

R. Dicke (1961)

$$10^{-10}$$

$$\alpha = \frac{4 \times 10^{-10}}{c^2 R} = 1.75 \times 10^{-18}$$

$$\alpha \propto \frac{1}{R} \quad \alpha_{L=14} = 2$$

$$\alpha_{L=20} = \frac{2 \times 10^{-10}}{c^2 R}$$

Soldner

J. Blamont

F. Rodd

$$\lambda = 4607 \text{ \AA}$$

PD

$$4.92 \cdot 10^{-15}$$

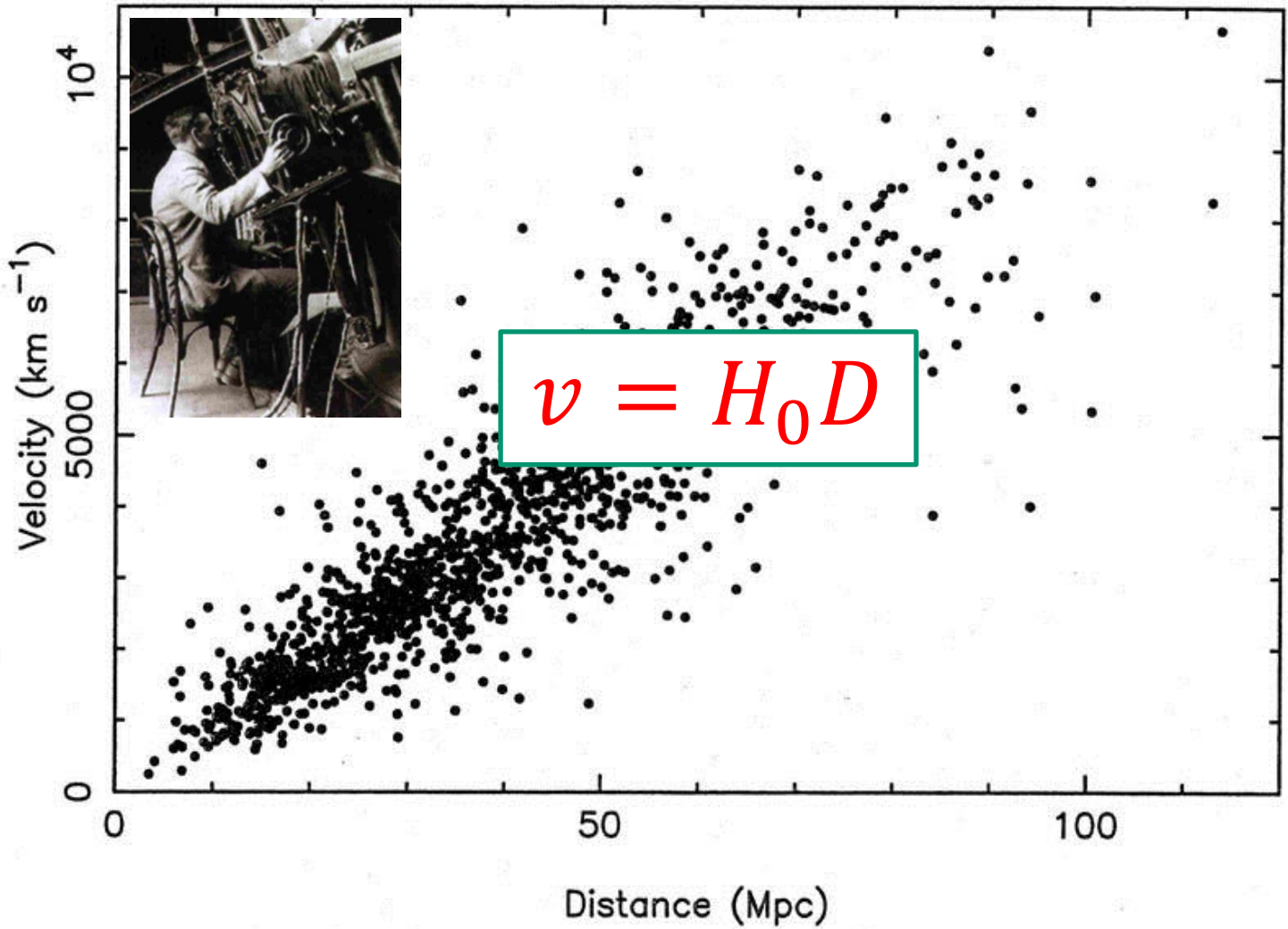
$$\frac{v_{ex}}{c} = 0.97 \pm$$

$$0.035$$



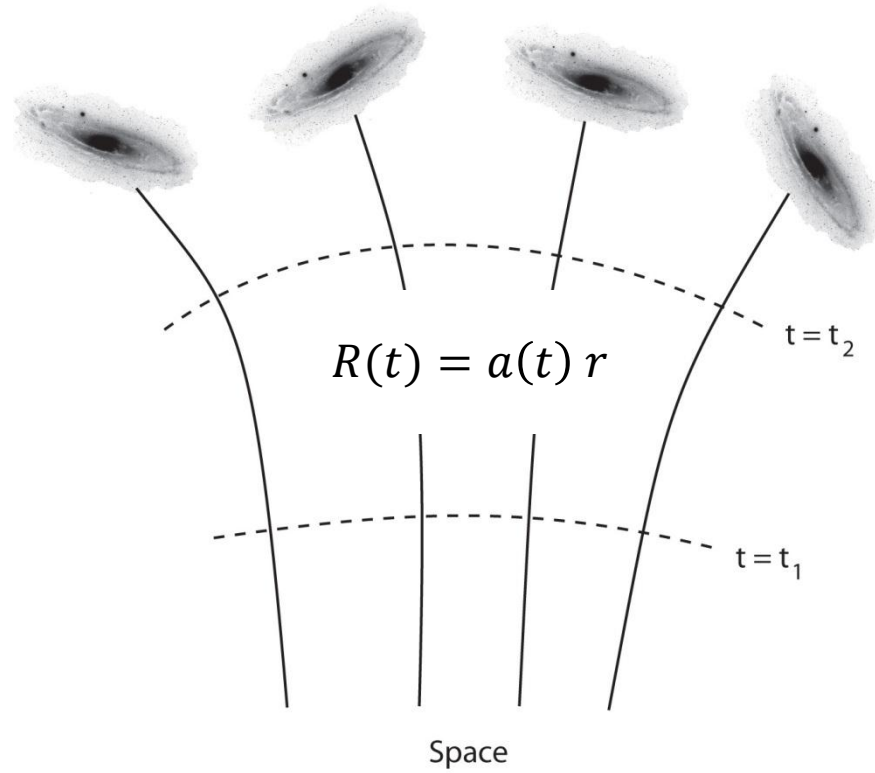


The $R_h = ct$ Universe



$H_0 = 74.2 \pm 3.6 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (Riess et al. 2009)

