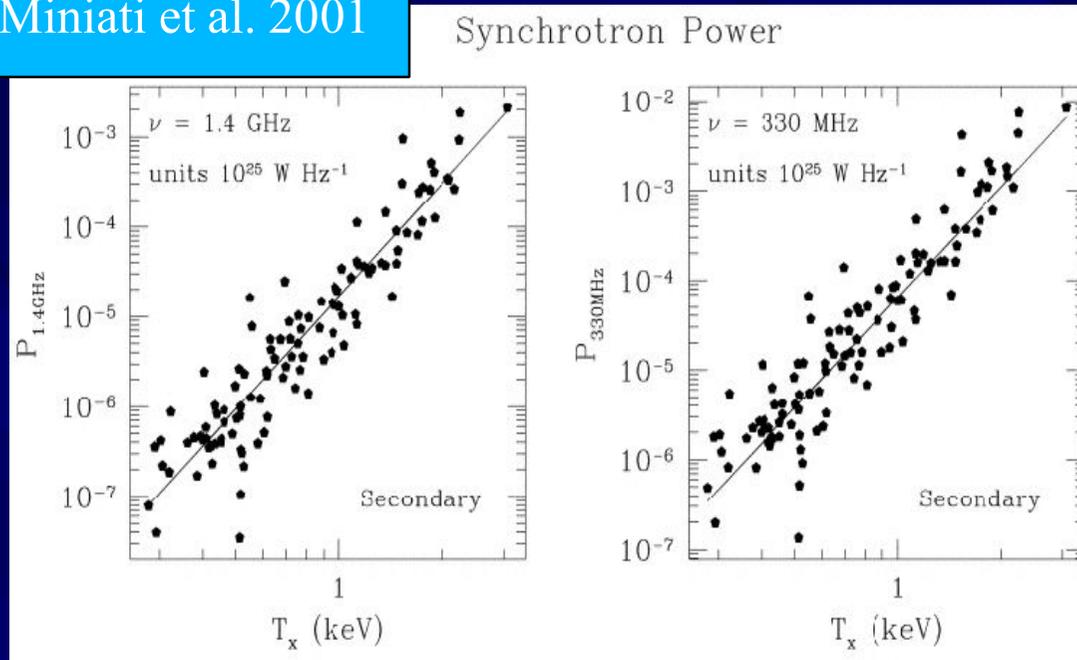


First possibility: *secondary models*, relativistic electrons continuously injected in the ICM by inelastic proton-proton collisions through productions and decay of charged pions (e.g., *Dennison 1980, Blasi & Colafrancesco 1999, Dolag & Ensslin 2000; Pfrommer & Ensslin 2004*)

Second possibility : *in situ re-acceleration* by MHD turbulence developed in the cluster volume during the merger events (e.g., *Brunetti et al. 2001, 2004; Petrosian 2001; Ohno et al. 2002; Fujita et al. 2003; Brunetti & Blasi 2005; Cassano & Brunetti 2005; Brunetti & Lazarian 2007; Petrosian & Bykov 2008*)

# Drawback of secondary models

Miniati et al. 2001

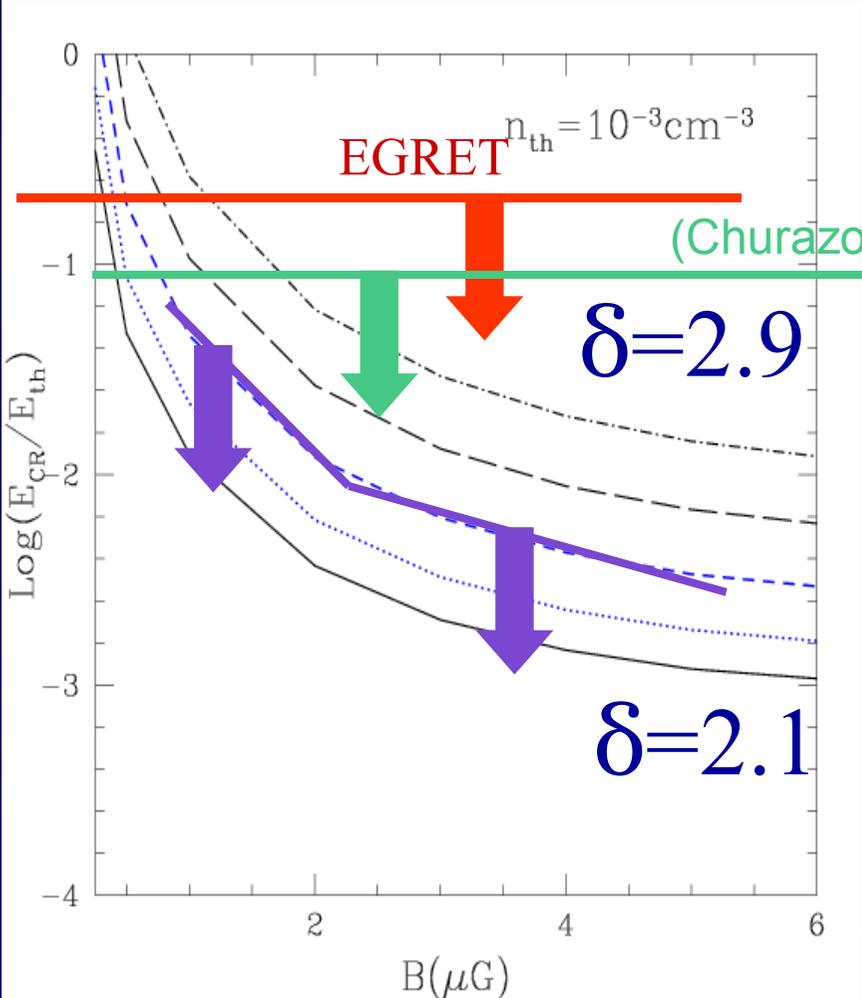
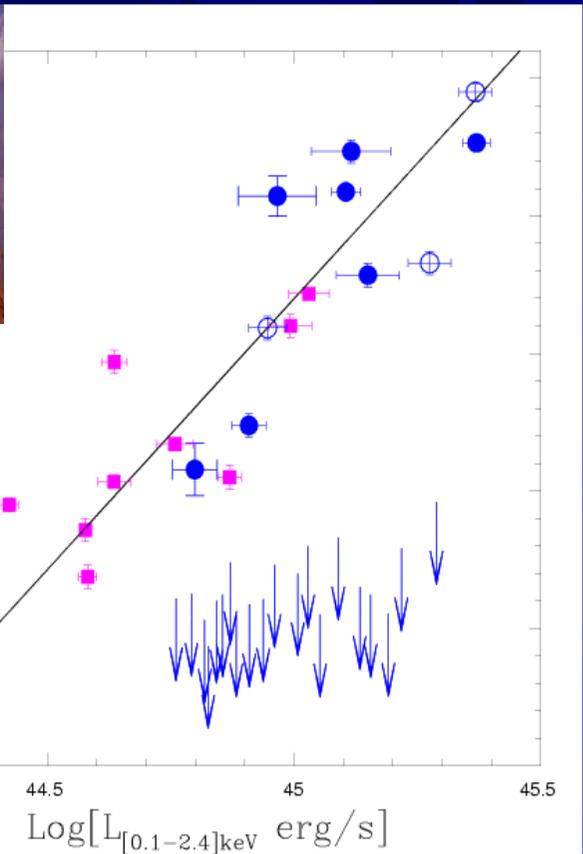


**In case clusters have similar magnetic fields :**

- Radio Halos are long living (cluster “life-time”) phenomena (difficult to understand connection with mergers)
- Clusters with similar thermal properties have similar radio halos

# .. limits on CR protons

Brunetti +al. 2007



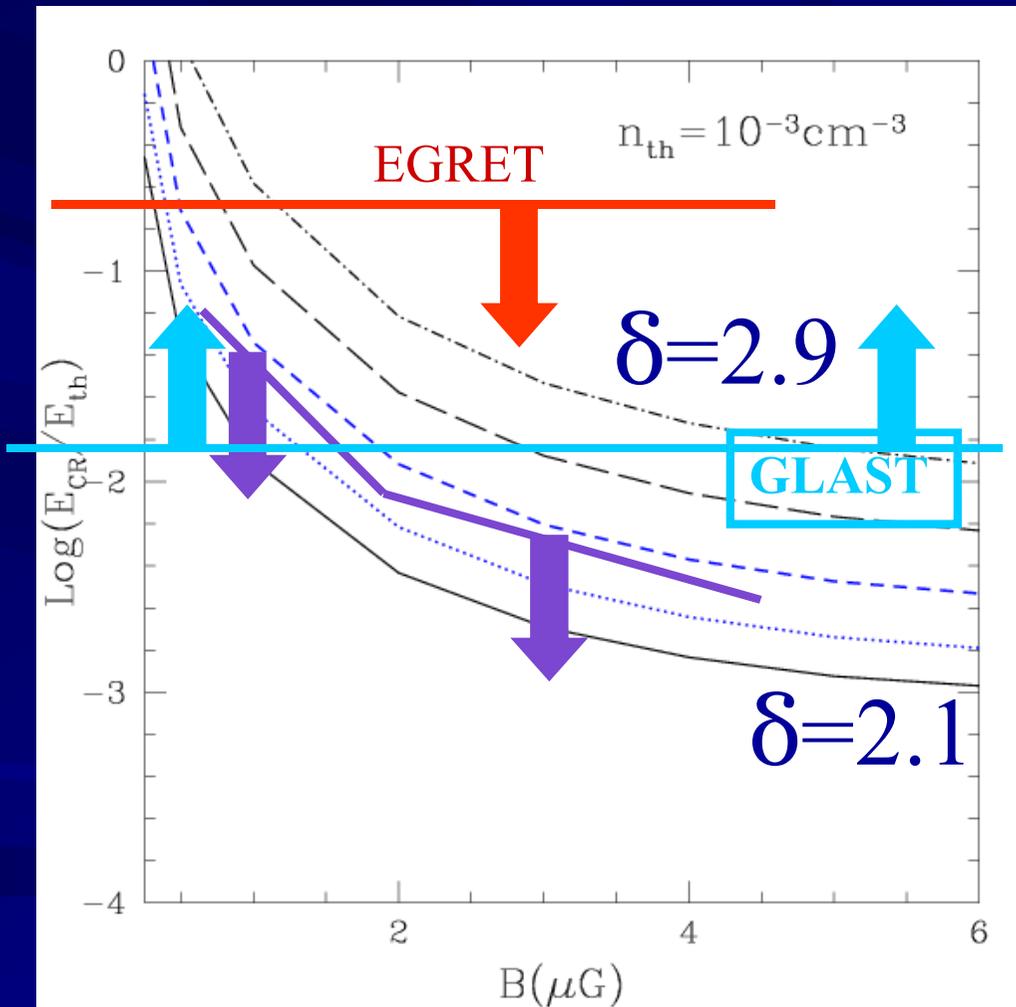
Synchrotron emission from secondaries should be smaller than upper limits .

limit on :  $B$  ,  $E_{CRp}$  ,  $\delta$



# GLAST: CR & B in GC

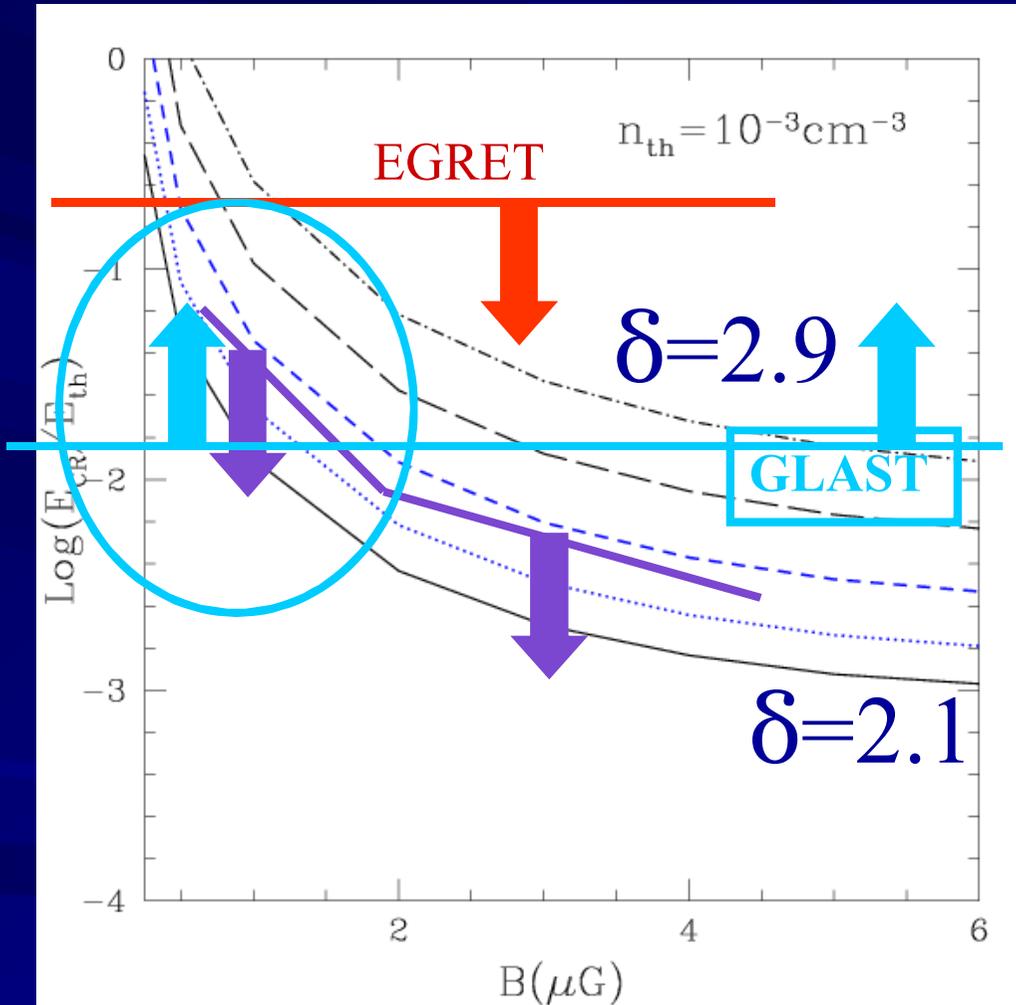
Brunetti +al. 2007



The combination of synchrotron observations (limits) of clusters without RHs with GLAST observations will constrain also B !

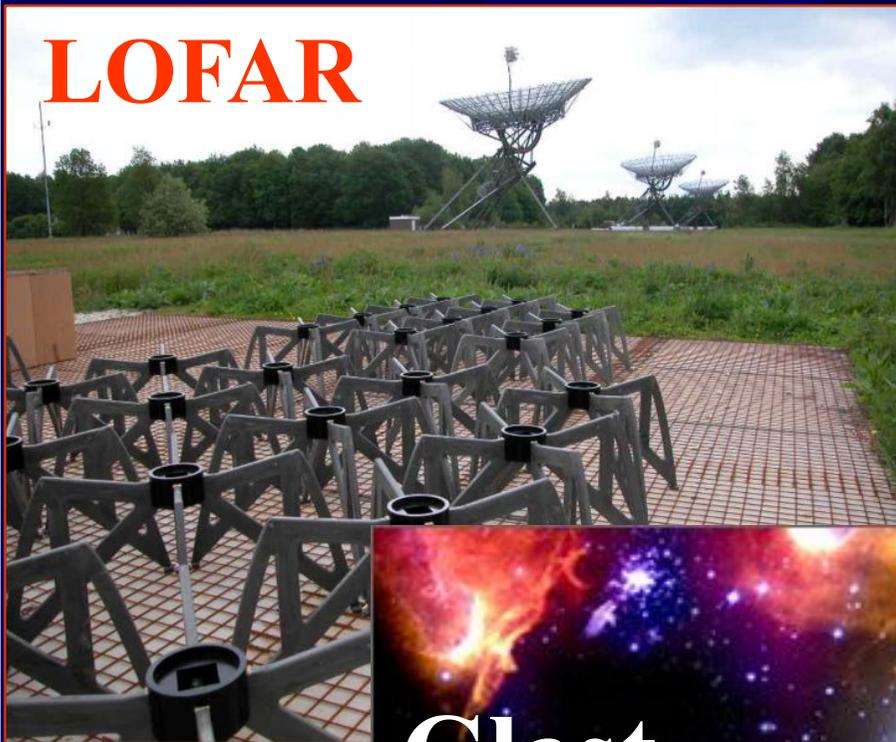
# GLAST: CR & B in GC

Brunetti +al. 2007

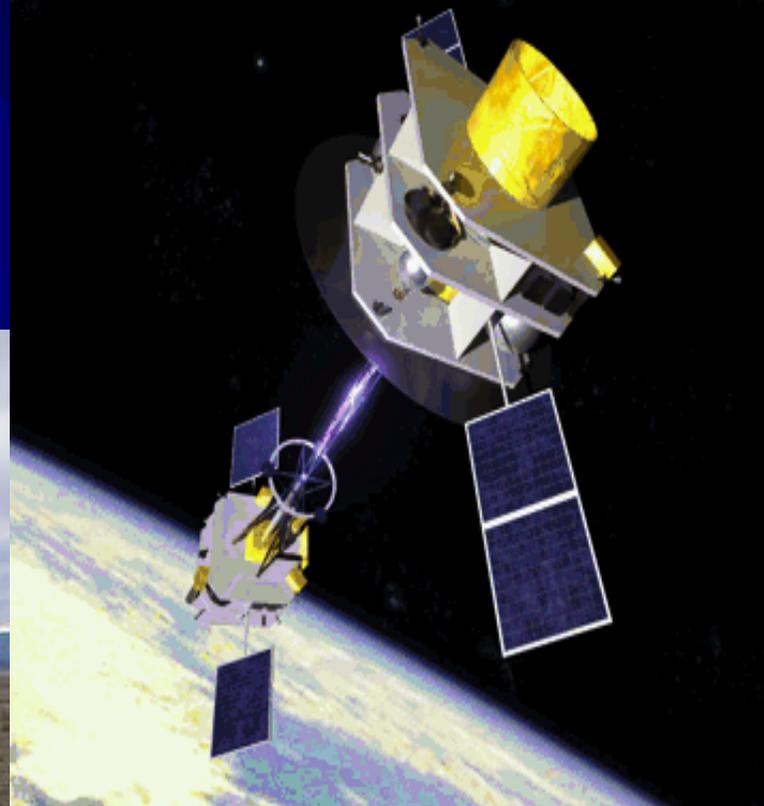


The combination of synchrotron observations (limits) of clusters without RHs with GLAST observations will constrain also  $B$  !

**LOFAR**



**Simbol-X + Next + Nustar**



**Glast**

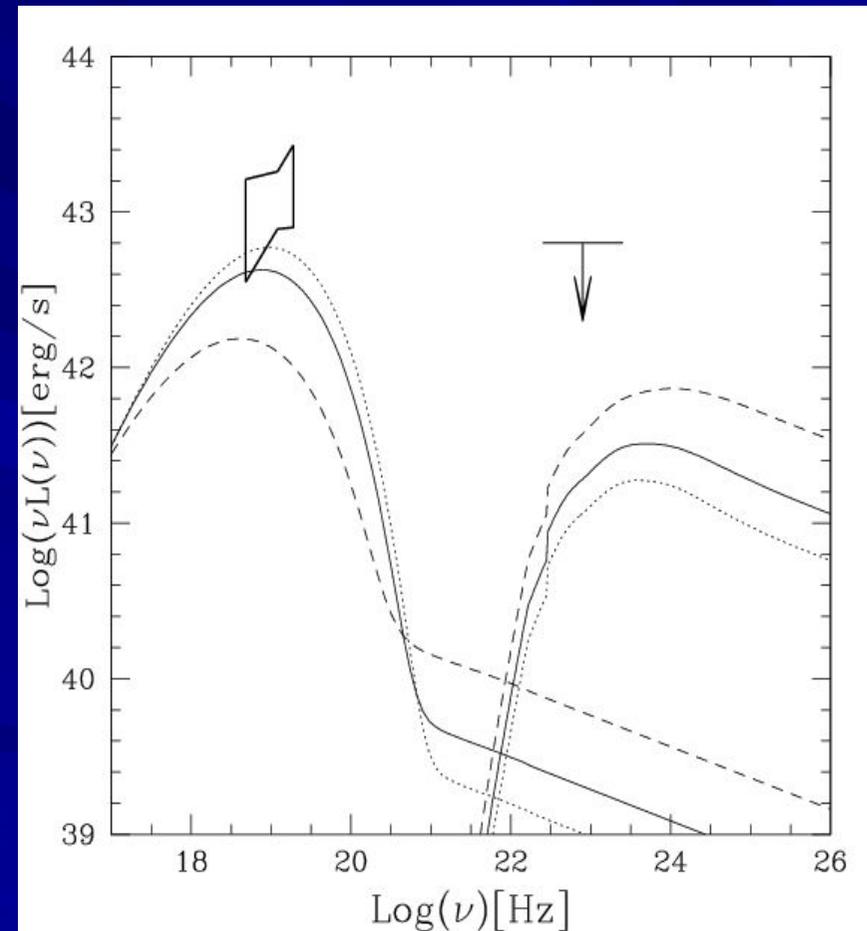
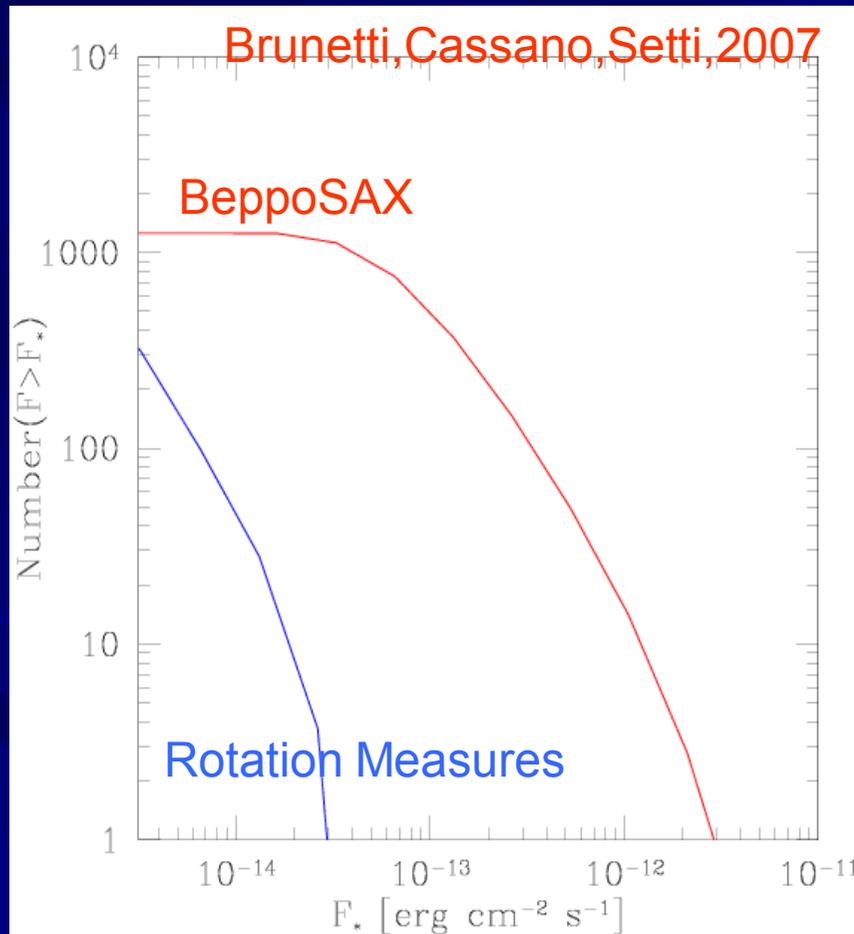


