

# The effect of Coulomb correlations on non-equilibrium charge redistribution tuned by tunneling current

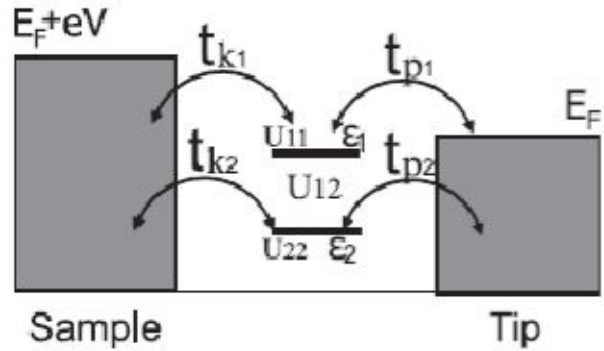
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## Two-level system

a



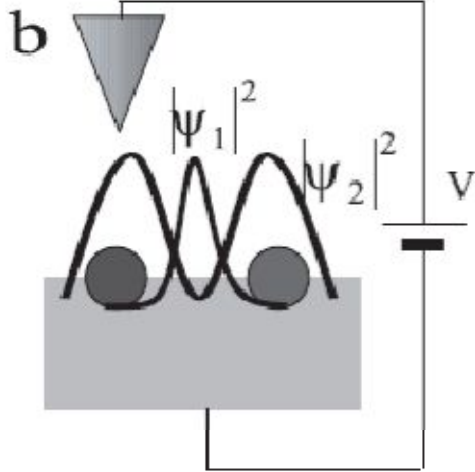
$$\hat{H} = \sum_{i\sigma} \varepsilon_i n_{i\sigma} + \sum_{k\sigma} \varepsilon_k c_{k\sigma}^\dagger c_{k\sigma} + \sum_{p\sigma} \varepsilon_p c_{p\sigma}^\dagger c_{p\sigma}$$

$$+ \sum_{ij\sigma\sigma'} U_{ij}^{\sigma\sigma'} n_{i\sigma} n_{j\sigma'} +$$

$$+ \sum_{ki\sigma} t_{ki} (c_{k\sigma}^\dagger c_{i\sigma} + h.c.) + \sum_{pi\sigma} t_{pi} (c_{p\sigma}^\dagger c_{i\sigma} + h.c.)$$

Current

$$I = I_{k\sigma} = \sum_{i\sigma} I_{ki\sigma} = i \sum_{ki\sigma} t_{ki} (\langle c_{k\sigma}^\dagger c_{i\sigma} \rangle - \langle c_{i\sigma}^\dagger c_{k\sigma} \rangle)$$



## Current calculations

$$i \frac{\partial c_{k\sigma}^+ c_{i\sigma}}{\partial t} = (\varepsilon_i - \varepsilon_k) \cdot c_{k\sigma}^+ c_{i\sigma} + U_{ii} n_{i-\sigma} \cdot c_{k\sigma}^+ c_{i\sigma} + U_{ij} (n_{j\sigma} + n_{j-\sigma}) \cdot c_{k\sigma}^+ c_{i\sigma} \\ - t_{ki} \cdot (n_{i\sigma} - \hat{f}_k) + \sum_{k' \neq k} t_{k'i} c_{k\sigma}^+ c_{k'\sigma} + \sum_{i \neq j} t_{kj} c_{j\sigma}^+ c_{i\sigma} = 0$$

$$\hat{f}_k = c_{k\sigma}^+ c_{k\sigma}$$

$$n_{1-\sigma} (1 - n_{2-\sigma}) (1 - n_{2\sigma}) c_{k\sigma}^+ c_{1\sigma} =$$

$$\{ (t_{k1} \cdot (n_{1\sigma} - \hat{f}_k) + \sum_{k' \neq k} t_{k'1} c_{k\sigma}^+ c_{k'\sigma} + t_{k2} c_{2\sigma}^+ c_{1\sigma}) \cdot n_{1-\sigma} (1 - n_{2-\sigma}) (1 - n_{2\sigma}) \} \cdot \{ \varepsilon_1 - \varepsilon_k + U_{11} \}^{-1}$$

Simplifications due to  $\hat{n}_i^2 = 1$

$$(1 - n_{1-\sigma}) (1 - n_{2-\sigma}) (1 - n_{2\sigma}) + n_{1-\sigma} (1 - n_{2-\sigma}) (1 - n_{2\sigma}) + \\ + \sum_{\sigma'} n_{2\sigma'} (1 - n_{1-\sigma}) (1 - n_{2-\sigma'}) + \sum_{\sigma'} n_{1-\sigma} n_{2\sigma'} (1 - n_{2-\sigma'}) + n_{2-\sigma} n_{2\sigma} (1 - n_{1-\sigma}) + n_{1-\sigma} n_{2-\sigma} n_{2\sigma} = 1$$

## Current in terms of correlators

$$I_{k1\sigma} = i t_{ki} (\langle c_{k\sigma}^+ c_{1\sigma} \rangle - \langle c_{1\sigma}^+ c_{k\sigma} \rangle) \quad \longrightarrow$$