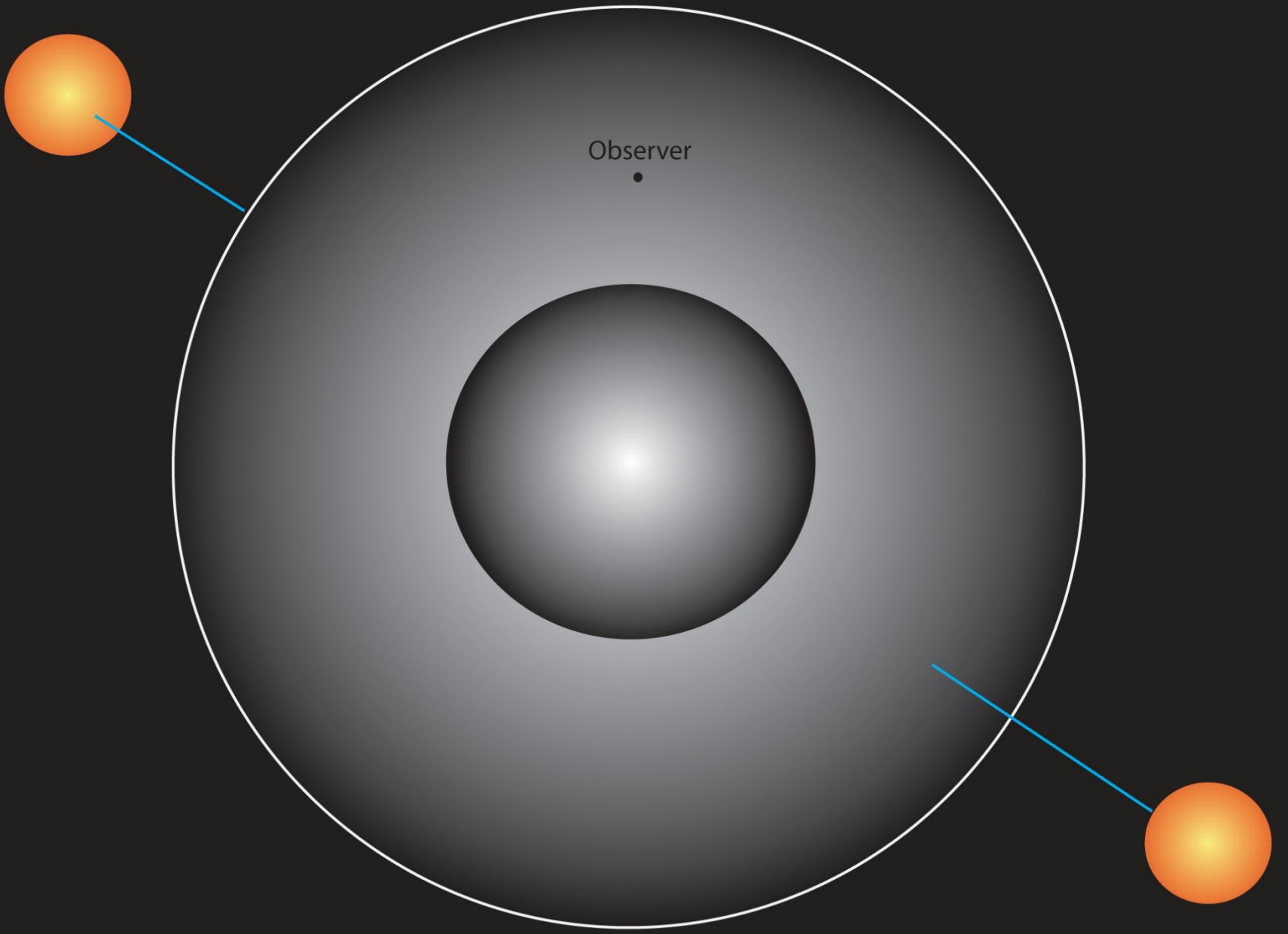
Weyl's Postulate



The Hubble Constant

$$v = \frac{dR}{dt} = \frac{da}{dt}r \qquad v = \frac{\dot{a}}{a}ar \qquad v = HR$$

$$H = \frac{\dot{a}}{a}$$



Observer

The Gravitational Horizon

$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3}\rho - \frac{kc^2}{a^2}$$

$$R_h = \frac{2GM(R_h)}{c^2}$$

where $M(R_h) = \frac{4\pi}{3} R_h^3 \rho$

In a flat geometry ($k=0$),

$$\rho = \rho_c = \frac{3c^2 H^2}{8\pi G}$$

Thus,

$$R_h = \frac{c}{H(t)}$$

Weyl's Postulate Revisited

R_h is the proper radius that defines a proper volume

So according to Weyl's Postulate,

$$R_h = a(t)r_h \quad r_h = \text{constant}$$

Therefore, with

$$R_h = \frac{c}{H(t)} = \frac{ca}{\dot{a}}$$

one gets

$$\dot{a} = c r_h = \text{constant}$$

So

$$R_h = ct$$

The Standard (Λ CDM) Model

$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3}\rho - \frac{kc^2}{a^2}$$