**LWA**



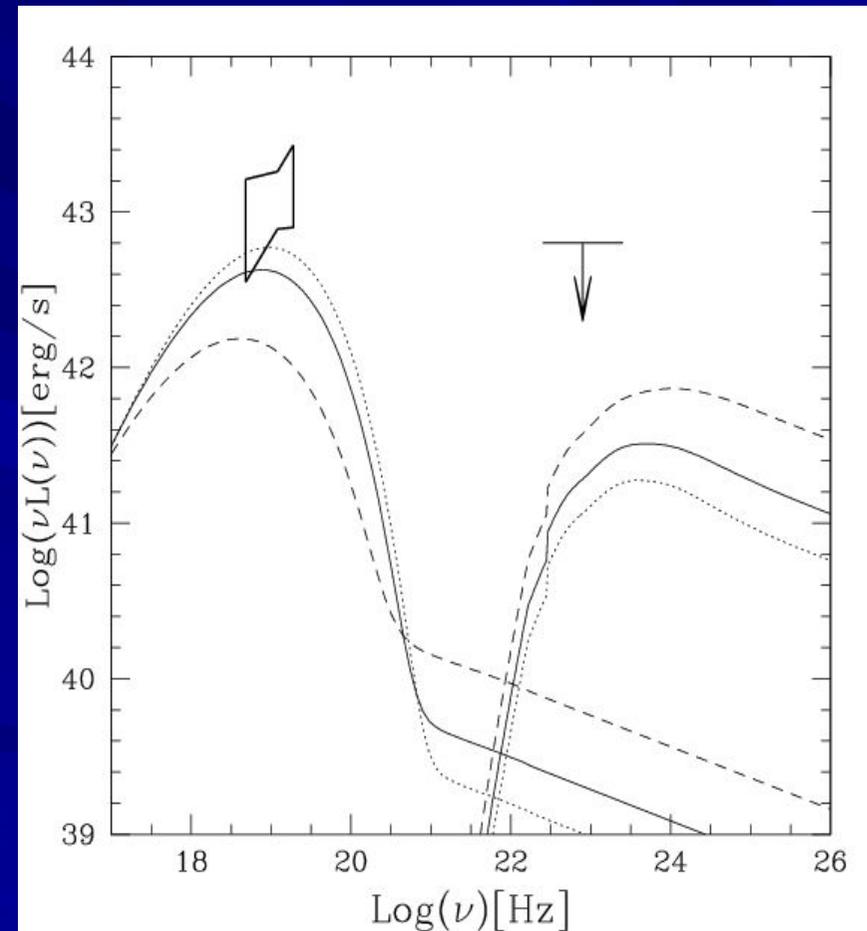
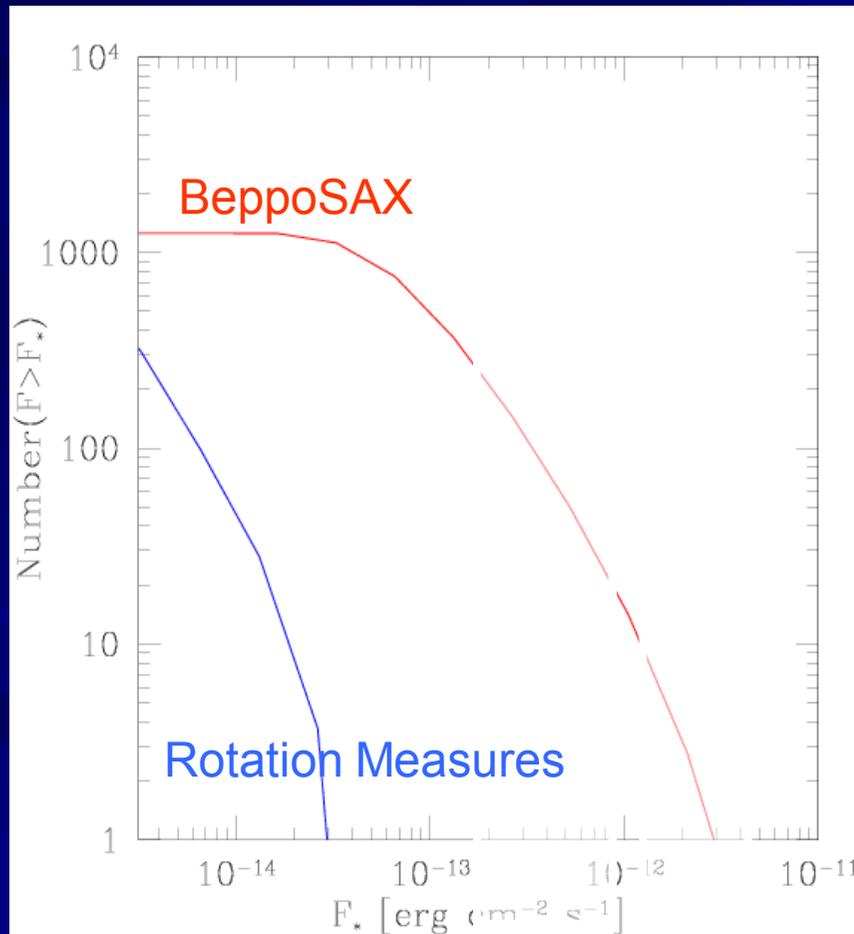
# Simbol-X + Next + Nustar

The level of IC emission from the radio emitting regions in Radio Halos depends on the magnetic field.



# Simbol-X + Next + Nustar

Future hard X-ray telescopes will give a final(?) answer on the strength of the magnetic field in the IGM



# Summary

Turbulent  
acceleratio  
n

**Observations:** bi-modality of GC (radio “quiet” & radio “loud”)

**Observations:** break/cut-off in the synchrotron spectrum of RH

**Observations:** new class of RH (USSRH)

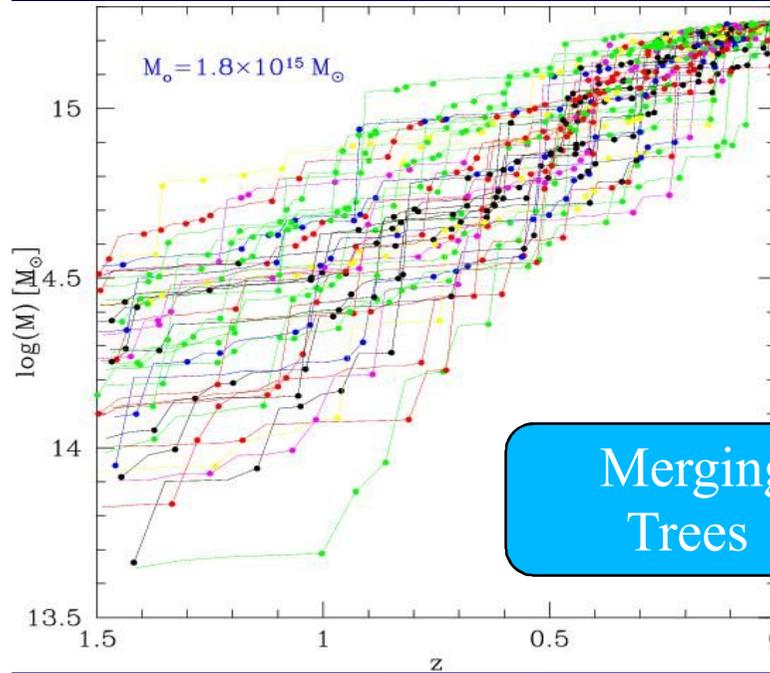
**Models:** magnetosonic acceleration (... need pitch angle scattering)  
(... need really turbulent media)

**Models:** Alfvénic acceleration (... need injection driven by KPIs)

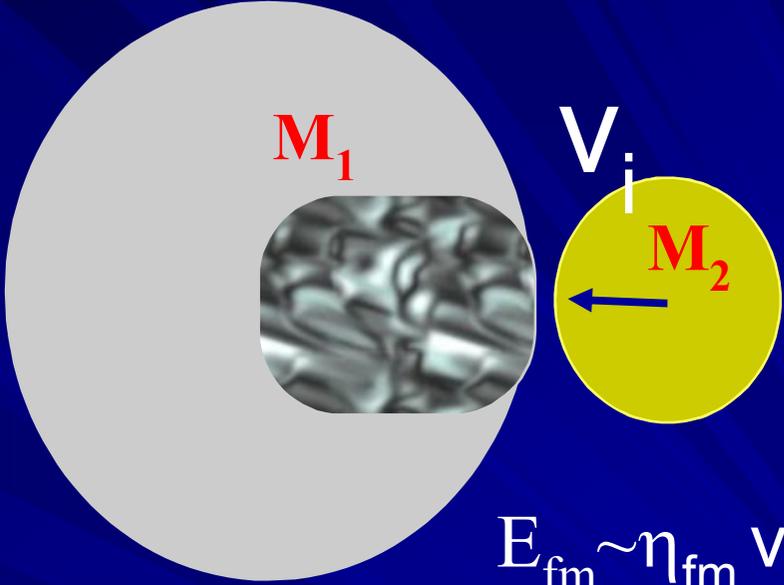
**Future:** USSRH and spectral studies of RH (LOFAR, LWA)  
Hard-X-rays (Simbol-X, Nustar, Next)  
Gamma-rays (GLAST, Cerenkov)

# HXR: Calculations

Cassano & Brunetti 2005; Cassano et al. 2006

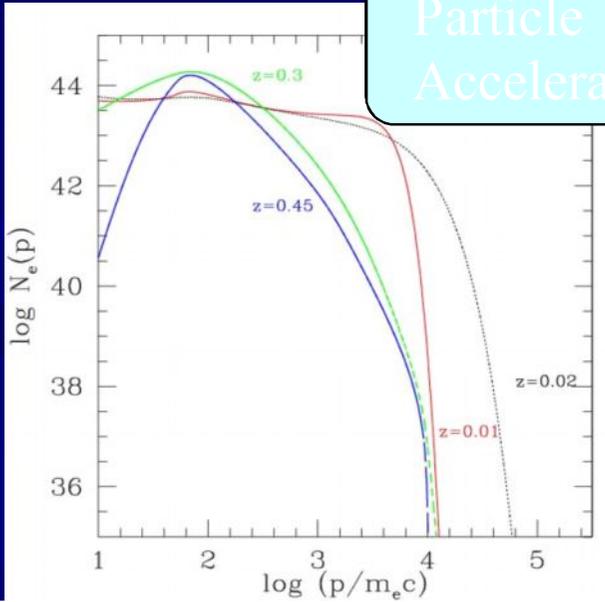


Merging  
Trees

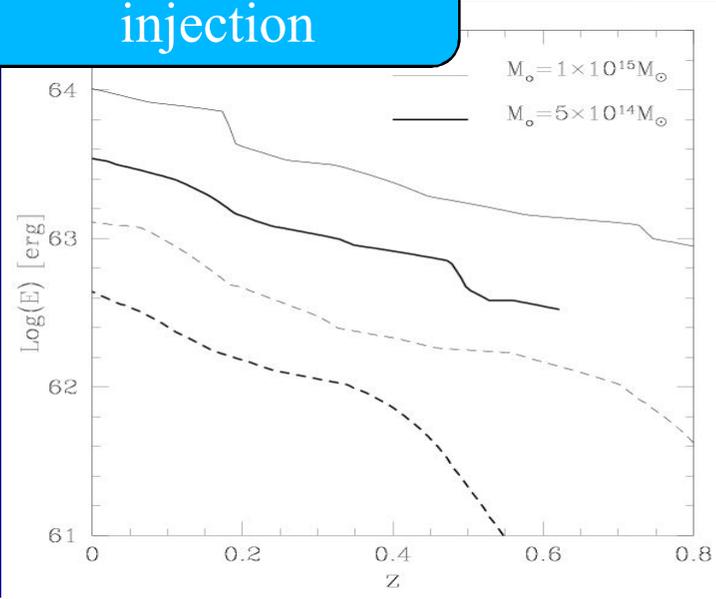


$$E_{fm} \sim \eta_{fm} v_i^2$$

Turbulent  
injection

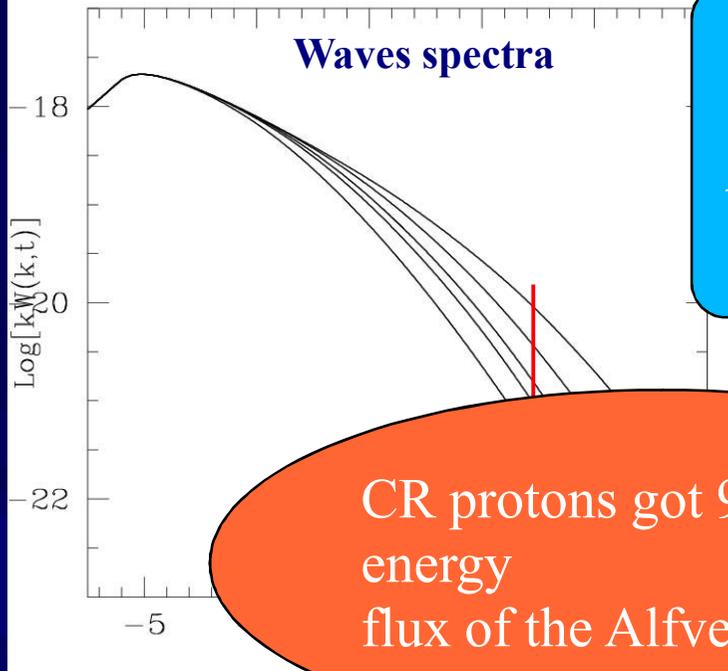


Particle  
Acceleration

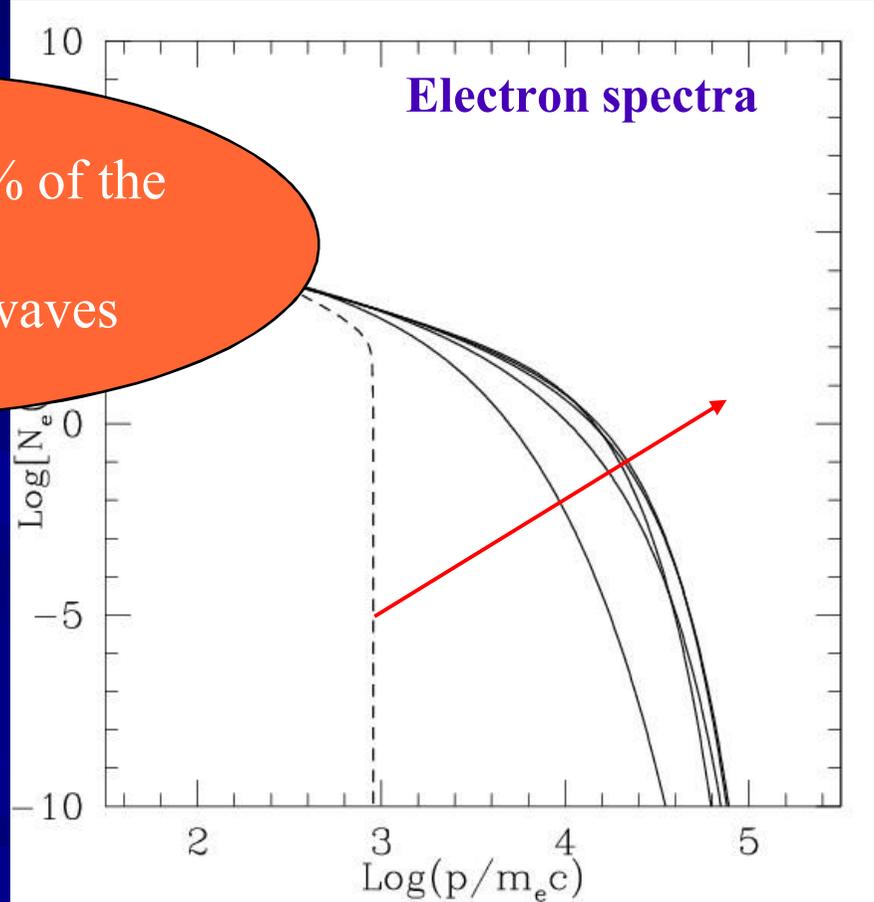
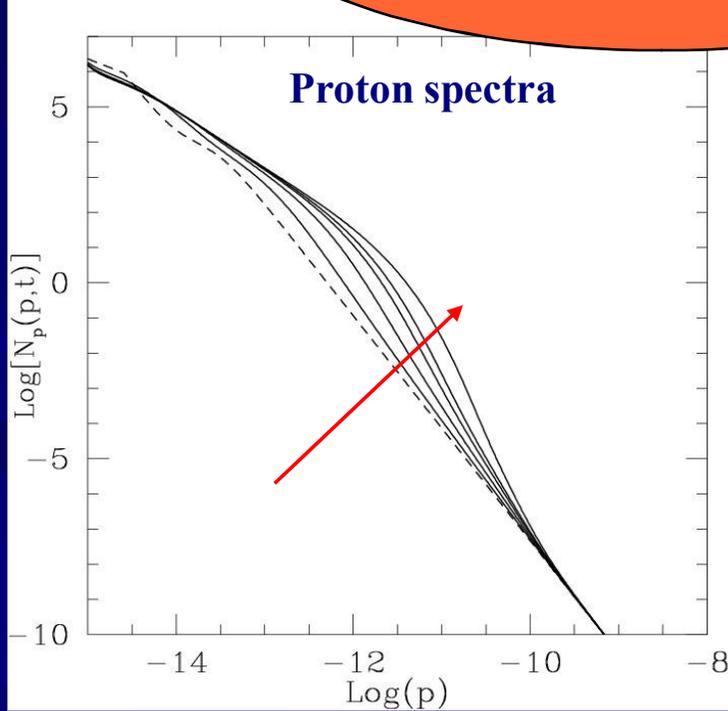


# Full Alfven-Wave--Particle Coupling

(Brunetti +al. 2004; Brunetti & Blasi 2005)



CR protons got 90% of the energy flux of the Alfven waves



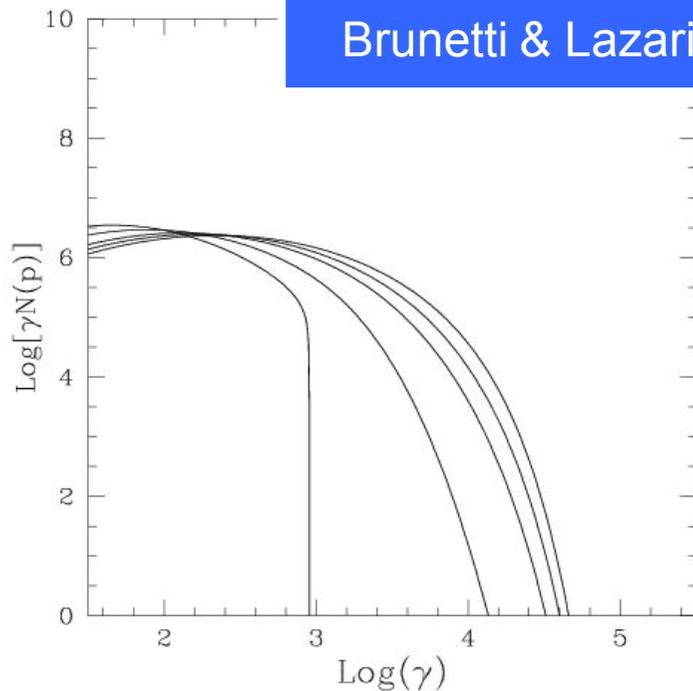
Waves + electrons + Protons

# Stochastic Particle Acceleration (formalism)

$$\frac{\partial N_c(p, t)}{\partial t} = \frac{\partial}{\partial p} \left( N_c(p, t) \left[ \left( \frac{dp}{dt} \right)_{\text{rad}} + \left( \frac{dp}{dt} \right)_i - \frac{2}{p} D_{pp} \right] \right) + \frac{\partial}{\partial p} \left( D_{pp} \frac{\partial N_c(p, t)}{\partial p} \right)$$

$$\frac{\partial \mathcal{W}(k, t)}{\partial t} = \frac{\partial}{\partial k} \left( k^2 D_{kk} \frac{\partial}{\partial k} \left( \frac{\mathcal{W}(k, t)}{k^2} \right) \right) - \sum_i \Gamma_i(k, t) \mathcal{W}(k, t) + I(k, t)$$

Brunetti & Lazarian 2007



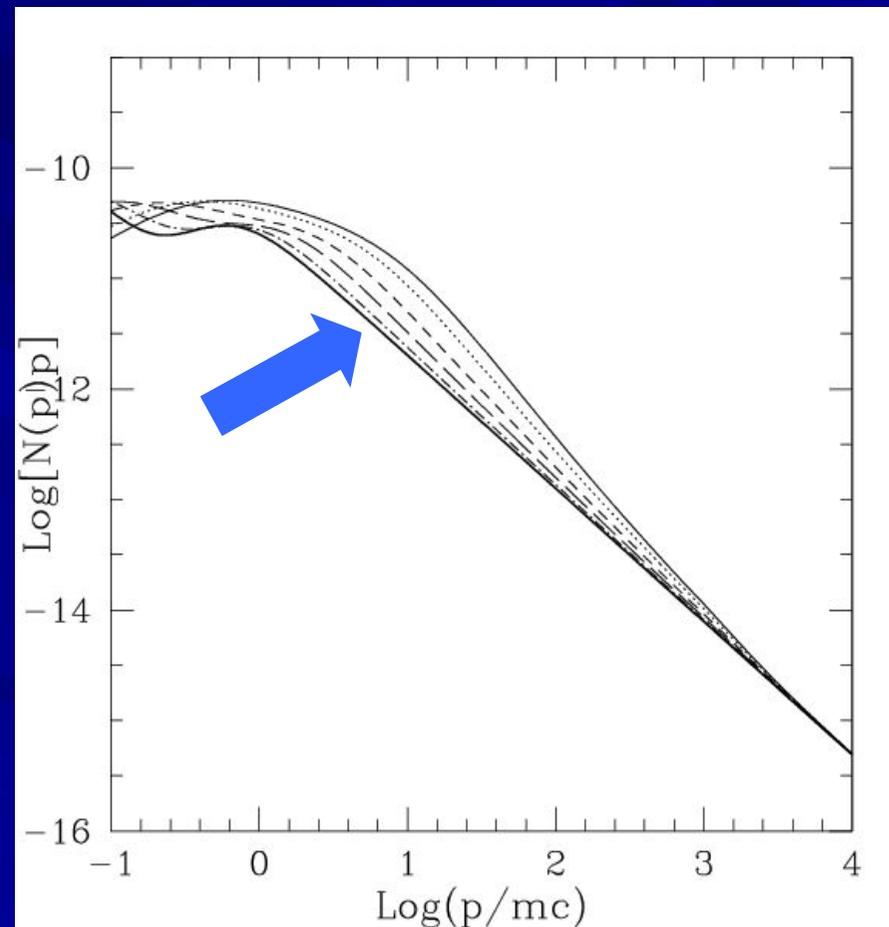
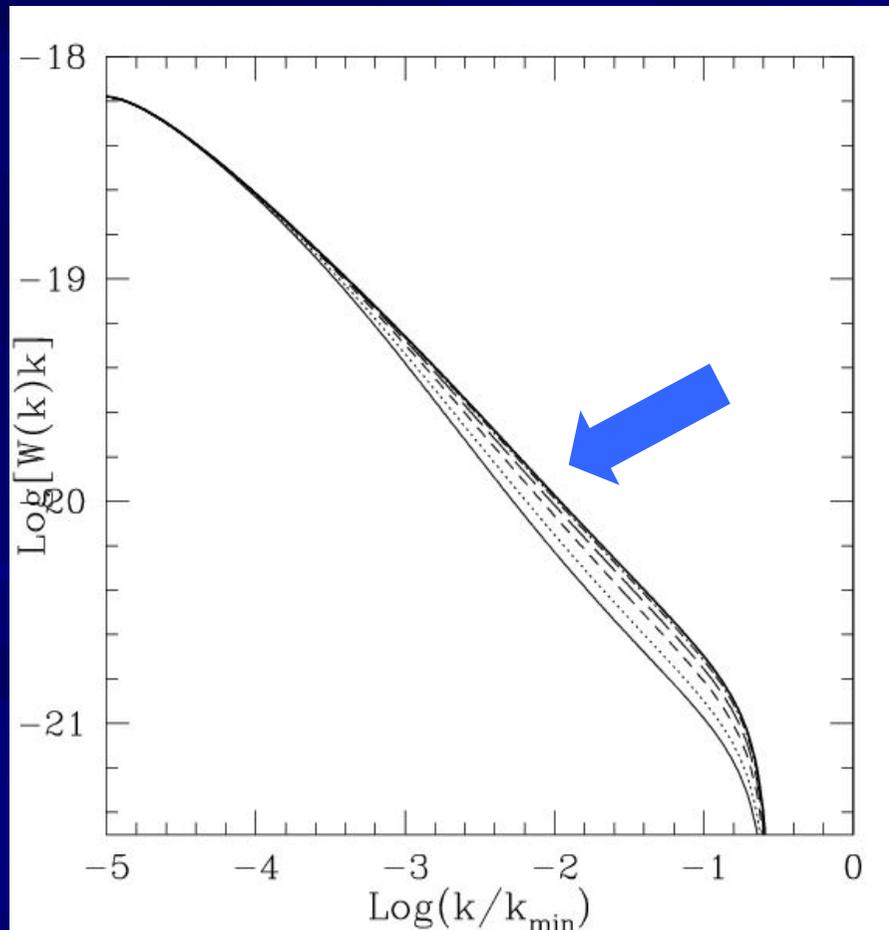
with thermal particles