$$\rho = \rho_m + \rho_r + \rho_{de}$$

$$\rho_m \propto a^{-3}$$

$$\rho_r \propto a^{-4}$$

$$\rho_{de} = \Lambda = \text{constant}$$

The Standard (Λ CDM) Model

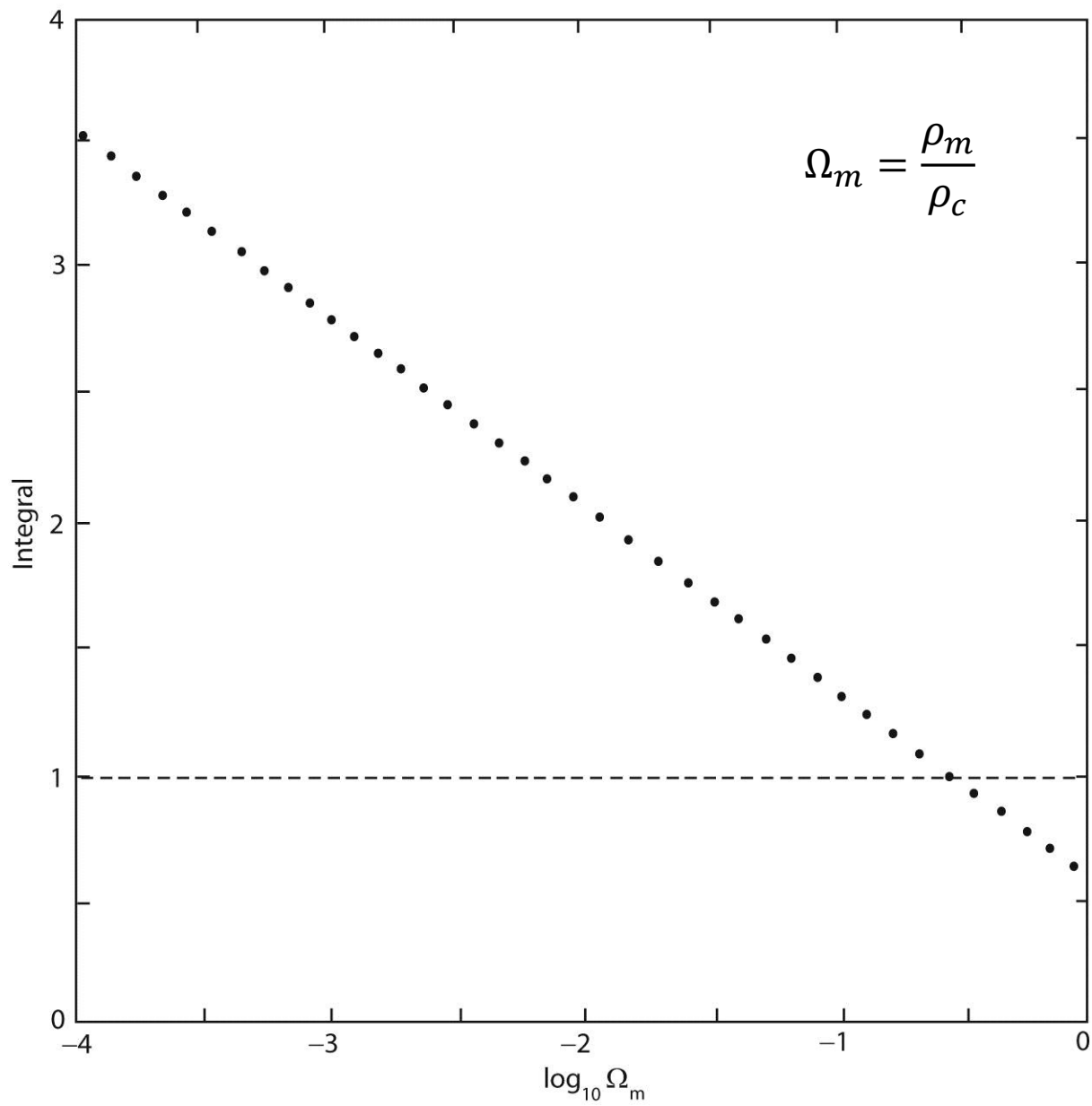
$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3}\rho - \frac{kc^2}{a^2}$$