# Alfvenic: results

$n_{th}, T, B_0, N_p(p,0), I(k)$



$N_p(p,t), N_{e\pm}(p,t), W(k,t), Q_{e\pm}(p,t), Q_{\pi}(p,t)$

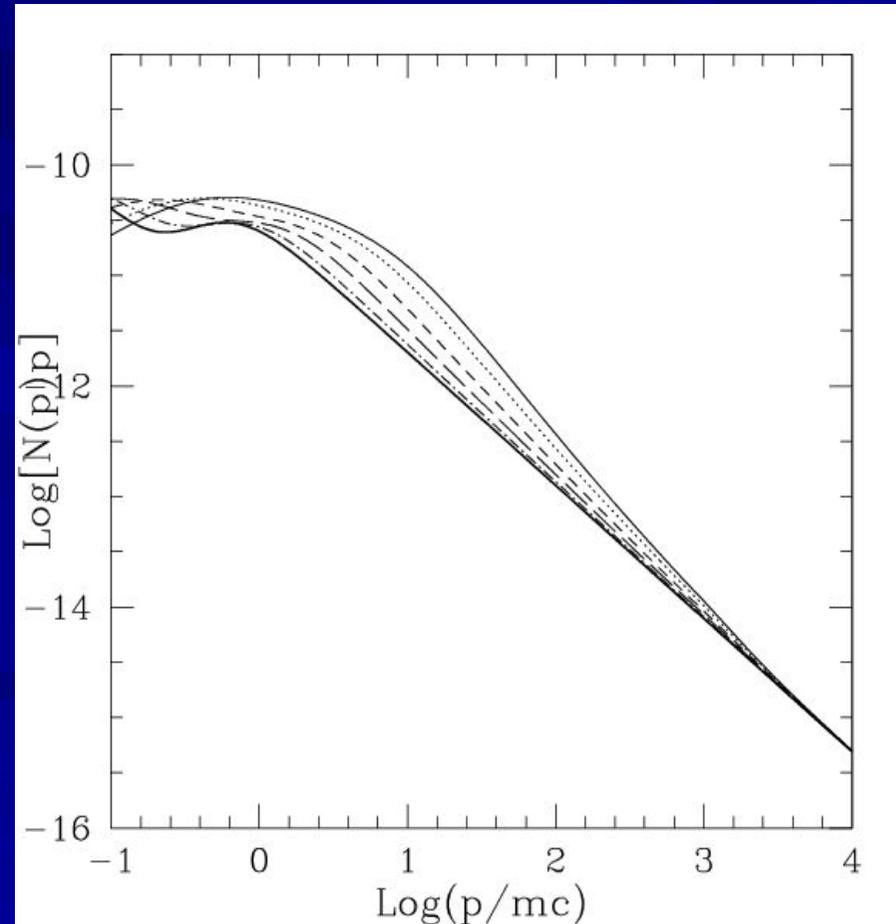
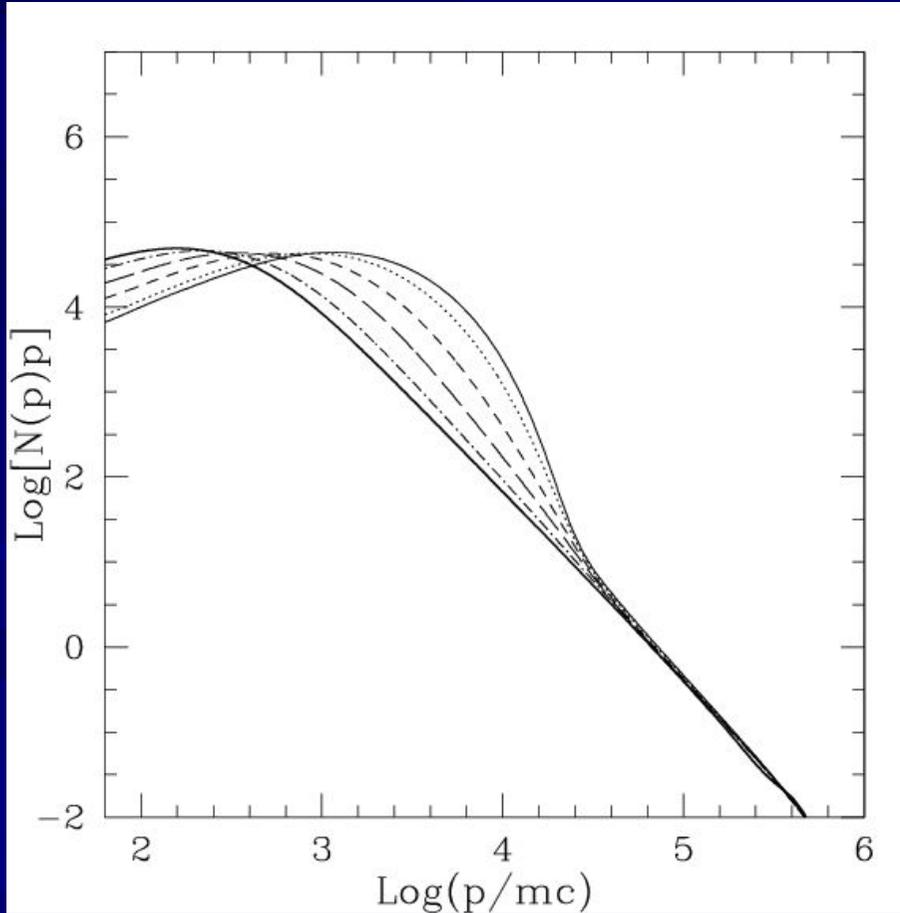


# Alfvenic: results

$n_{th}, T, B_0, N_p(p,0), I(k)$



$N_p(p,t), N_{e\pm}(p,t), W(k,t), Q_{e\pm}(p,t), Q_{\pi}(p,t)$

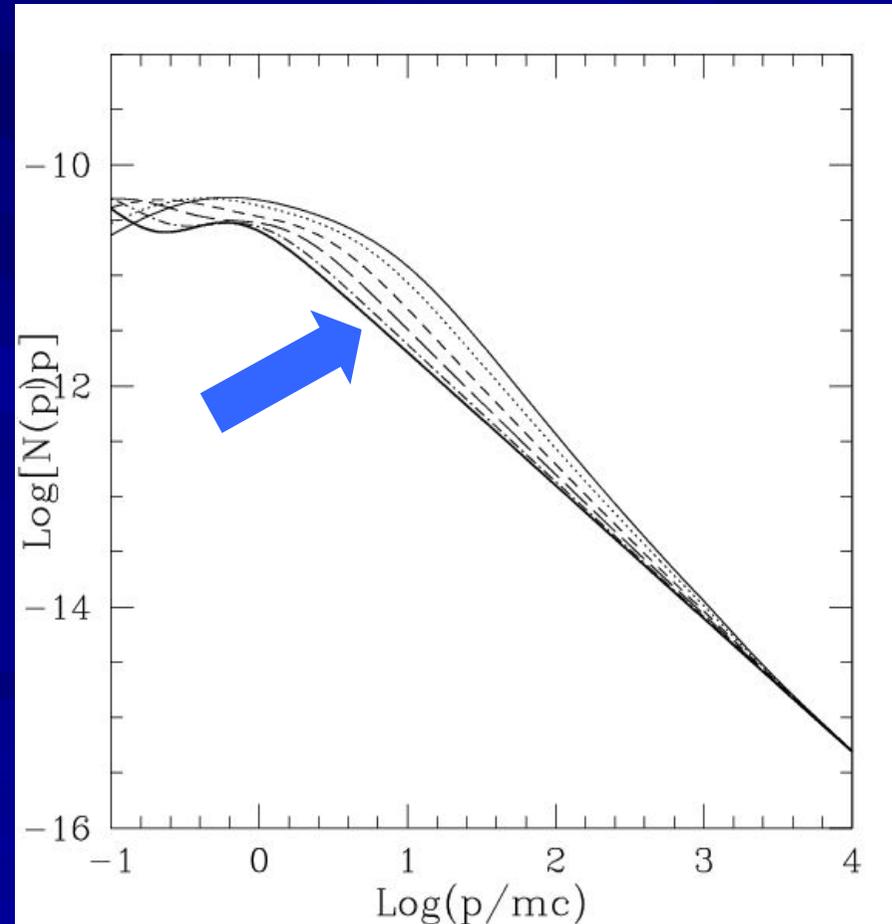
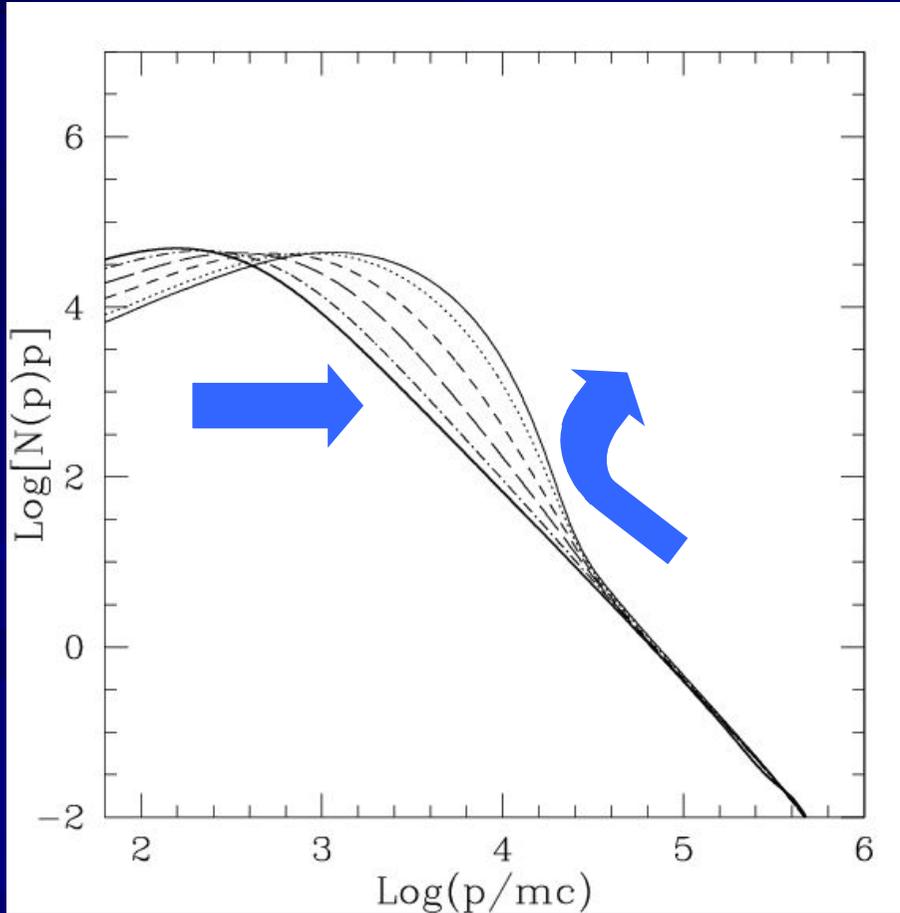


# Alfvenic: results

$n_{th}, T, B_0, N_p(p,0), I(k)$



$N_p(p,t), N_{e\pm}(p,t), W(k,t), Q_{e\pm}(p,t), Q_{\pi}(p,t)$

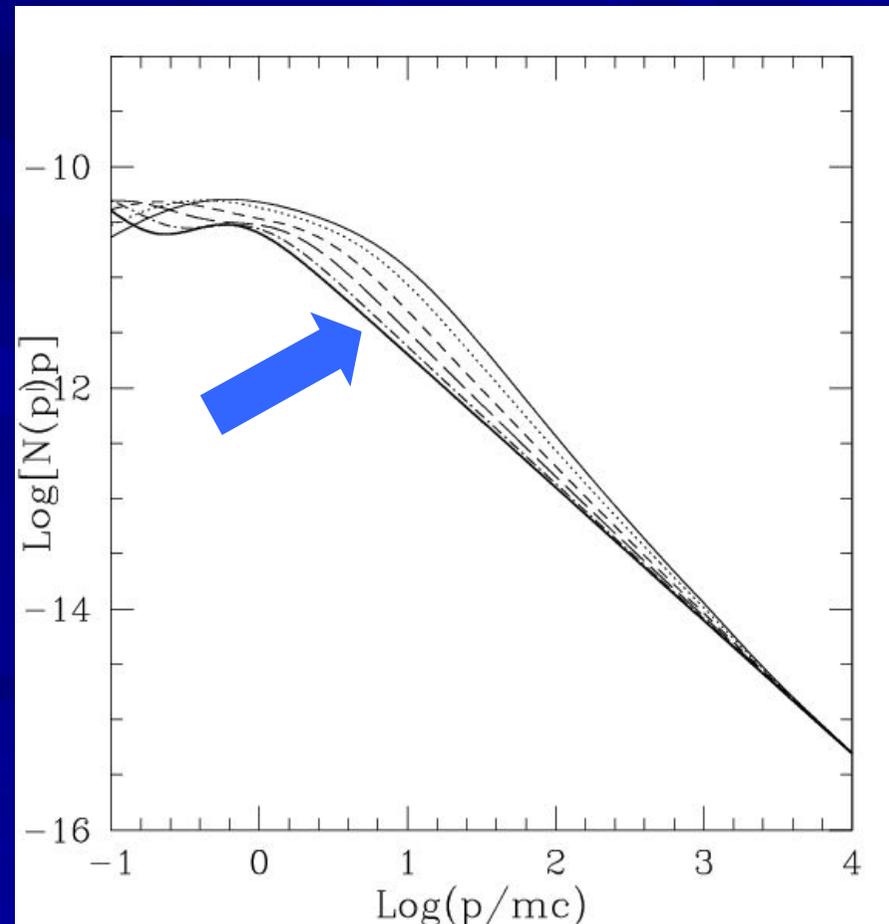
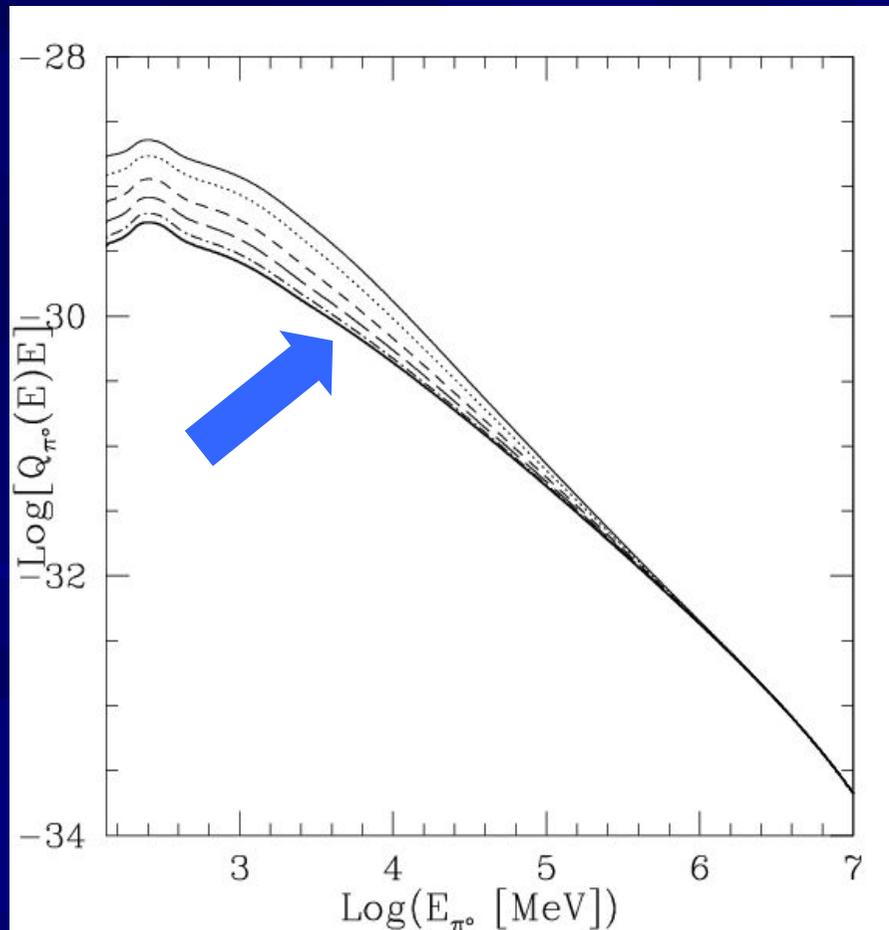


# Alfvenic: results

$n_{th}, T, B_0, N_p(p,0), I(k)$



$N_p(p,t), N_{e\pm}(p,t), W(k,t), Q_{e\pm}(p,t), Q_{\pi}(p,t)$



# Dissipation of turbulence in the ICM (quasi-linear theory)

Brunetti & Lazarian 2007

- TTD Resonant acceleration

$$\omega - k_{\parallel} v_{\parallel} - n \frac{\Omega_o}{\gamma} = 0 \quad n = 0$$

(provided there is an additional source of pitch angle scattering)

Damping-rate

Energy changing-rate

$$\Gamma = -i \left( \frac{E_i^* K_{ij}^a E_j}{16\pi W} \right)_{\omega_i=0} \omega_r$$



$$\int d^3 p E_{\alpha} \left( \frac{\partial f_{\alpha}(p)}{\partial t} \right) = \int dk \Gamma^{\alpha}(k, \theta) \mathcal{W}(k)$$

Energy damping-rate



Diffusion coeff. In momentum space

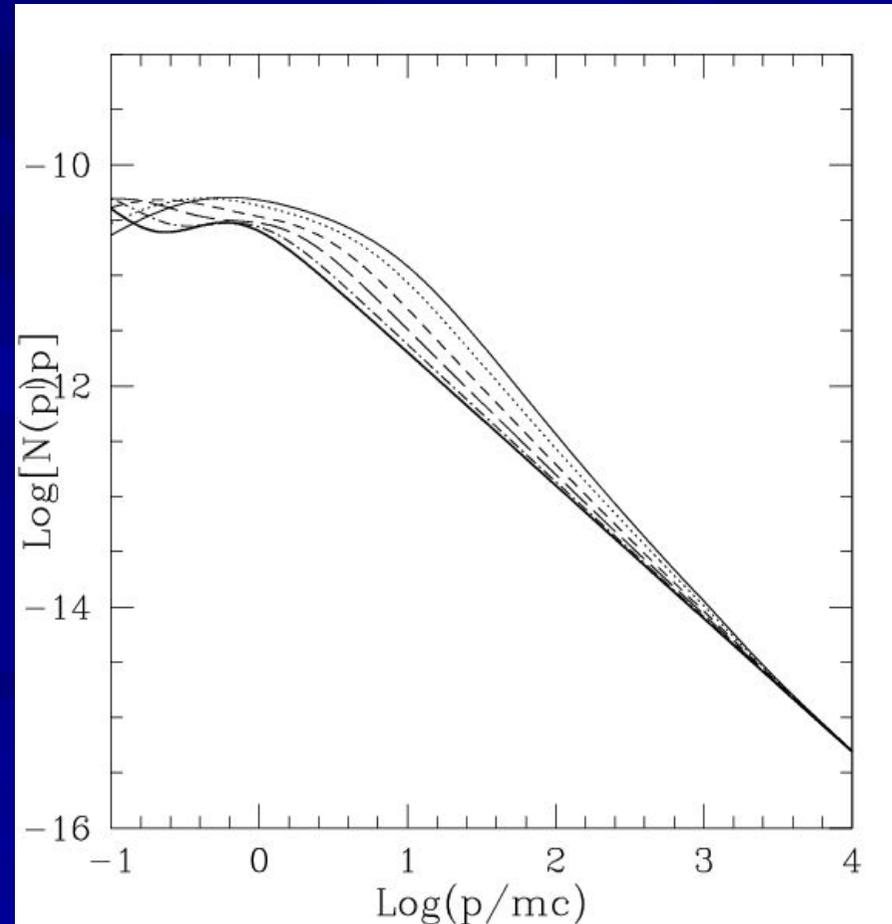
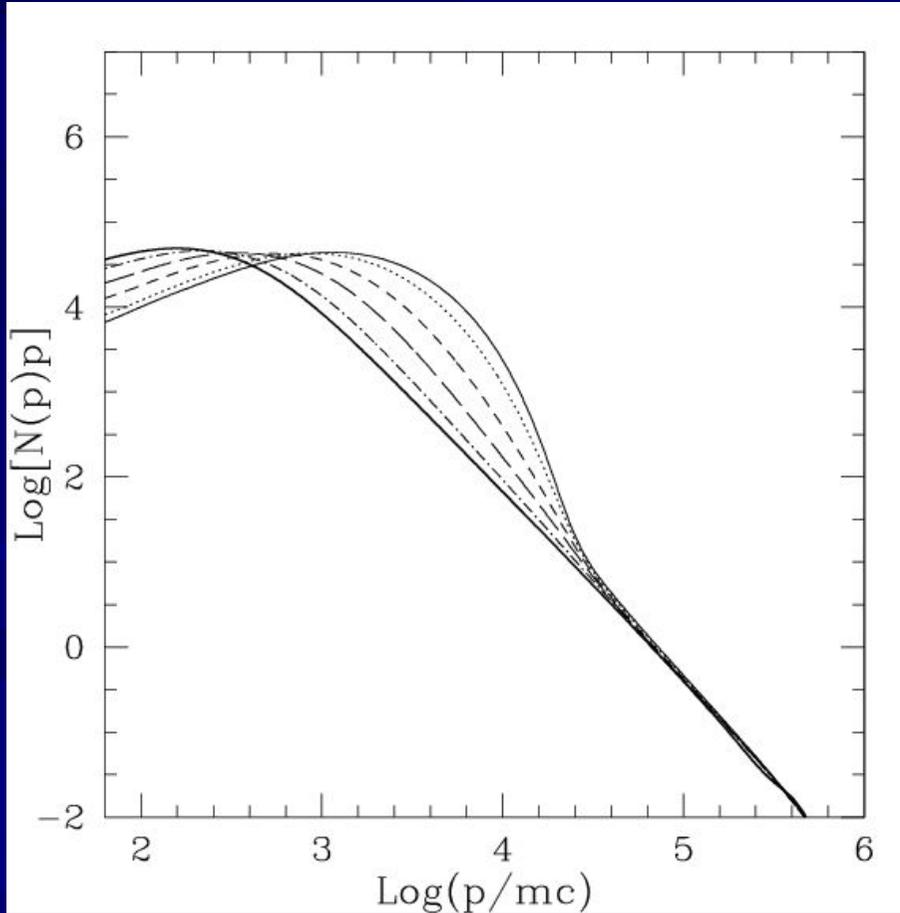
$$D_{pp}(p) = \frac{\pi^2}{2c} p^2 \frac{1}{B_o^2} \int_0^{\pi/2} d\theta V_{ph}^2 \frac{\sin^3(\theta)}{|\cos(\theta)|} \mathcal{H} \left( 1 - \frac{V_{ph}/c}{\cos \theta} \right) \left( 1 - \left( \frac{V_{ph}/c}{\cos \theta} \right)^2 \right)^2 \int dk \mathcal{W}_B(k) k$$

# Alfvenic: results

$n_{th}, T, B_o, N_p(p,0), N_e(p,0), I(k)$



$N_p(p,t), N_{e\pm}(p,t), W(k,t), Q_{e\pm}(p,t), Q_{\pi}(p,t)$

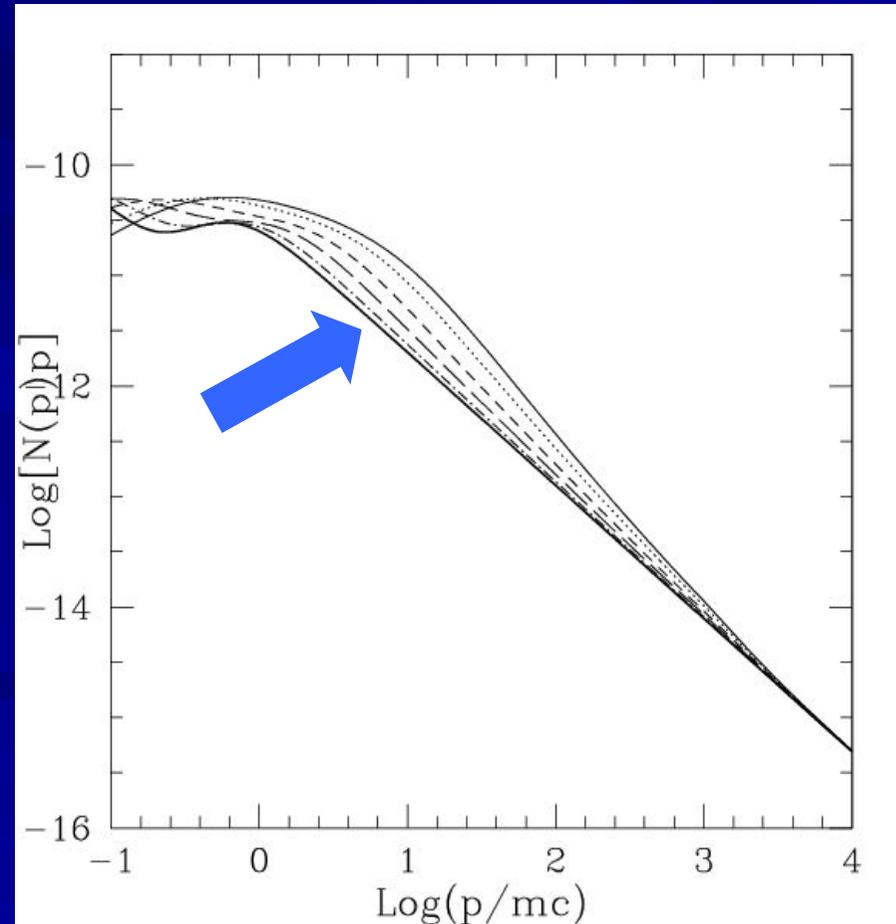
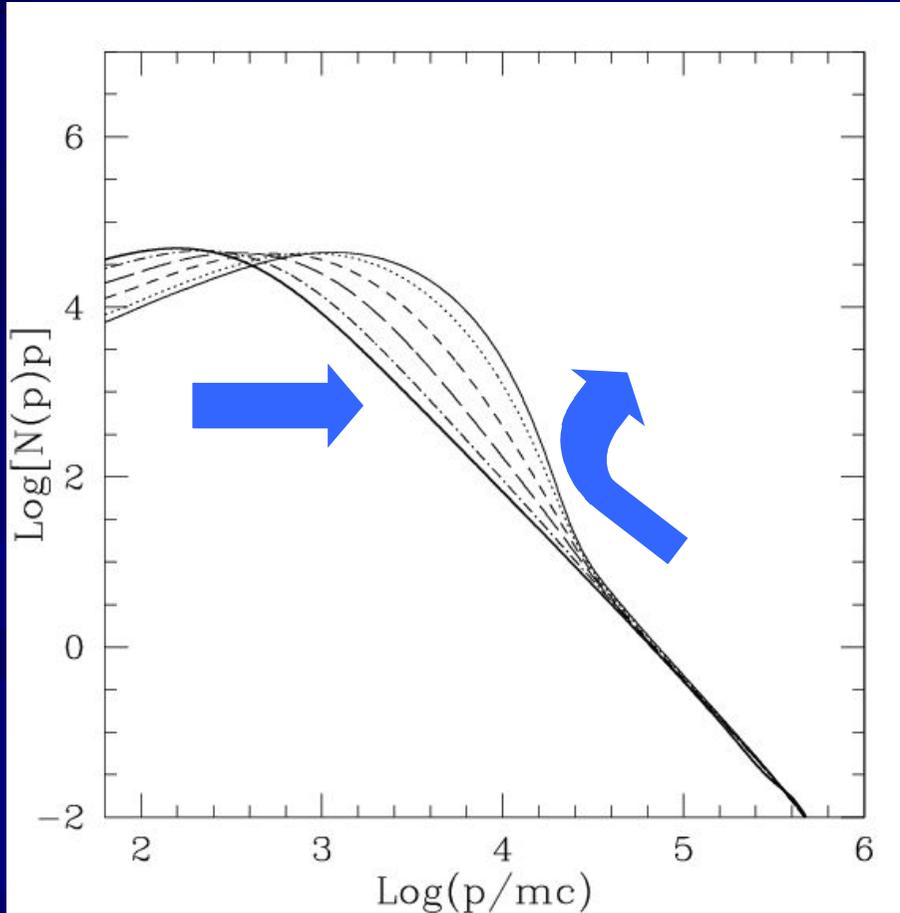


# Alfvenic: results

$n_{th}, T, B_o, N_p(p,0), N_e(p,0), I(k)$



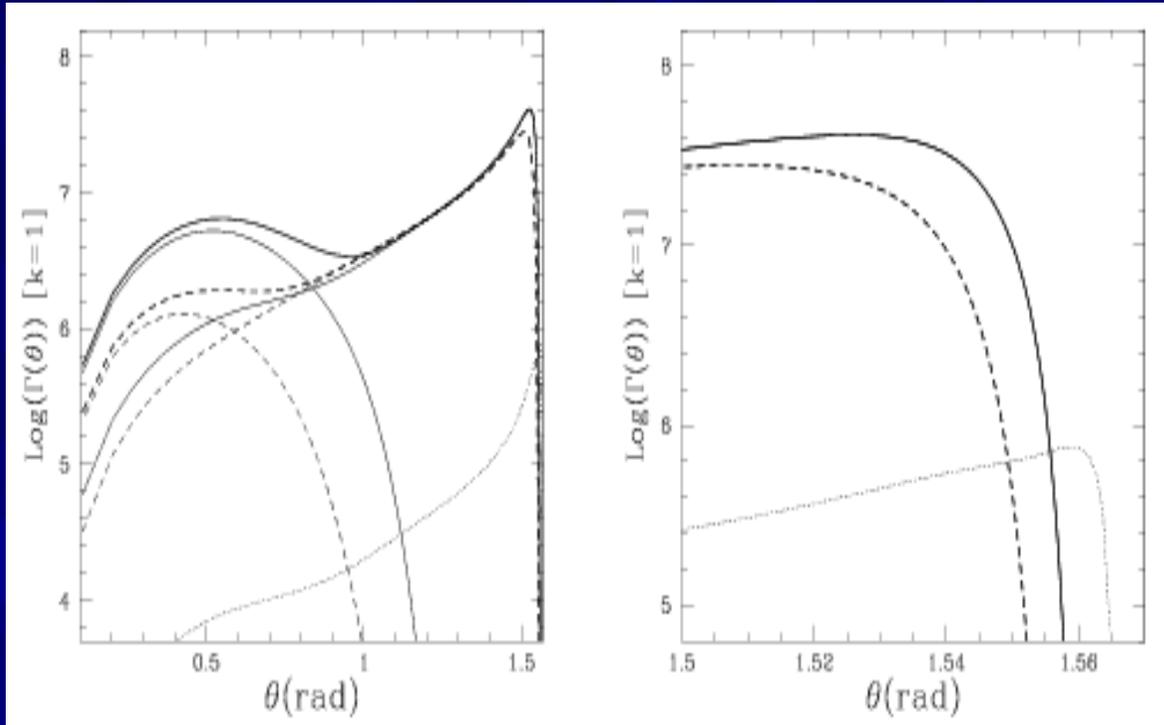
$N_p(p,t), N_{e\pm}(p,t), W(k,t), Q_{e\pm}(p,t), Q_{\pi}(p,t)$





# Dissipation of turbulence in the ICM (quasi-linear theory)

$$\Gamma = -i \left( \frac{E_i^* K_{ij}^a E_j}{16\pi W} \right)_{\omega_i=0} \omega_r$$



*Line-bending efficiency*  $\gg$  *damping efficiency*

$$\tau_{bb}(\mathbf{k})^{-1} \sim V_{1A} / l_A \quad \tau_d^{-1} = \Gamma(\mathbf{k})$$

*Isotropic Effective Damping*

$$l_{diss} \approx 100 \text{ pc}$$

# Dissipation of turbulence in the ICM (Hydro-turbulence)

Dissipation cut-off develops at  
scale :

$$\tau_{kk}(l) \geq \tau_{vis}(l) = l^2/\nu_K$$

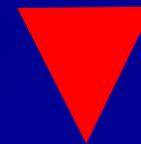
$$\nu_K \sim \frac{1}{3}v_i \times \min \{l_A, l_{mfp}\}$$

(e.g., Lazarian 2006)

$$Re = \frac{V_o L_o}{\nu_K} > 10^3$$



$$l_{diss} \sim L_o (Re)^{-\frac{3}{4}} < l_{mfp}$$

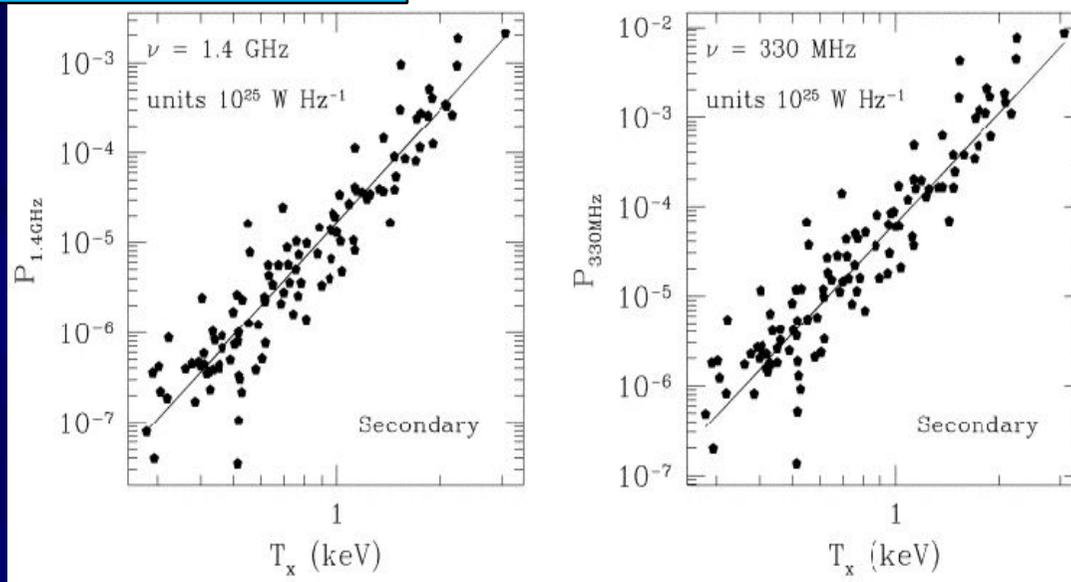


Collisionless dissipation !

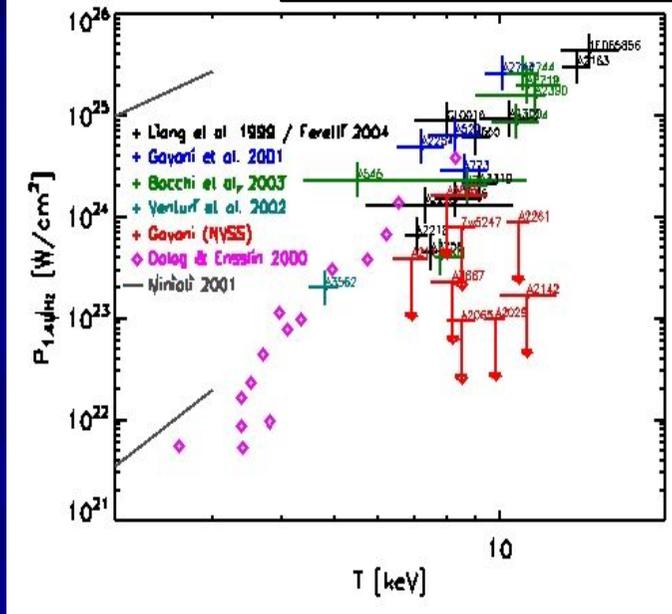
# Statistical properties of RH

Miniati et al. 2001

Synchrotron Power



Dolag 2005

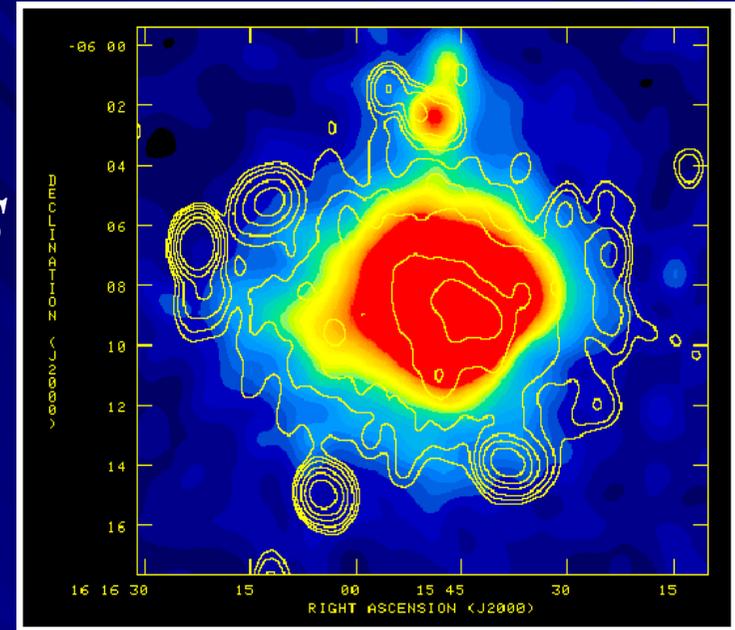


In case electrons are secondaries :

➤ RH are not transient phenomena

➤ GC with similar thermal properties have similar radio properties

# *Diffuse Radio Emission & origin of emitting electrons*



Aims:

- Statistical properties of RH
- Spectral studies of RH
- Connection with mergers

# Stochastic Particle Acceleration (formalism)

Brunetti +al. 2004, Brunetti & Blasi 2005, Brunetti +al. In prep

## Electrons/Positrons

$$\frac{\partial N_e(p, t)}{\partial t} = \frac{\partial}{\partial p} \left( N_e(p, t) \left[ \left( \frac{dp}{dt} \right)_{\text{rad}} + \left( \frac{dp}{dt} \right)_i - \frac{2}{p} D_{pp} \right] \right) + \frac{\partial}{\partial p} \left( D_{pp} \frac{\partial N_e(p, t)}{\partial p} \right) + Q_e(p, t)$$

## Protons

$$\frac{\partial N_p(p, t)}{\partial t} = \frac{\partial}{\partial p} \left( N_p(p, t) \left[ \left( \frac{dp}{dt} \right)_i - \frac{2}{p} D_{pp} \right] \right) + \frac{\partial}{\partial p} \left( D_{pp} \frac{\partial N_p(p, t)}{\partial p} \right) + Q_p(p, t)$$

$Q_e$ : secondaries from (CR)p-p collisions

## Waves

$$\frac{\partial \mathcal{W}(k, t)}{\partial t} = \frac{\partial}{\partial k} \left( k^2 D_{kk} \frac{\partial}{\partial k} \left( \frac{\mathcal{W}(k, t)}{k^2} \right) \right) - \sum_i \Gamma_i(k, t) \mathcal{W}(k, t) + I(k, t)$$

most could be with CR protons

# Stochastic particle RE- acceleration

- Stochastic turbulent compression (e.g. Ptuskin 1988)

(provided  $l \gg l_{mfp}$  &  $V_l^2 \ll c_s^2$ )

$$D_{pp} \simeq \frac{2}{9} D p^2 \frac{V_o^2}{L_o^{2/3}} \int_{1/L_o}^{1/l_{cut}} \frac{dy y^{1/3}}{c_s^2 + D^2 y^2}$$

With

$$D \sim \frac{c}{3} \max \left\{ l_{cut}, \min \{ l_A, l_{mfp} \} \right\}$$

Also ...  
efficient source of  
particle pitch-angle  
isotropization

# Dissipation of turbulence in the ICM (quasi-linear theory)

$$\omega - k_{\parallel} v_{\parallel} - n \frac{\Omega_o}{\gamma} = 0$$

Small scale  $n = +/-1, +/-2, +/-3, \dots$   
 Large scale  $n = 0$

**Transit-Time-Damping  $n = 0$**  (e.g. Schlickeiser & Miller 1998)

$$\omega = k_{\parallel} v_{\parallel}$$

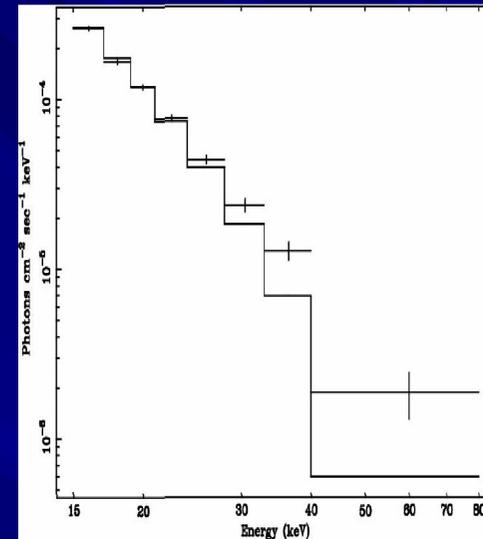
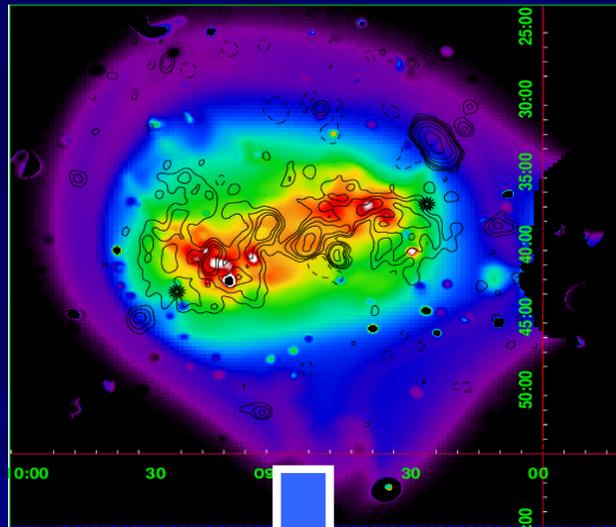
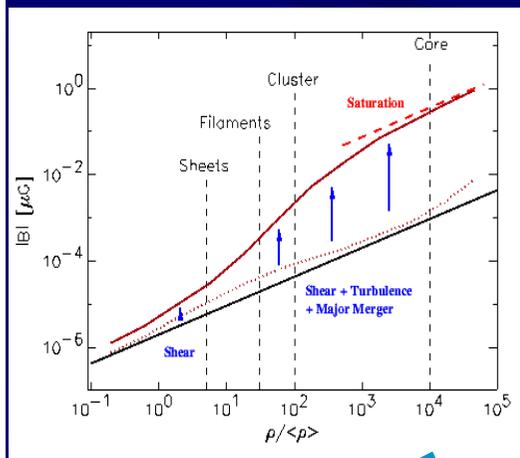
&

$$V_{\text{ph}}^2 = \frac{c_s^2}{2} \frac{\beta_{pl} + 1}{\beta_{pl}} \left\{ 1 + \sqrt{1 - 4 \left( \frac{k_{\parallel}}{k} \right)^2 \frac{\beta_{pl}}{(1 + \beta_{pl})^2}} \right\}$$

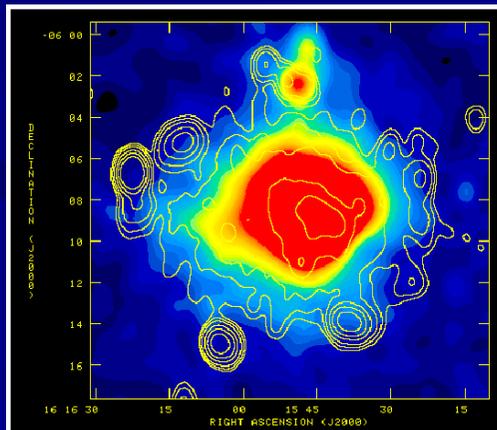
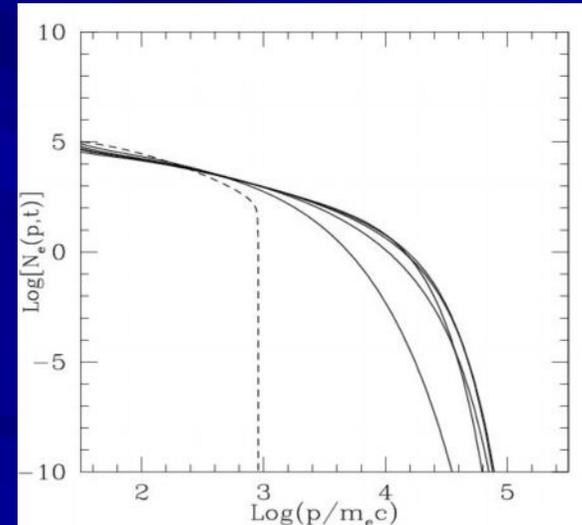
# Fermi II RE-Acceleration Models

(Brunetti et al. 2001, Petrosian 2001, ... ++ al.)