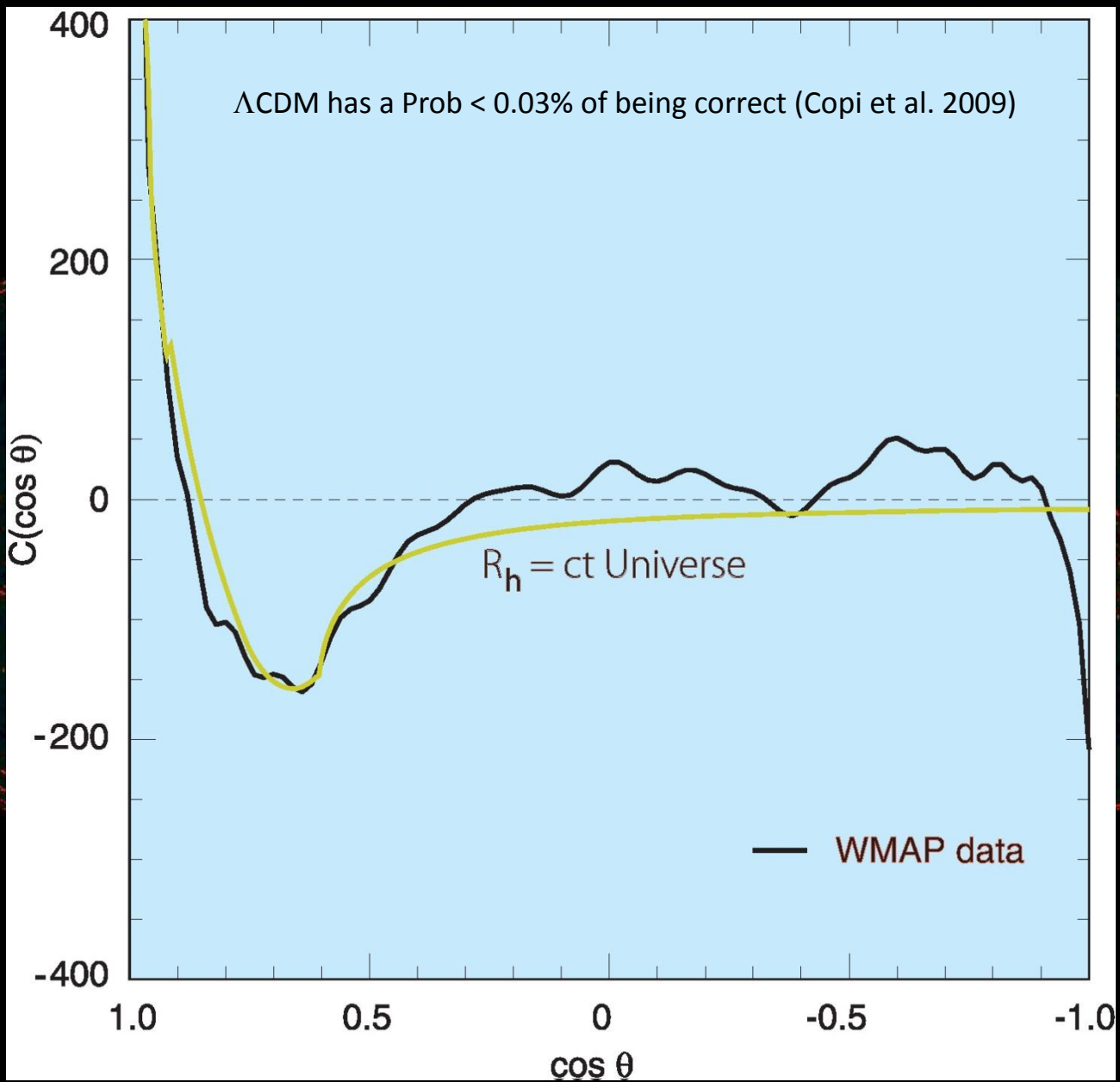
$$\int \frac{da}{f(a)} = \int dt$$

$$ct_0 = R_h(t_0) I(\rho_m, \rho_r, \Lambda)$$

So Weyl's Postulate requires

$$I(\rho_m, \rho_r, \Lambda) = 1$$





The Nearby Universe (Type Ia Supernovae)