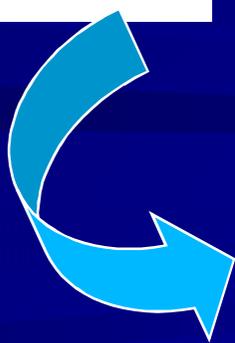
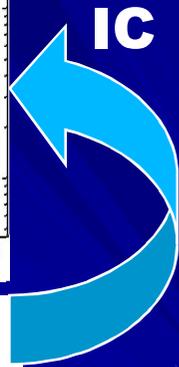
Dolag & Bruggen talks  
**MF Amplification**



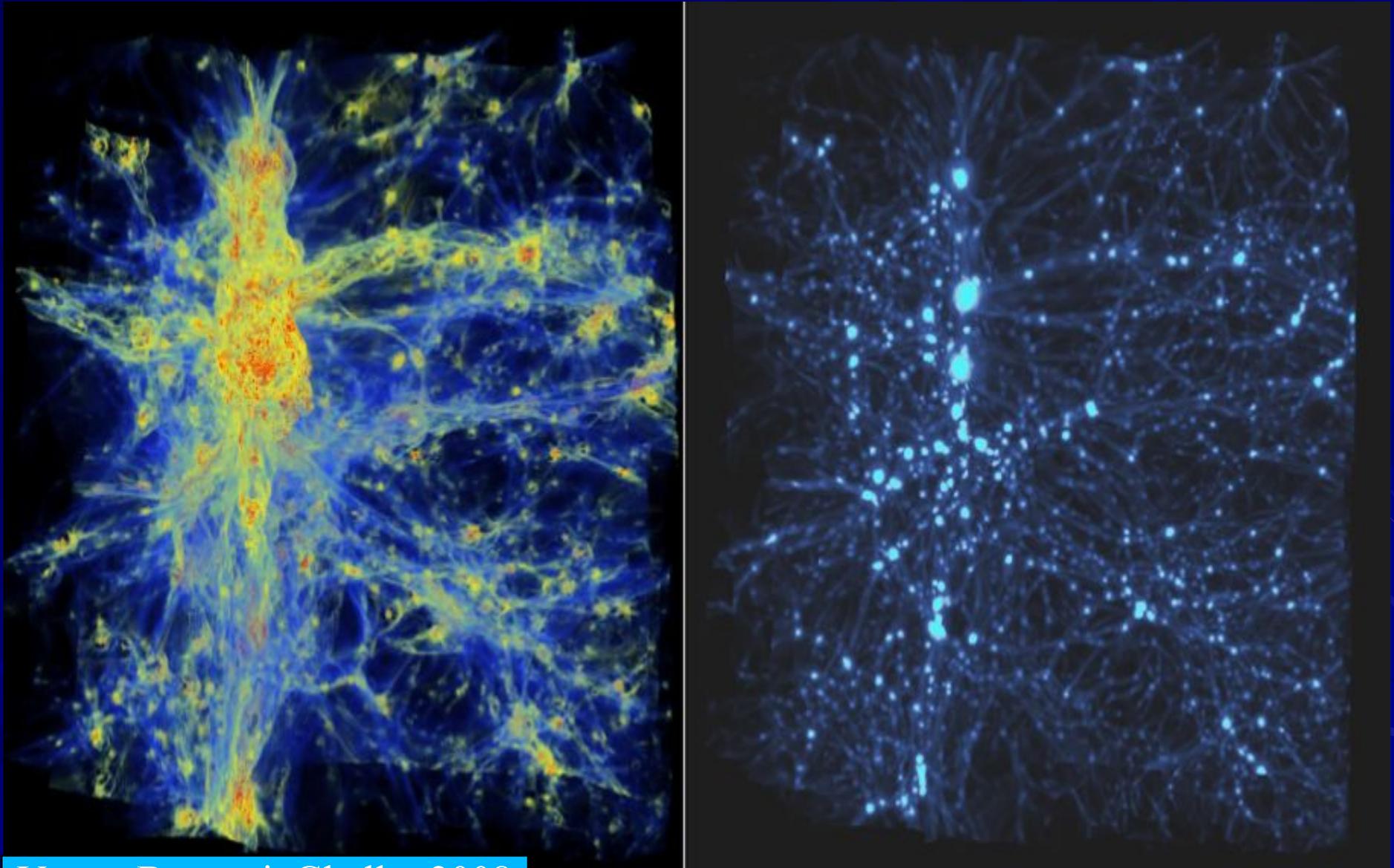
**Turbulence**



**Synchrotron**

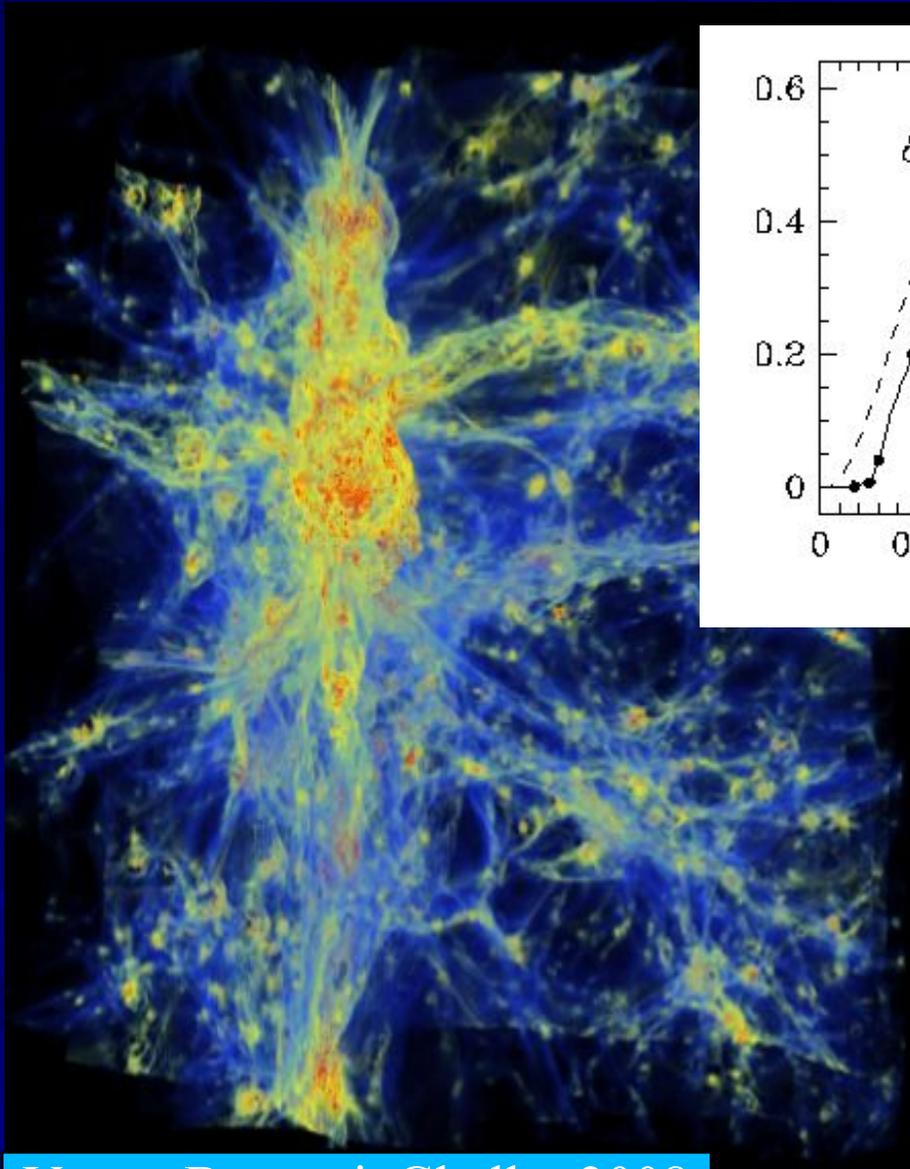


# Shocks in Galaxy Clusters

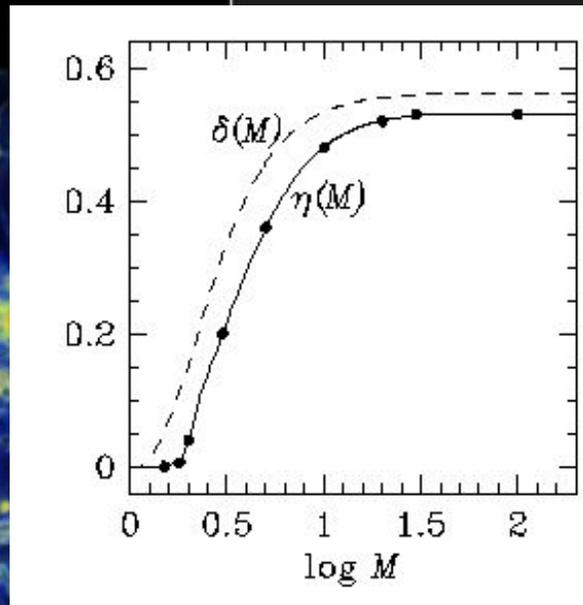


Vazza, Brunetti, Gheller 2008

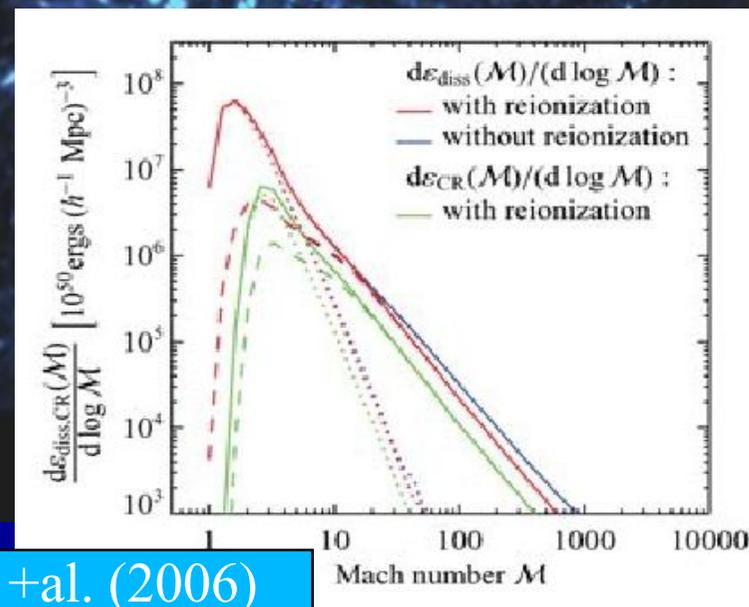
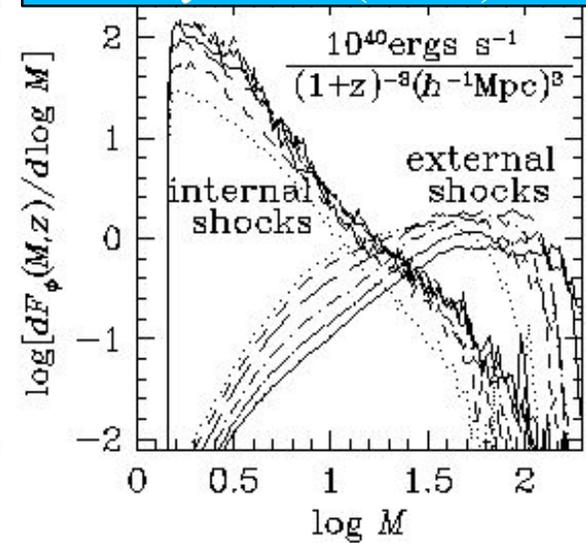
# Shocks in Galaxy Clusters



Vazza, Brunetti, Gheller 2008

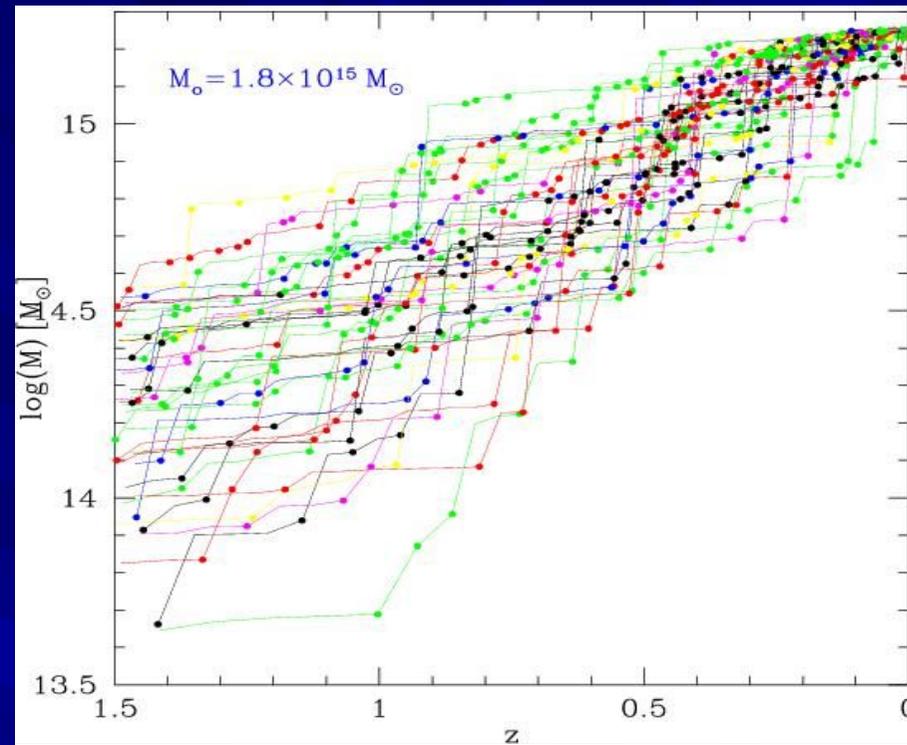
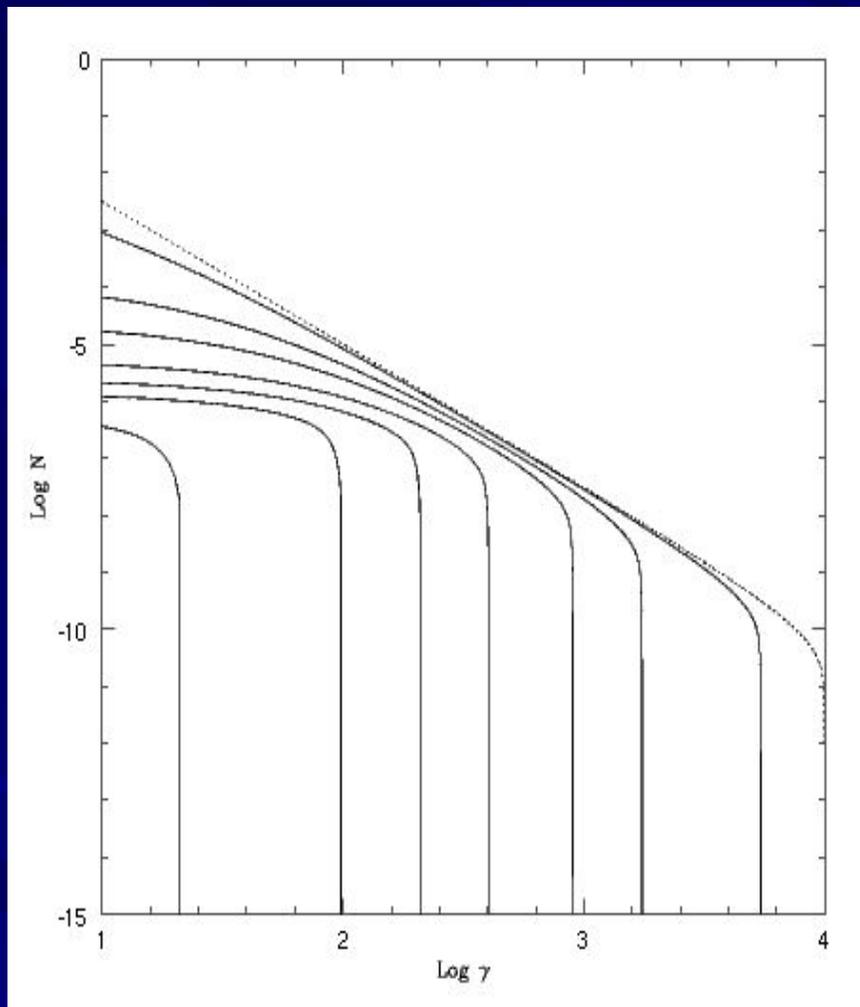


Ryu +al. (2003)

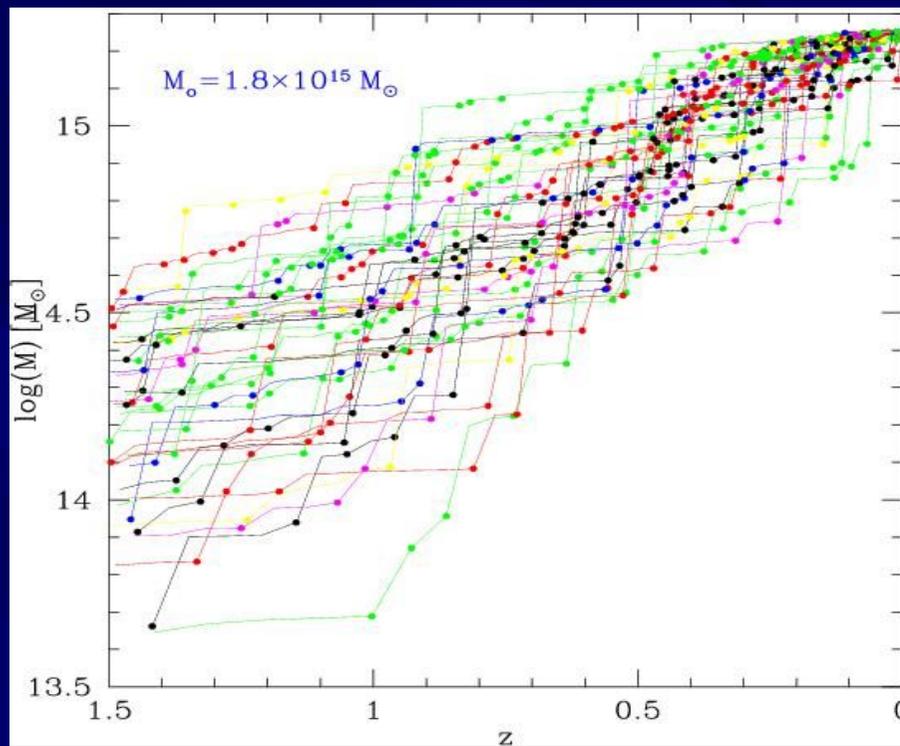


Pfrommer +al. (2006)

# CR Emission

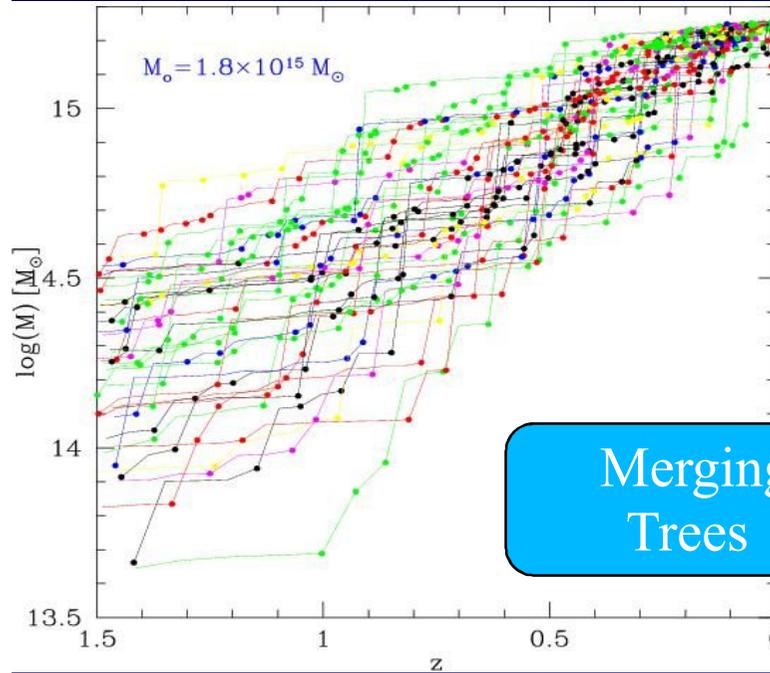


# CR Emission

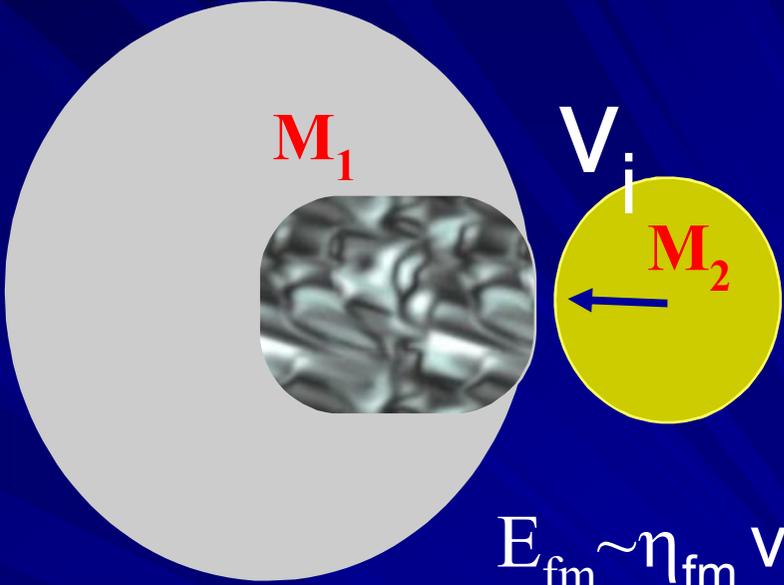


# HXR: Calculations

Cassano & Brunetti 2005; Cassano et al. 2006

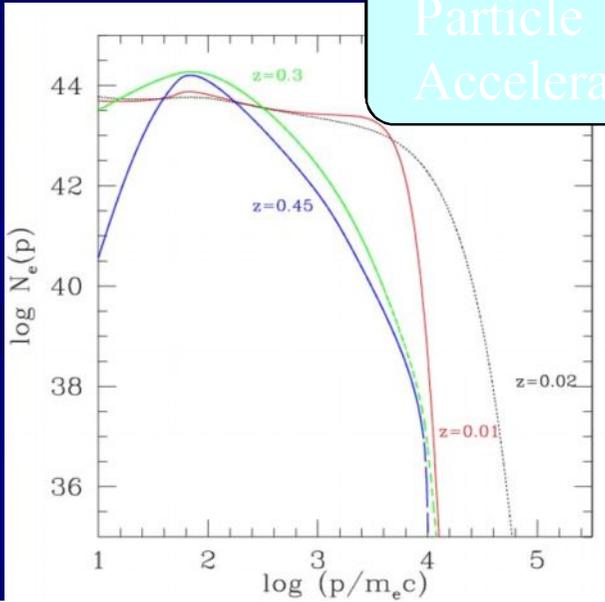


Merging Trees

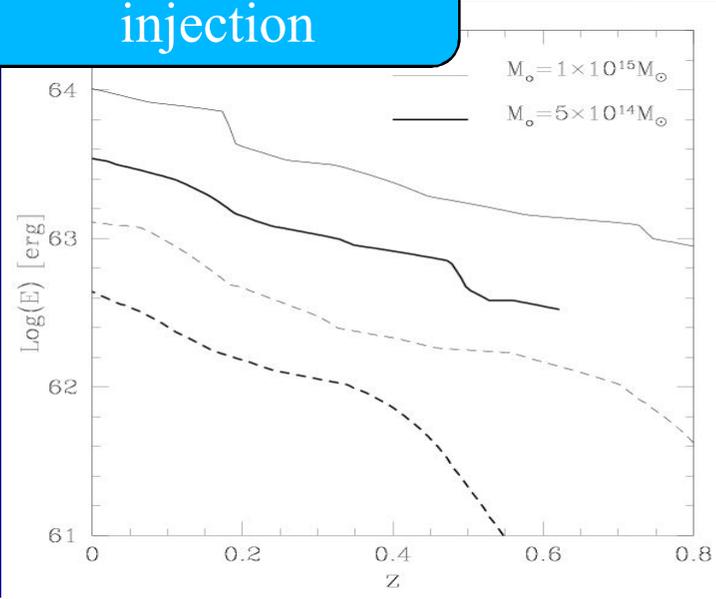


$$E_{fm} \sim \eta_{fm} v_i^2$$

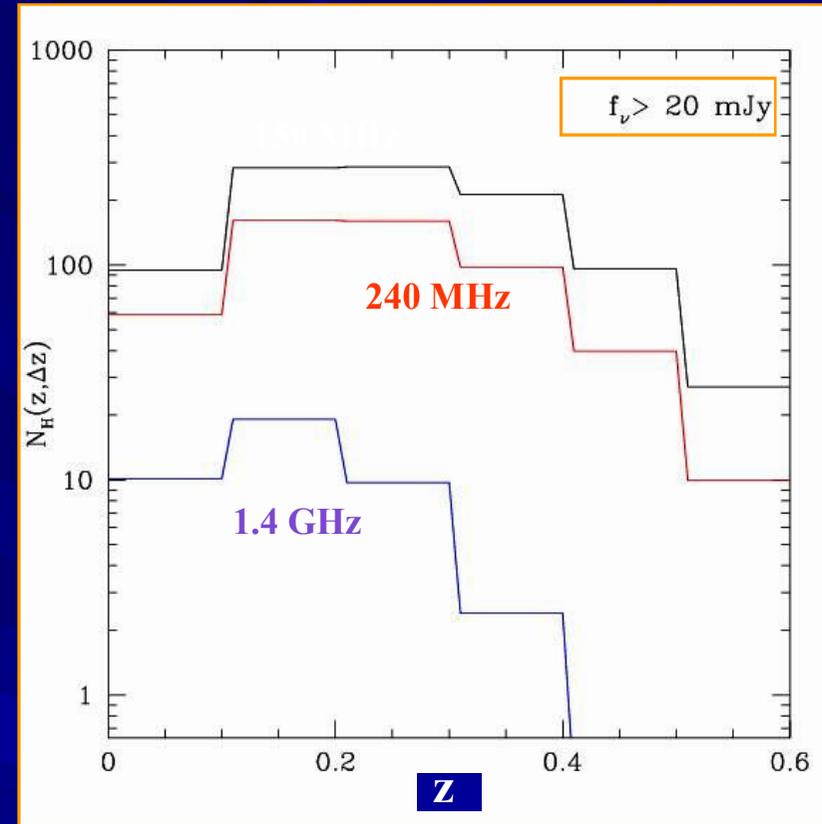
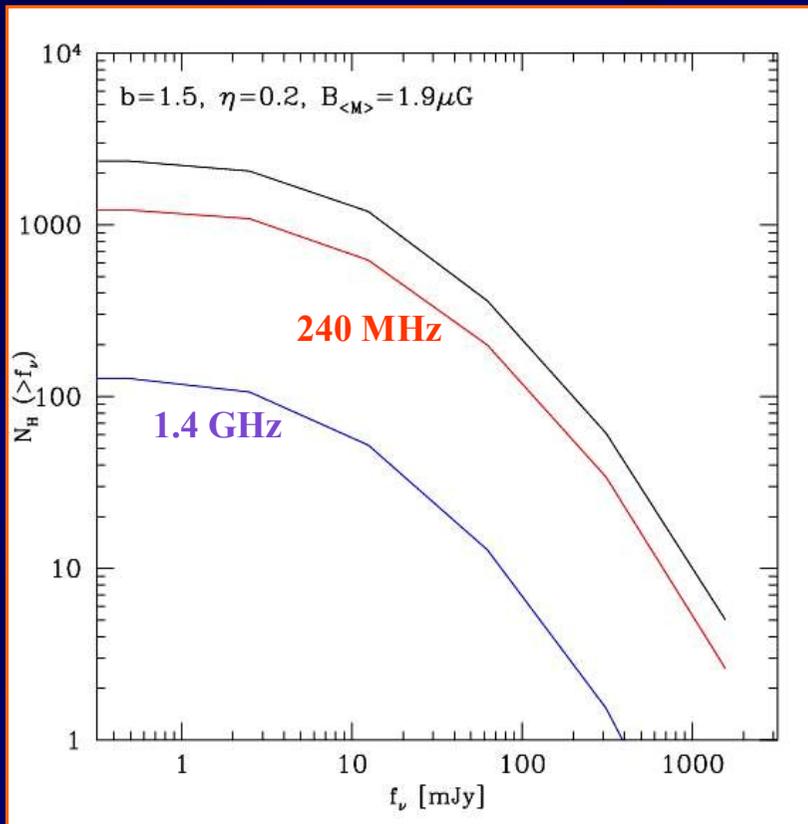
Turbulent injection



Particle Acceleration



# Number Counts of RHs at lower radio frequencies



The number of expected RHs increases at lower frequencies by about a factor 10!

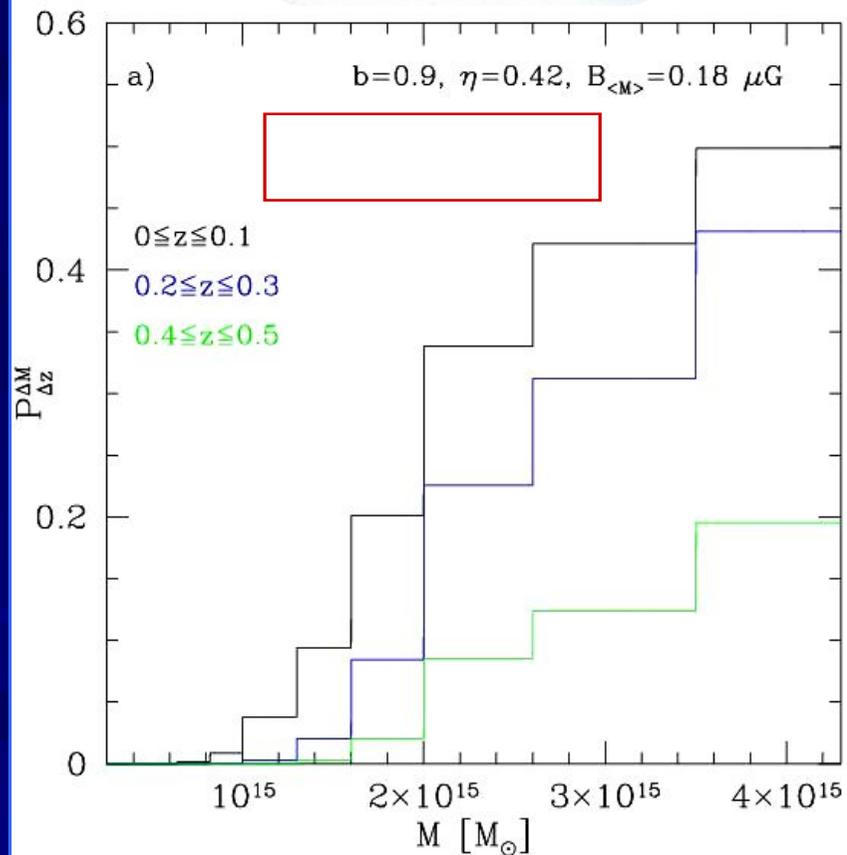
**LOFAR** should be able to catch the bulk of RHs!

The bulk of RHs emitting at **GHz frequencies** is expected at relatively low redshift: **0.1-0.3**.

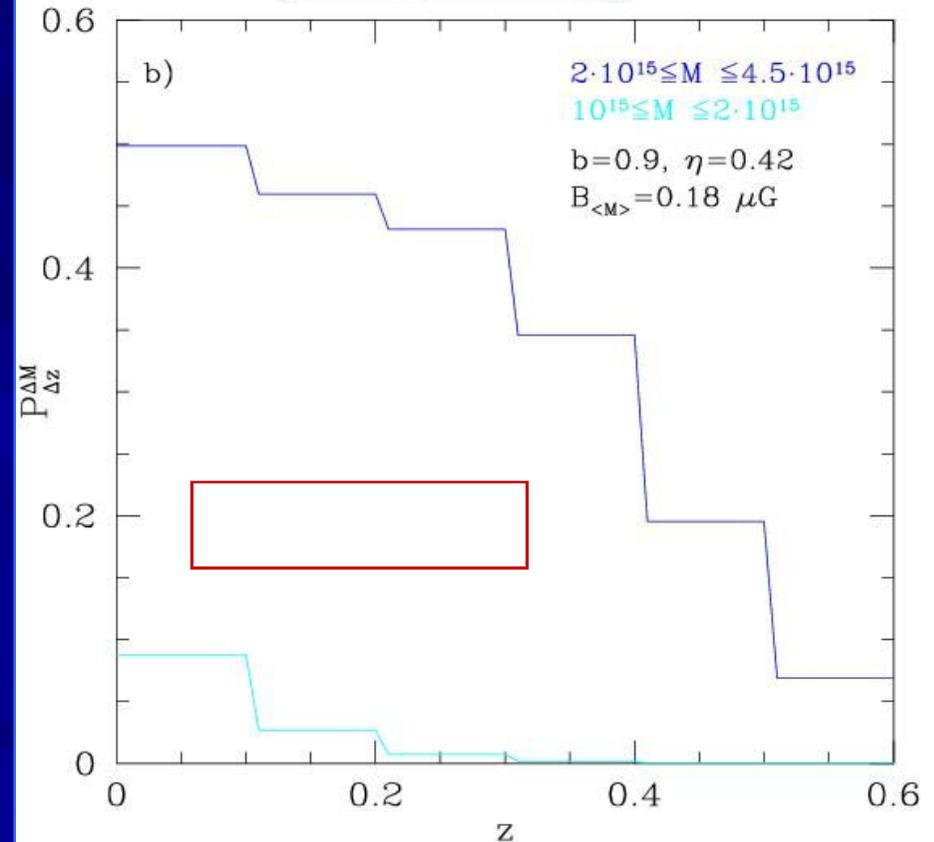
At **lower radio frequencies** a number of RHs is expected to be discovered at relatively higher redshifts  **$z > 0.4$** .

# Expected probabilities to form GRHs versus M & z

sub-linear  
scaling **b=0.9**



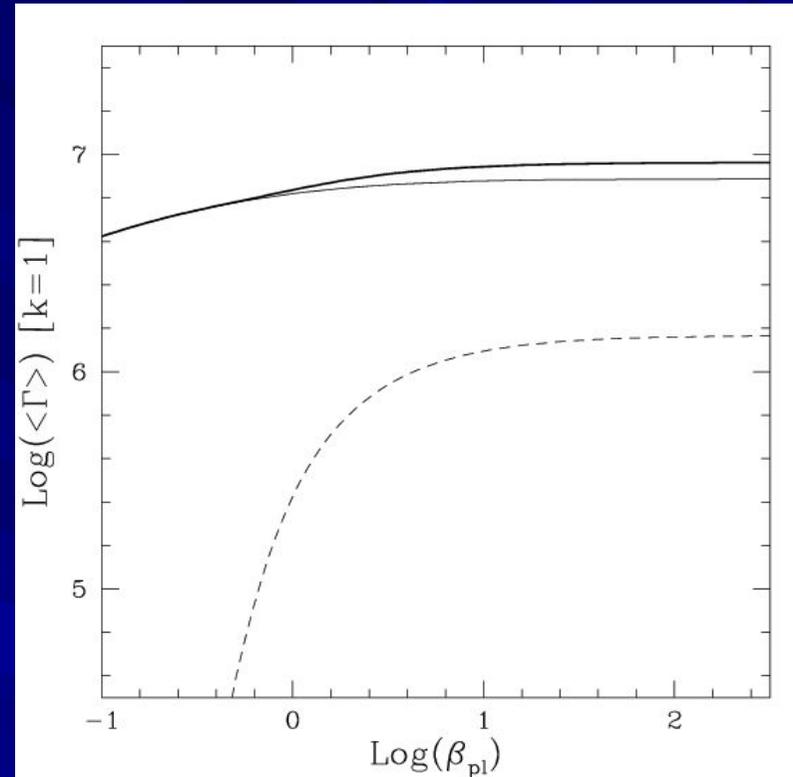
sub-linear  
scaling **b=0.9**



# Dissipation of turbulence in the ICM (quasi-linear theory)

(e.g., Melrose 1968; Barnes 1969;  
Barnes & Scargle 1973)

$$\Gamma = -i \left( \frac{E_i^* K_{ij}^a E_j}{16\pi W} \right)_{\omega_i=0} \omega_r$$



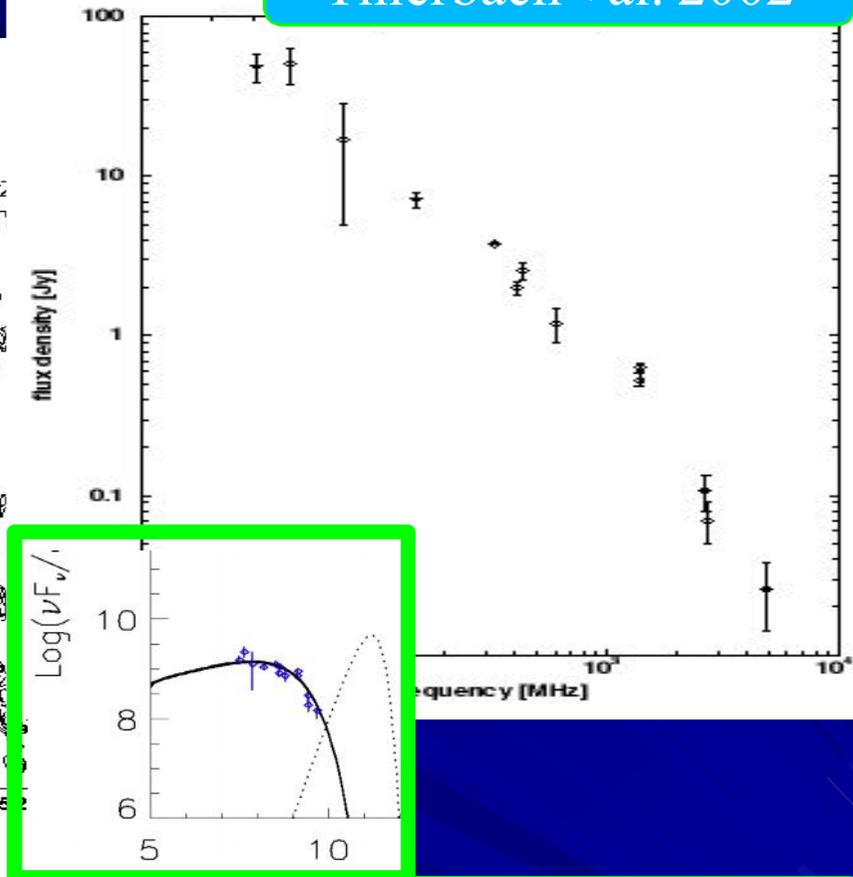
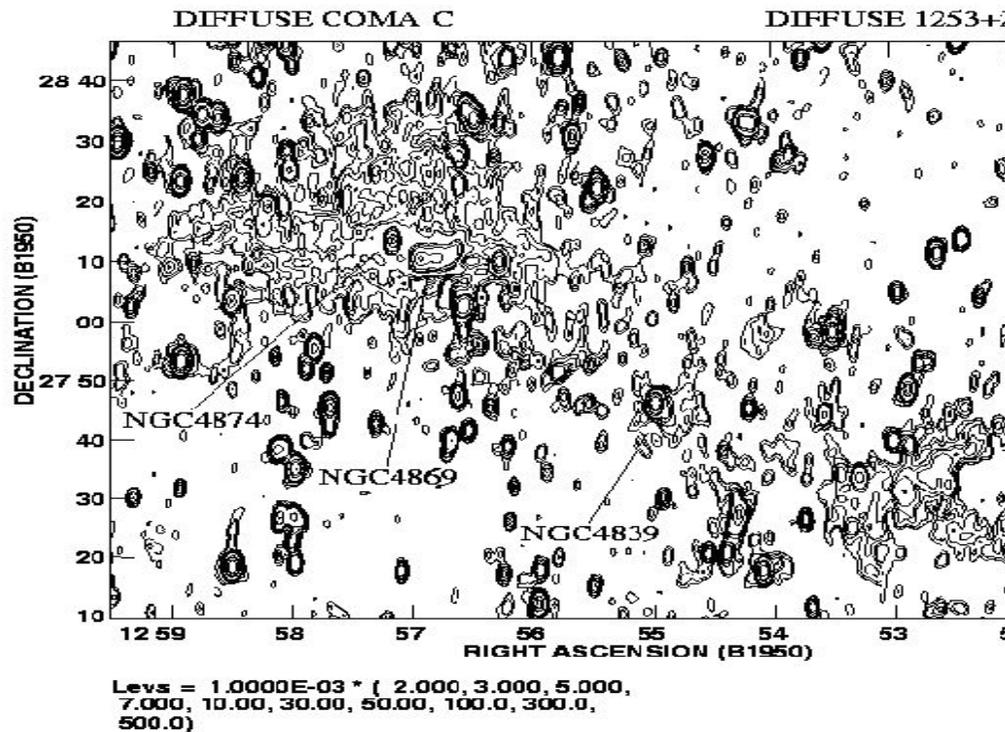
**L** Damping is dominated by thermal electrons since they are faster than the phase velocity of the modes. **CR are not important provided they are not a dominant component in the ICM**  
*Damping is simple !*

ency

(**k**)

Thierbach +al. 2002

# RADIO

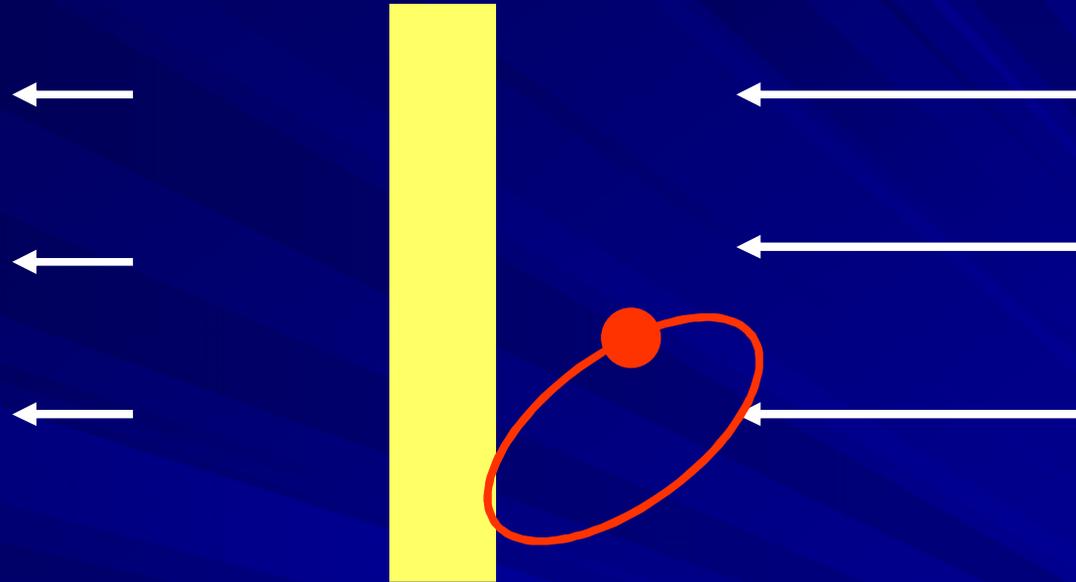


Reimer +al. 2004

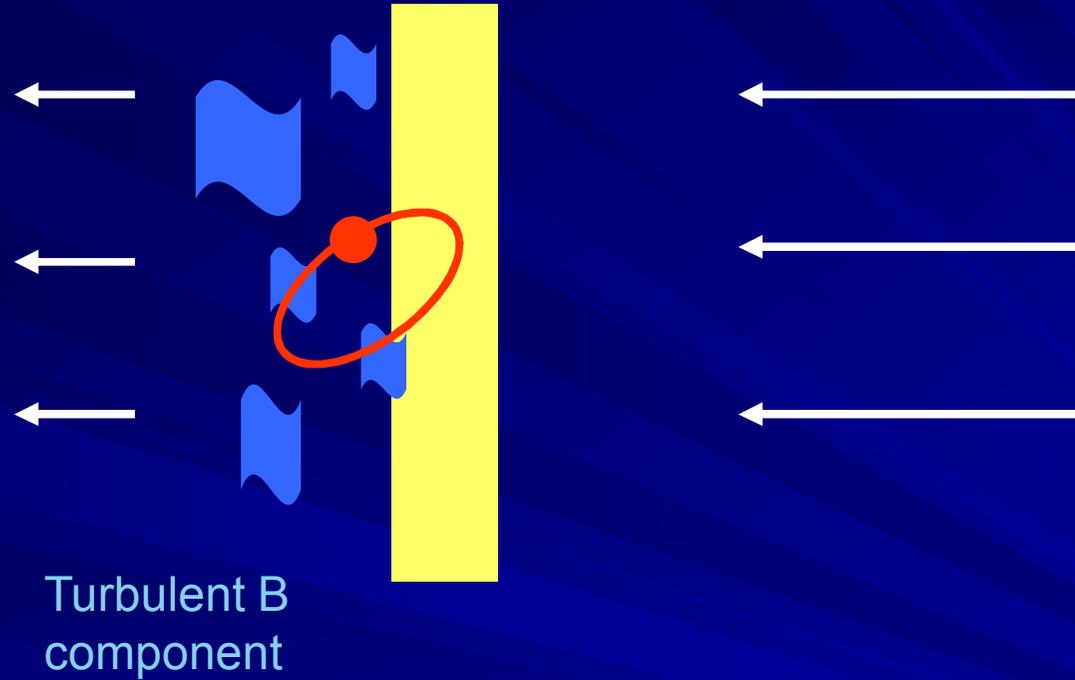
$$\tau_e(\text{Gyr}) \sim 4 \times \left\{ \frac{1}{3} \left( \frac{\gamma}{300} \right) \left[ \left( \frac{B_{\mu\text{G}}}{3.2} \right)^2 \frac{\sin^2 \theta}{2/3} + (1+z)^4 \right] + \left( \frac{n_{\text{th}}}{10^{-3}} \right) \left( \frac{\gamma}{300} \right)^{-1} \left[ 1.2 + \frac{1}{75} \ln \left( \frac{\gamma/300}{n_{\text{th}}/10^{-3}} \right) \right] \right\}^{-1}$$

**< 0.1 Gyrs**

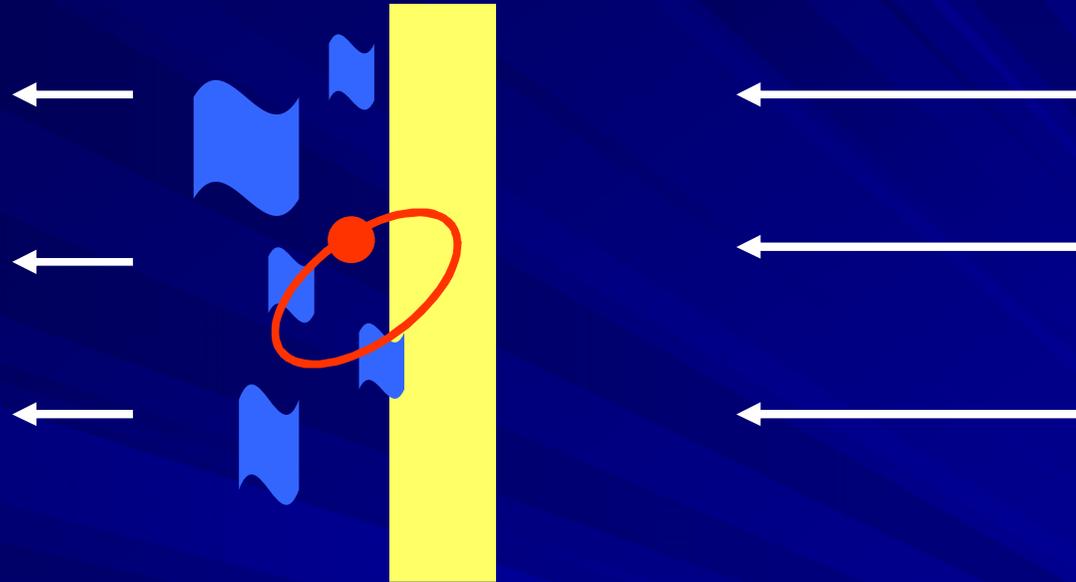
# Acceleration of CR at shocks



# Acceleration of CR at shocks



# Acceleration of CR at shocks



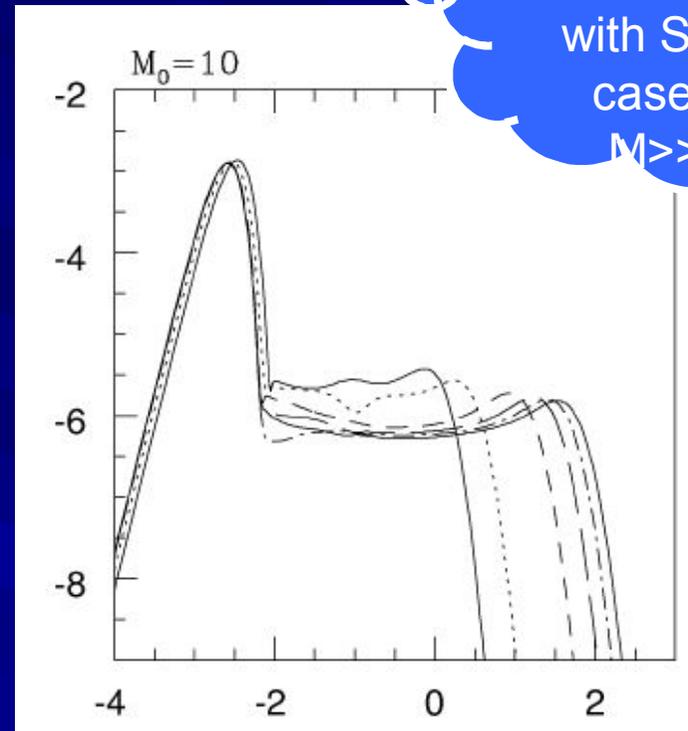
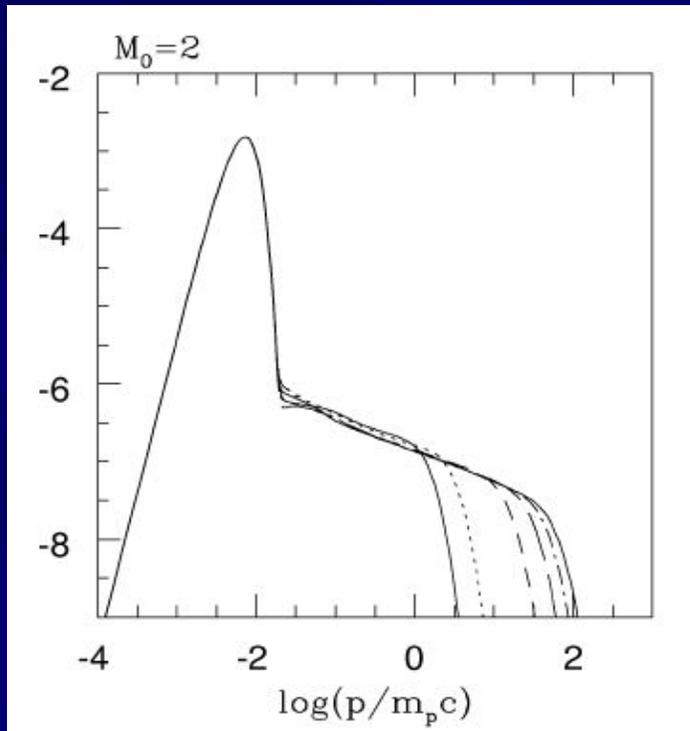
The level of amplification of the turbulent field in the post shock region is necessary to calculate the efficiency of particle acceleration & the minimum momentum of particles that can be accelerated at the shock.