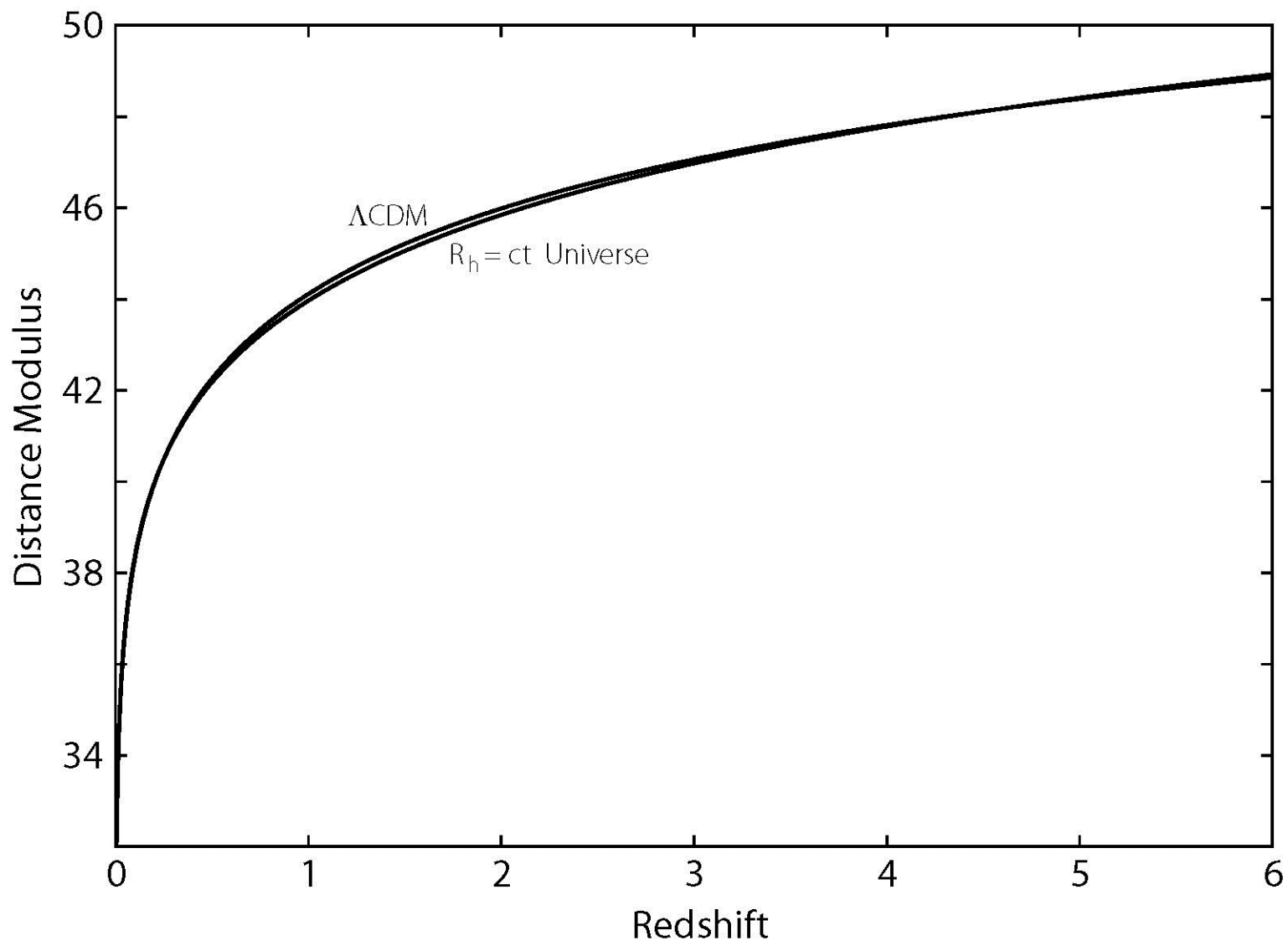
Λ CDM

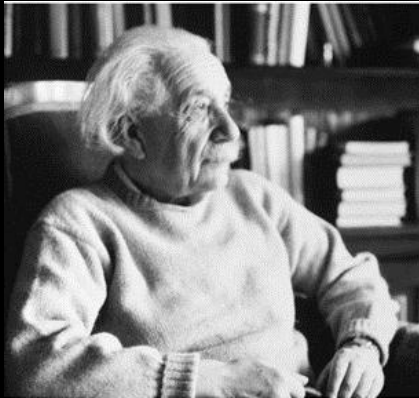
$$d_L = R_h(1+z) \int_{(1+z)^{-1}}^1 \frac{du}{\sqrt{\Omega_r + u\Omega_m + u^4\Omega_\Lambda}}$$

$R_h = ct$

$$d_L = R_h(1+z) \ln(1+z)$$

Plus 4 “nuisance” parameters that must be optimized along with cosmological model to determine the individual supernova distance moduli: (1) the normalization to the time-dependent SED of the SN, (2) the deviation from the average light-curve shape, (3) the deviation from the mean SN B-V color, and (4) a host-mass dependent correction.





Einstein (1879-1955)



Friedmann (1888-1925)



Blrkhoff (1884-1944)



Weyl (1885-1955)

The Universe may turn out to be far simpler than we thought . . .

It is apparently flat ($k = 0$) so it has no net energy

Its size today is consistent with a constant expansion rate

And it may have expanded without any inflation . . .