This physics is not yet under control !

# Acceleration of CRp at shocks

$p_{inj}$  is a “free parameter” ... it's a *guess* !

$p_{inj}$  is calibrated with SN in case of  $M \gg 1$



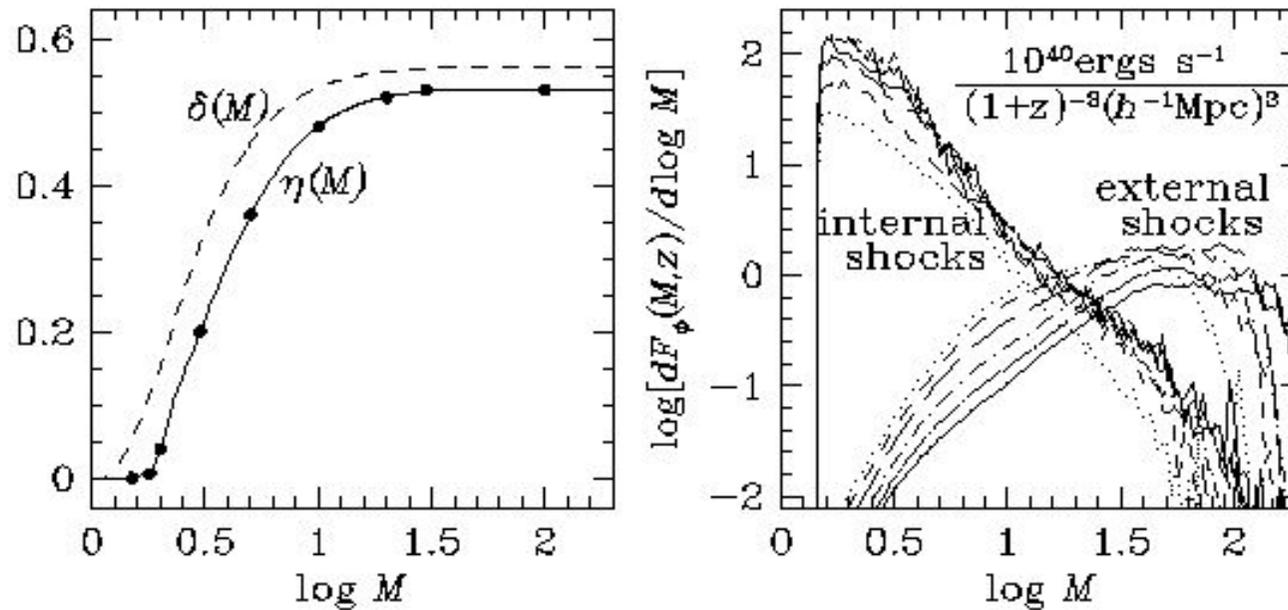
(Kang & Jones 2002; see also Malkov 1997, Kang & Jones 2005, 07, Amato & Blasi 2006)

However going from  $p_{inj} = 3.5 p_{th}$  to  $3.8$  reduces the acceleration efficiency by a factor of 10 !

# Acceleration of CRp at shocks

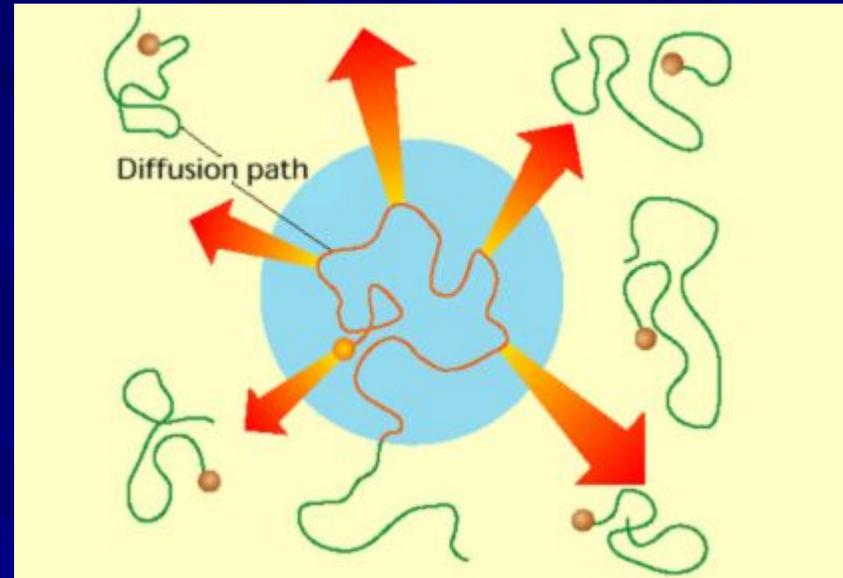
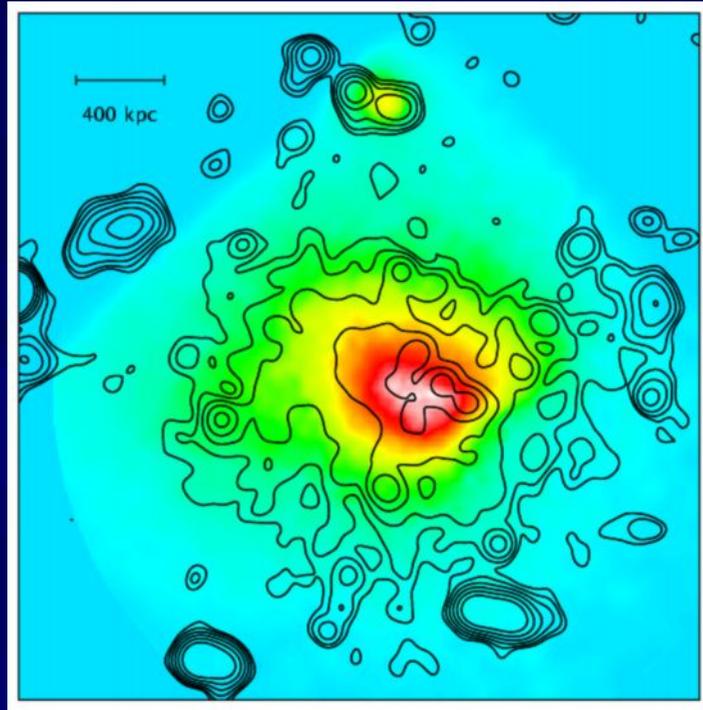
The efficiency strongly depends on Mach number !!!

Ryu et al. 2003

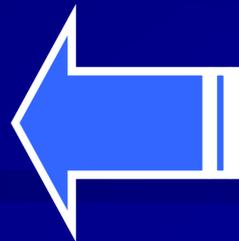


Having  $M=2$  or  $M=2.5$  implies a difference of 10 in terms of acceleration efficiency

# Origin of Radio Halos



$$R \approx 2\sqrt{\tau D}$$

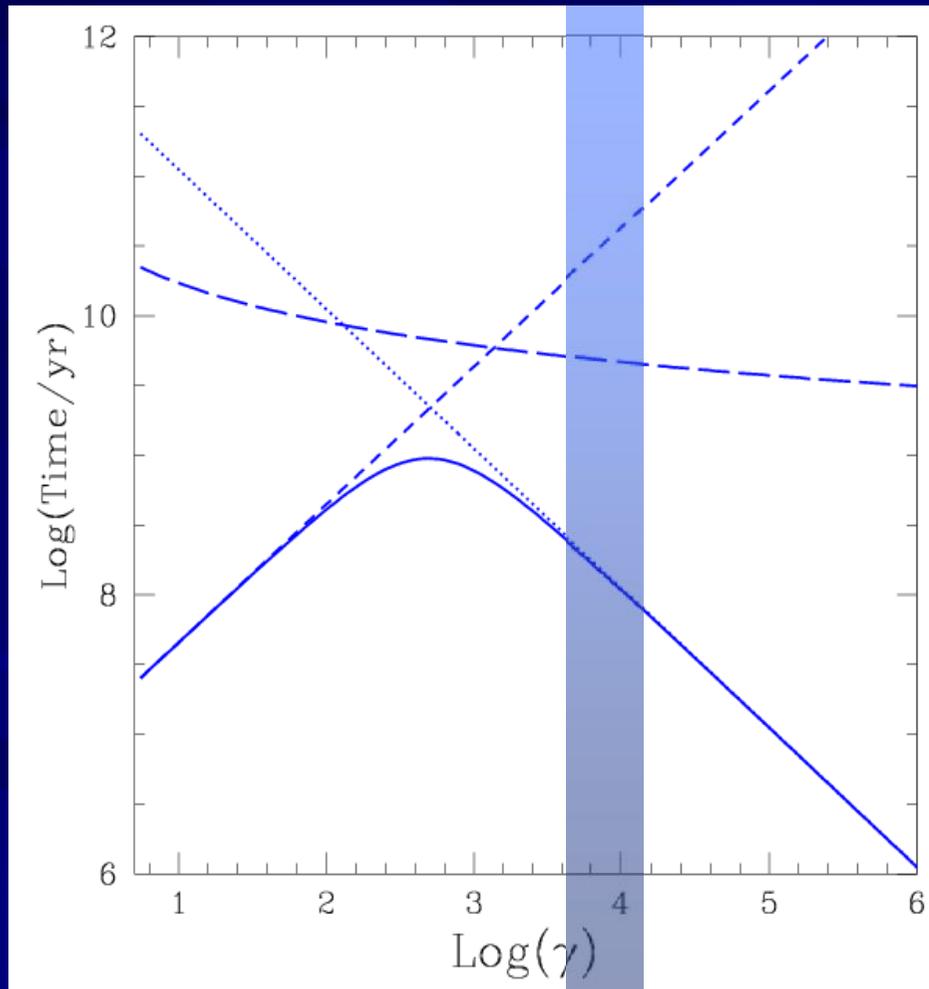


$$\frac{\partial n_p(E_p, r, t)}{\partial t} - D(E) \nabla^2 n_p(E_p, r, t)$$

$$D(E_p) = \frac{1}{3} r_{LC} \frac{B^2}{\int_{1/r_L}^{\infty} dk P(k)}$$

# Physics of CR Leptons

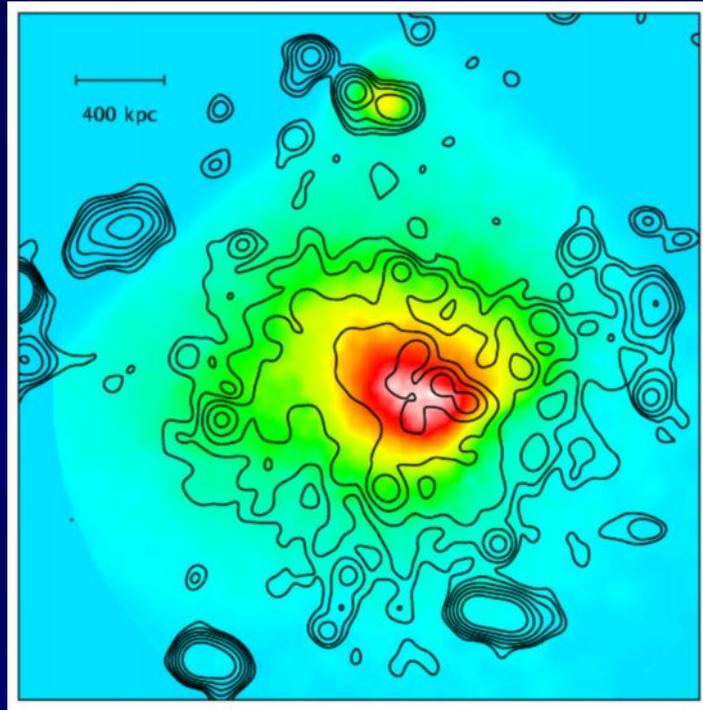
$$(dE/dt) \sim \mathbf{E} / \mathbf{Time}$$



$$\tau_e(\text{Gyr}) \sim 4 \times \left\{ \frac{1}{3} \left( \frac{\gamma}{300} \right) \left[ \left( \frac{B_{\mu G}}{3.2} \right)^2 \frac{\sin^2 \theta}{2/3} + (1+z)^4 \right] + \left( \frac{n_{th}}{10^{-3}} \right) \left( \frac{\gamma}{300} \right)^{-1} \left[ 1.2 + \frac{1}{75} \ln \left( \frac{\gamma/300}{n_{th}/10^{-3}} \right) \right] \right\}^{-1}$$

*The life-time of electrons depends on quantities that are well measured*

# Radio Halos



The diffusion time of the emitting electrons necessary to cover Mpc distances is 100 times larger than their radiative life-time

$$\tau = \tau_E$$

$$R \approx 2\sqrt{\tau D}$$

Brunetti 2003

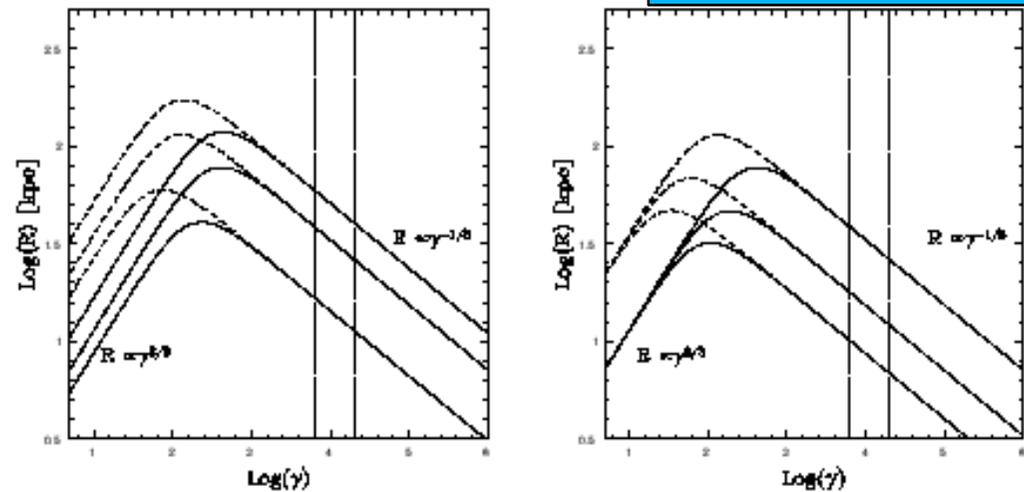
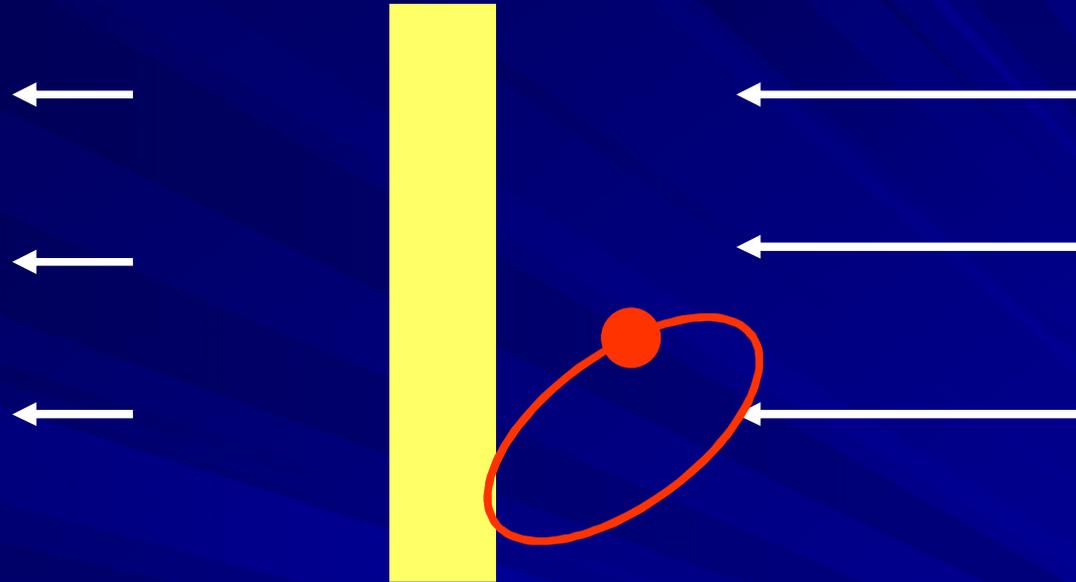
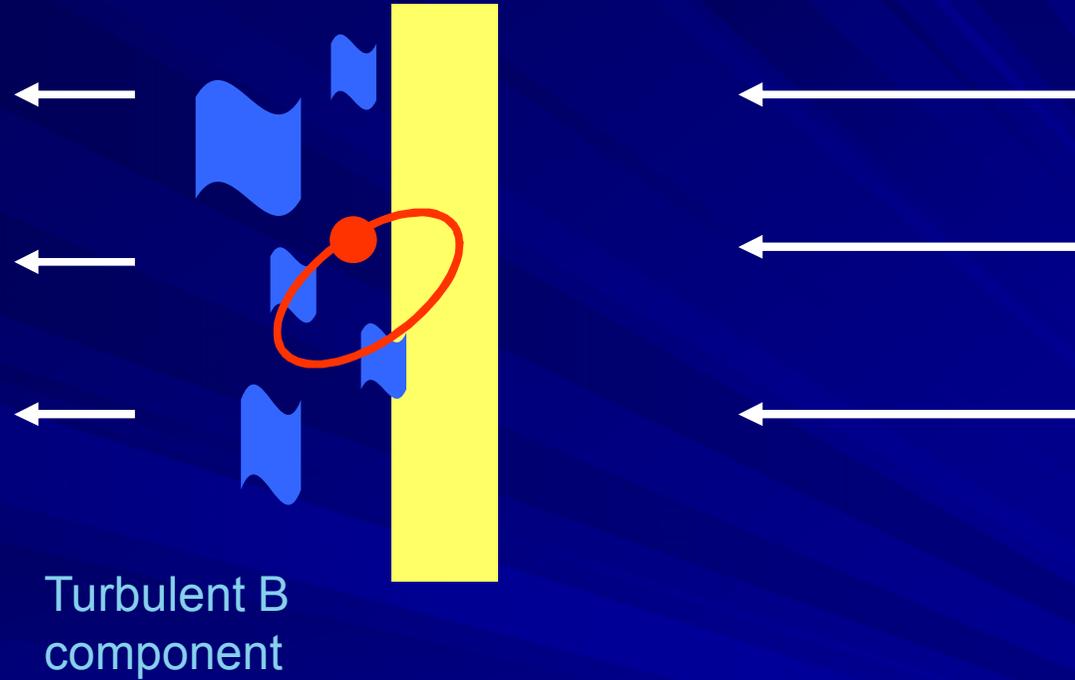


Figure 2. **Panel a)** : Diffusion lengths are reported as a function of  $\gamma$  of the electrons. Calculations are performed at  $z = 0$ , for  $n_{\text{th}} = 10^{-3} \text{ cm}^{-3}$  (solid lines) and  $10^{-4} \text{ cm}^{-3}$  (dashed lines) assuming (from the bottom)  $B = 5, 1, \text{ and } 0.1 \mu\text{G}$ . **Panel b)** : Diffusion lengths as in panel a), but assuming  $B = 1 \mu\text{G}$ , and  $z = 0, 0.5, \text{ and } 1.0$  (from the top). The energy range of the radio emitting electrons is reported in both panels (vertical dotted lines).

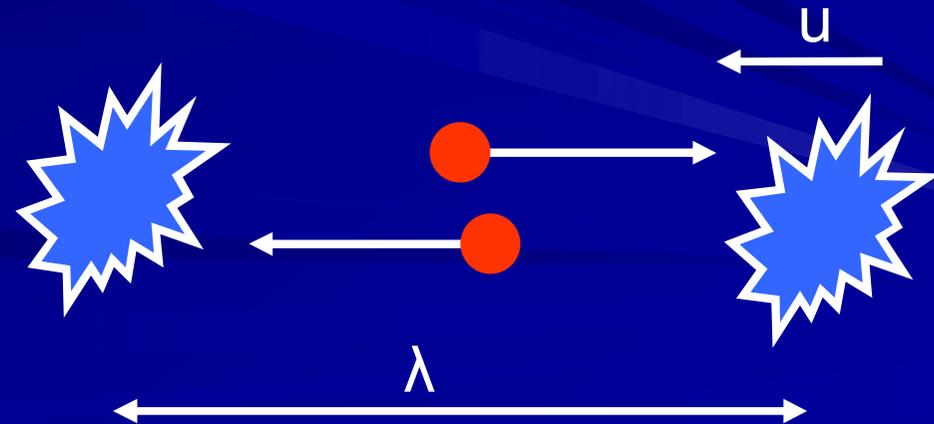
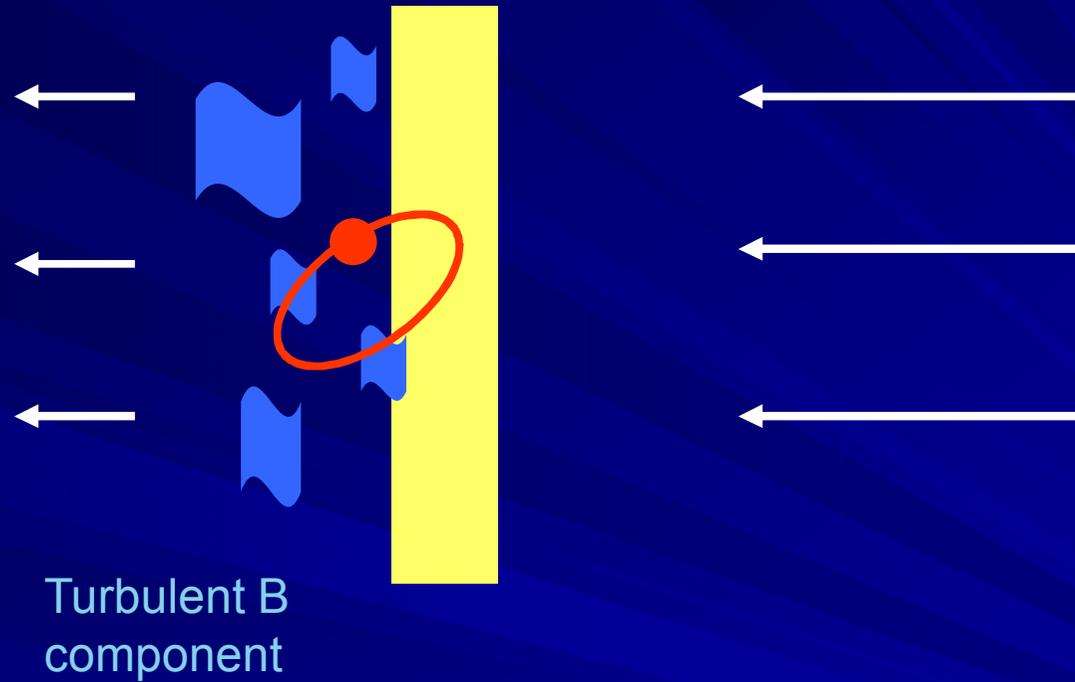
# Acceleration of CR at shocks

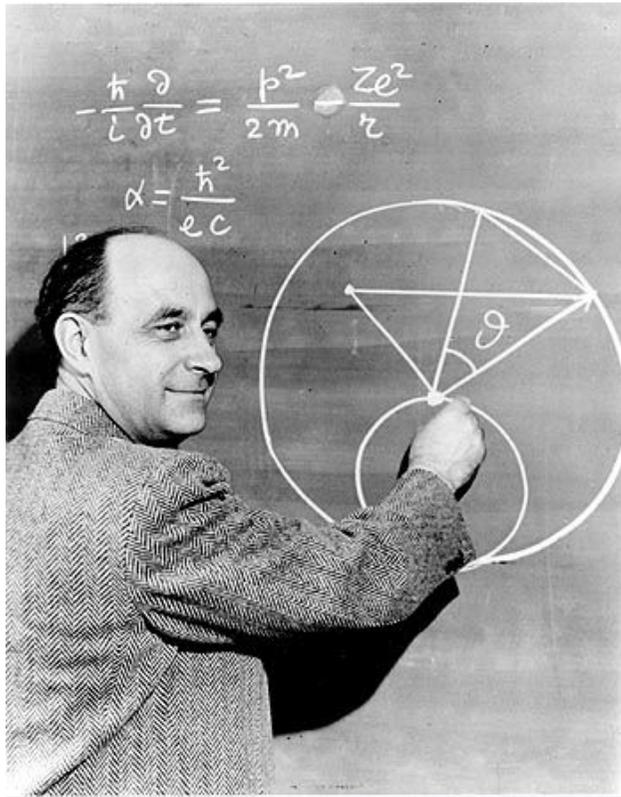


# Acceleration of CR at shocks

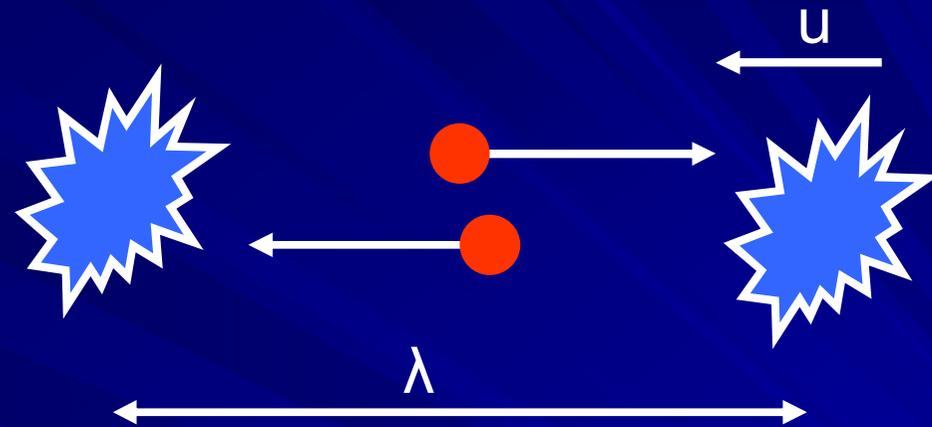


# Acceleration of CR at shocks





# First order Fermi Mechanisms (Fermi 1949)



Frequency of collisions: 
$$V_+ = \frac{u + c}{\lambda}$$

Energy gain per collisions: 
$$\Delta p_+ = 2p \frac{u}{c}$$

Energy gain per second: 
$$\left\langle \frac{\Delta p}{\Delta t} \right\rangle \approx 2p \frac{u}{c} \frac{c}{\lambda}$$

# Physics of CR Leptons

Sarazin 1999 ; Brunetti 2003 for reviews

$(dE/dt) / m_e c^2 = b =$  rate of energy losses in units of  $m_e c^2$

$$b_{\text{IC}}(\gamma) = \frac{4}{3} \frac{\sigma_T}{m_e c} \gamma^2 U_{\text{CMB}} = 1.37 \times 10^{-20} \gamma^2 (1+z)^4 \text{ s}^{-1},$$

$$b_{\text{syn}}(\gamma) = \frac{4}{3} \frac{\sigma_T}{m_e c} \gamma^2 U_B = 1.30 \times 10^{-21} \gamma^2 \left( \frac{B}{1 \mu\text{G}} \right)^2 \text{ s}^{-1},$$

Photon  
Collisions

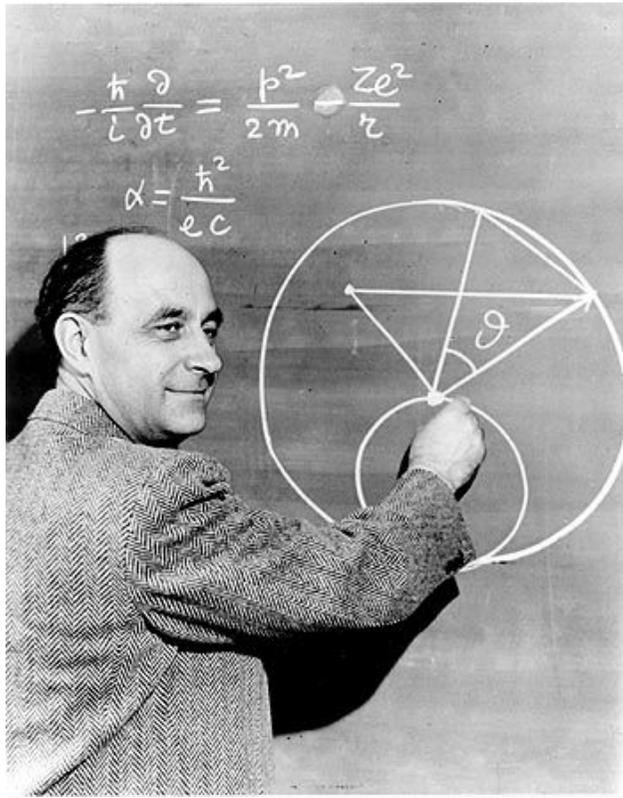
Particle  
Collisions

$$b_{\text{Coul}}(\gamma) \approx 1.2 \times 10^{-12} n_e \left[ 1.0 + \frac{\ln(\gamma/n_e)}{75} \right] \text{ s}^{-1},$$

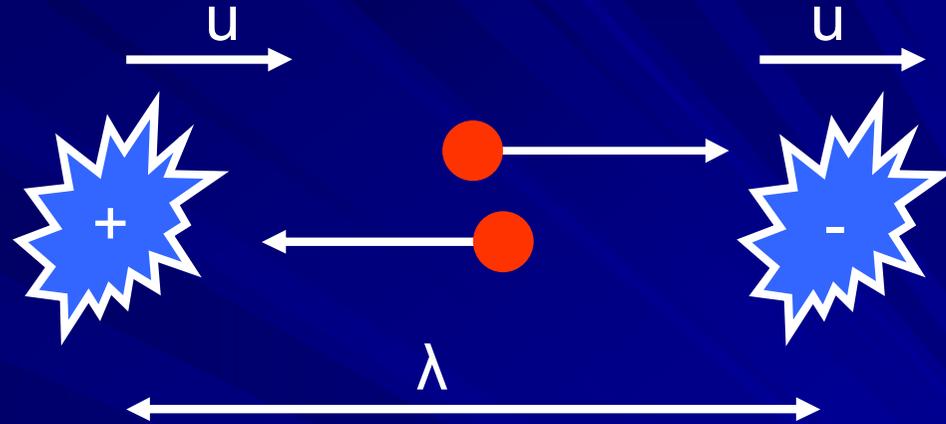
$$b_{\text{brem}}(\gamma) \approx 1.51 \times 10^{-16} n_e \gamma [\ln(\gamma) + 0.36] \text{ s}^{-1},$$

# IV - Conclusion

- (a) Synchrotron emission from secondaries is an unavoidable process in the IGM
- (b) Still this is probably not the (unique) process at the origin of Radio Halos ... the level of CR protons is below that necessary to explain Radio Halos



# Second order Fermi Mechanisms (Fermi 1949)



Frequency of collisions:  $\nu_+ = \frac{u + c}{\lambda}$      $\nu_- = \frac{c - u}{\lambda}$

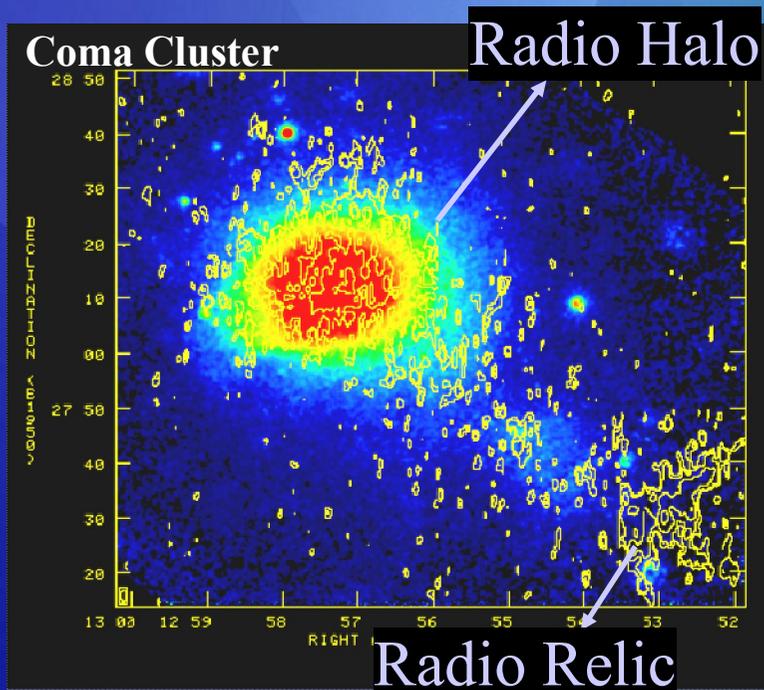
Energy gain per collisions:  $\Delta p_{\pm} \approx \pm 2 p \frac{u}{c}$

$$\left\langle \frac{\Delta p}{\Delta t} \right\rangle = \nu_+ \Delta p_+ + \nu_- \Delta p_- \approx 2 p \frac{u^2}{c^2} \frac{c}{\lambda}$$

# Non-thermal components

## Observational evidences

Diffuse synchrotron radio sources from the ICM (not associated with any individual galaxy):



**Radio Halos** ( $L_{1.4\text{GHz}} \sim 10^{24}-10^{26} h_{70}^{-2} \text{ Watt/Hz}$ )

- steep spectrum sources ( $\alpha \sim 1.1-1.5$ )
- low surface brightness ( $\mu\text{Jy arcsec}^{-2}$  at 1.4 GHz)
- at the cluster centre
- generally regular shape (mimic the X-ray morphology) (~Mpc size)

**Radio Relics** ( $L_{1.4\text{GHz}} \sim 10^{23}-10^{25} h_{70}^2 \text{ Watt/Hz}$ )

- steep spectrum sources ( $\alpha \sim 1.1-1.5$ )
- at the cluster outskirts
- elongated morphology + polarised

**Halos** and **Relics** prove the presence of **non-thermal components**, **GeV** electrons ( $\gamma \sim 10^4$ ) and  $\mu\text{G}$  magnetic field, mixed with the thermal ICM on Mpc scales

**CR+B : important not only for particle acceleration ....**

**Thermal conduction and kin. viscosity in the ICM**

**(e.g., Lazarian 2006)**

**Heating of the ICM and “cooling flow” problem**

**(e.g., Fujita , Matsumoto, Weda 2004; Guo & Oh 2008)**

**Diffusion and transport of metals in the ICM**

**(e.g., Voigt & Fabian 2004; Rebusco +al. 2005)**

**B-Amplification from Cosmological seed fields**

**(e.g., Dolag +al. 1999,02; Subramanian +al. 2006)**

**Diffusion and scattering of HE & UHECR in the Universe**

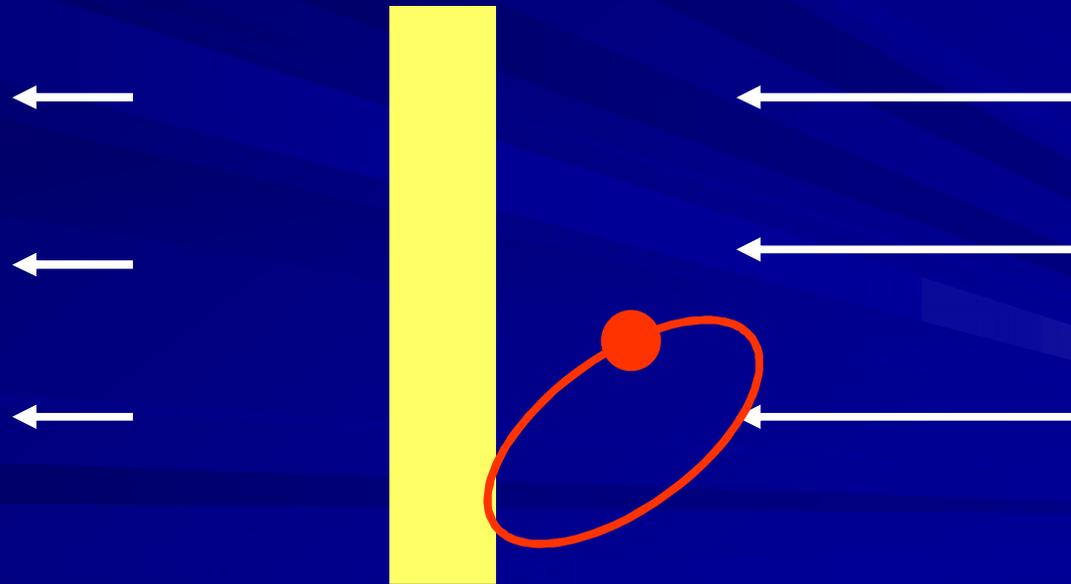
**(e.g., Sigl +al. 2005; Dolag +al. 2005)**

# Acceleration of CRp at shocks

$$N(p) \propto p^{-\delta}$$

$$\delta = 2 \frac{\mathcal{M}^2 + 1}{\mathcal{M}^2 - 1}$$

Linear Theory  
(e.g., Blandford & Eichler 1987)

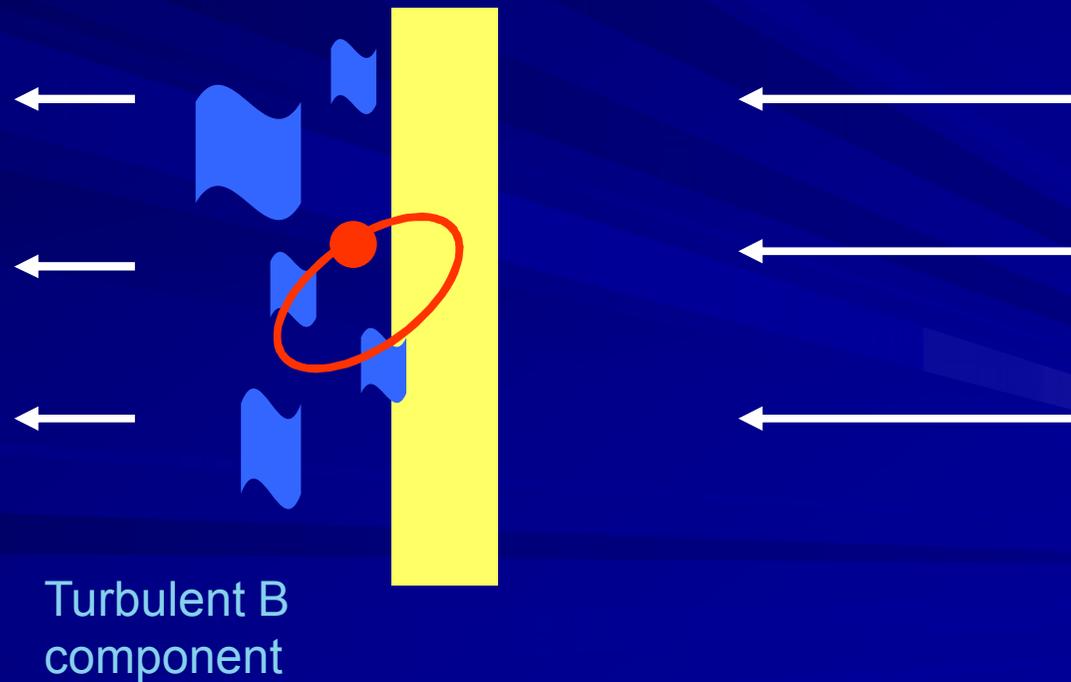


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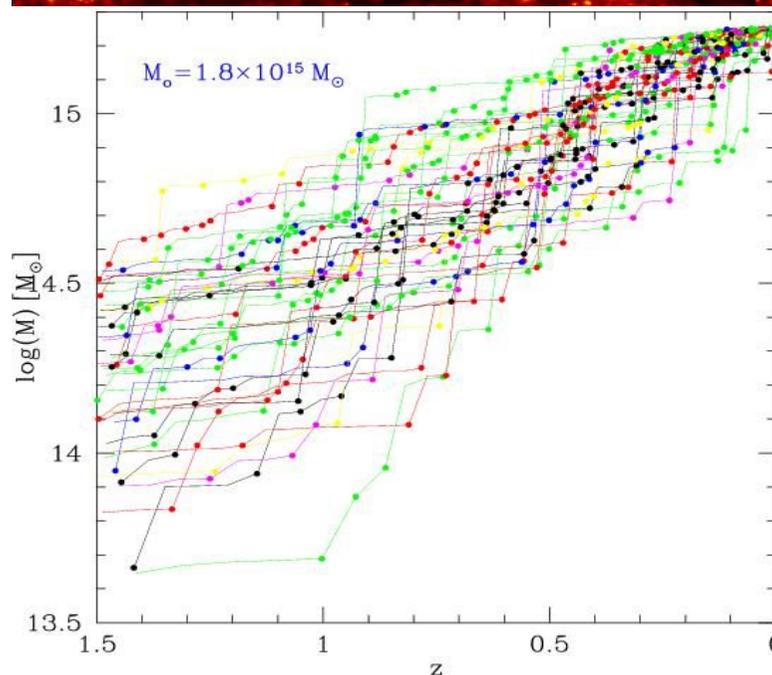
Linear Theory  
(e.g., Blandford & Eichler 1987)



Mergings are the most energetic events in the Universe  $\approx$  few  $10^{63}$  ergs in a crossing time

$$E_M = \frac{10^{63-64}}{10} \approx 10^{47} \text{ ergs}$$

$t_{\text{cross}} \rightarrow 10^9 \text{ yrs}$



1E 0657-56

Markevitch et al.

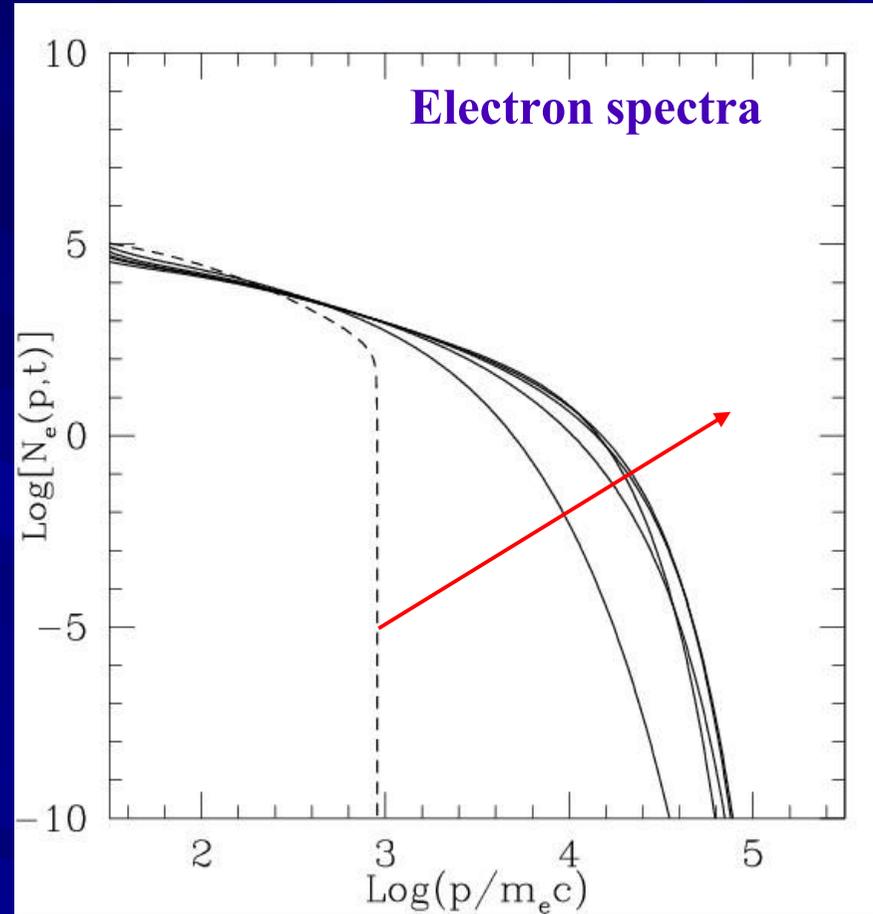
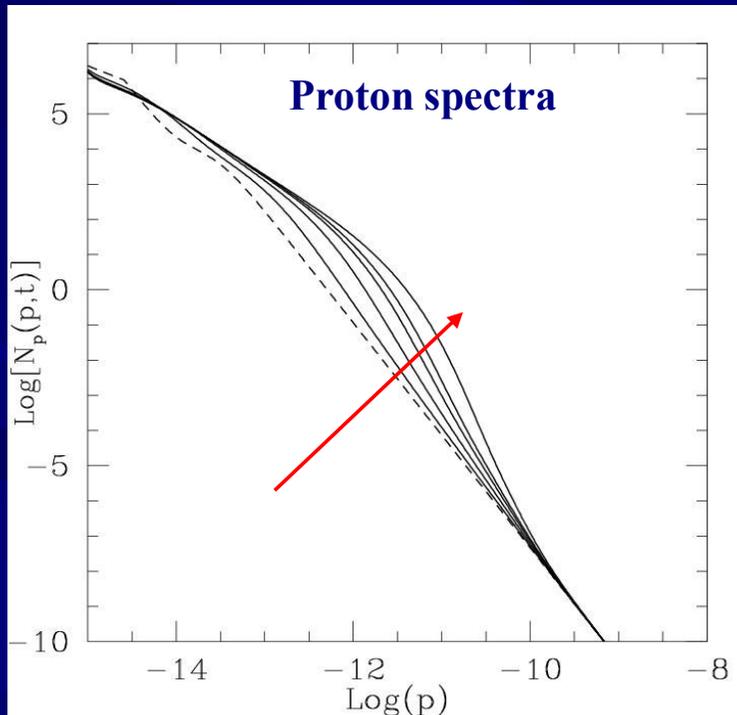
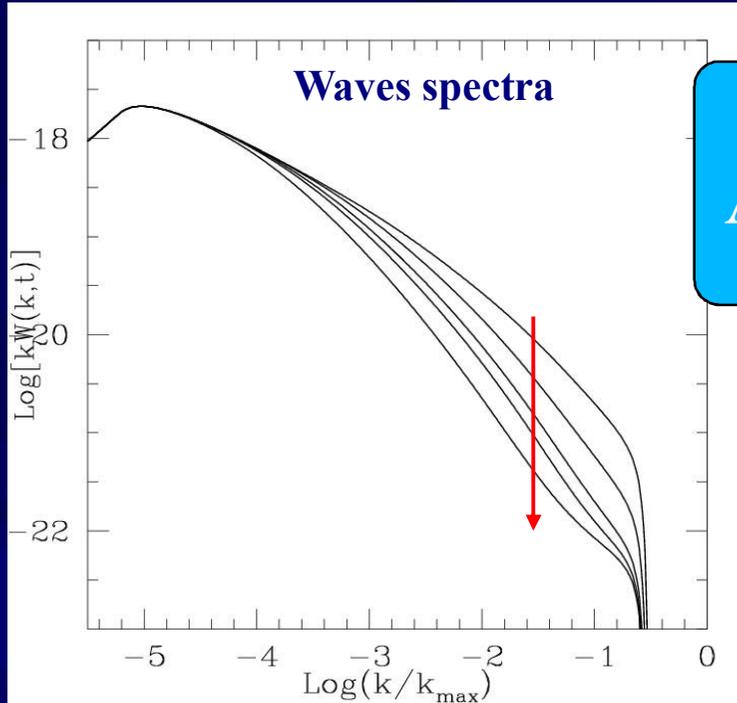
Chandra 0.5 Msec image

0.5 Mpc

z=0.3

# Full Alfven-Wave--Particle Coupling

(Brunetti et al. 2004)



Waves + electrons + Protons