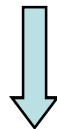
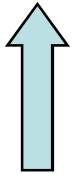
$$I_{k1\sigma} = \Gamma_{k1} \{ \langle n_{1\sigma} \rangle - \langle (1-n_{1-\sigma})(1-n_{2-\sigma})(1-n_{2\sigma}) \rangle f_k(\varepsilon_1) - \langle n_{1-\sigma}(1-n_{2-\sigma})(1-n_{2\sigma}) \rangle \cdot f_k(\varepsilon_1 + U_{11}) - \\ - \langle n_{2\sigma}(1-n_{2-\sigma})(1-n_{1-\sigma}) \rangle \cdot f_k(\varepsilon_1 + U_{12}) - \langle n_{2-\sigma}(1-n_{2\sigma})(1-n_{1-\sigma}) \rangle \cdot f_k(\varepsilon_1 + U_{12}) - \\ - \langle n_{1-\sigma}n_{2\sigma}(1-n_{2-\sigma}) \rangle \cdot f_k(\varepsilon_1 + U_{11} + U_{12}) - \langle n_{1-\sigma}n_{2-\sigma}(1-n_{2\sigma}) \rangle \cdot f_k(\varepsilon_1 + U_{11} + U_{12}) - \\ - \langle n_{2\sigma}n_{2-\sigma}(1-n_{1-\sigma}) \rangle \cdot f_k(\varepsilon_1 + 2U_{12}) - \langle n_{1-\sigma}n_{2-\sigma}n_{2\sigma} \rangle \cdot f_k(\varepsilon_1 + U_{11} + 2U_{12}) \} +$$

$$+ t_{k1} t_{k2} v_{0k} c_{2\sigma}^+ c_{1\sigma} + \sum_{k' \neq k} \langle t_{k1} t_{k'1} c_{k\sigma}^+ c_{k'\sigma} \rangle \times [\dots]$$

## Stationarity conditions

$$\frac{\partial}{\partial t} \langle n_{i\sigma} n_{j\sigma'} \rangle = 0$$

$$\frac{\partial}{\partial t} \langle n_{j\sigma} n_{j-\sigma} n_{i-\sigma'} \rangle = 0$$



Triple correlators as functions of pair correlators

## Equations for the pair correlators

$$K_{11} \equiv \langle n_{1\sigma} n_{1-\sigma} \rangle \quad K_{22} \equiv \langle n_{2\sigma} n_{2-\sigma} \rangle \quad K_{12} \equiv \langle n_{1\sigma} n_{2\sigma} \rangle$$

$$\begin{pmatrix} \mathbf{A} \end{pmatrix} \times \begin{pmatrix} K_{11} \\ K_{12} \\ K_{22} \end{pmatrix} = \begin{pmatrix} \mathbf{F} \end{pmatrix} \quad \mathbf{F} = \begin{pmatrix} n_1^T(\varepsilon_1 + U_{11}) \cdot n_{1\sigma} \\ n_2^T(\varepsilon_2 + U_{22}) \cdot n_{2\sigma} \\ \frac{\Gamma_1}{\Gamma_1 + \Gamma_2} n_1^T(\varepsilon_1 + U_{12}) n_{2\sigma} + \frac{\Gamma_2}{\Gamma_1 + \Gamma_2} n_2^T(\varepsilon_2 + U_{12}) n_{1\sigma} \end{pmatrix}$$

$$a_{12} = 2 \cdot n_1^T(\varepsilon_1 + U_{11}) - n_1^T(\varepsilon_1 + U_{11} + U_{12}) - 2 \cdot \frac{\Gamma_2}{\Gamma_1} \cdot n_2^T(\varepsilon_2 + U_{22} + U_{12}) \cdot \Phi_1$$

$$\Phi_i = \frac{n_i^T(\varepsilon_i + U_{ii}) - n_i^T(\varepsilon_i + U_{ii} + U_{ij})}{3 + n_i^T(\varepsilon_i + 2 \cdot U_{ij}) - n_i^T(\varepsilon_i + U_{ii} + 2 \cdot U_{ij})} + \frac{n_i^T(\varepsilon_i + U_{ii} + 2 \cdot U_{ij})}{3 + n_i^T(\varepsilon_i + 2 \cdot U_{ij}) - n_i^T(\varepsilon_i + U_{ii} + 2 \cdot U_{ij})}$$

$$n_i^T(\varepsilon) = \frac{\Gamma_{ki} f_k(\varepsilon) + \Gamma_{pi} f_p(\varepsilon)}{\Gamma_{ki} + \Gamma_{pi}}$$

For large U we neglect triple correlators

$$I_{k1\sigma} = \Gamma_k \cdot \{ \langle n_{1\sigma} \rangle - (1 - \langle n_{1\sigma} \rangle - 2\langle n_{2\sigma} \rangle + K_{22} + 2K_{12}) \cdot f_k(\varepsilon_1) - \\ - (\langle n_{1\sigma} \rangle - 2K_{12}) \cdot f_k(\varepsilon_1 + U_{11}) - 2 \cdot (\langle n_{2\sigma} \rangle - K_{12} - K_{22}) \cdot f_k(\varepsilon_1 + U_{12}) \}$$

Solutions for the pair correlators look like:

$$K_{12} = \frac{\frac{1}{2} n^T(\varepsilon_1 + U_{12}) \cdot (1 - n^T(\varepsilon_2 + U_{22})) \cdot n_{2\sigma} + \frac{1}{2} n^T(\varepsilon_2 + U_{12}) \cdot (1 - n^T(\varepsilon_1 + U_{11})) \cdot n_{1\sigma}}{1 + n^T(\varepsilon_1 + U_{12}) \cdot (\frac{1}{2} - n^T(\varepsilon_2 + U_{22})) + n^T(\varepsilon_2 + U_{12}) \cdot (\frac{1}{2} - n^T(\varepsilon_1 + U_{11}))}$$

$$U_{ij} \rightarrow \infty$$

$$n_{1\sigma} = \frac{n_1^T(\varepsilon_1)(1 - n_2^T(\varepsilon_2))}{(1 + n_1^T(\varepsilon_1))(1 + n_2^T(\varepsilon_2)) - 4n_1^T(\varepsilon_1)n_2^T(\varepsilon_2)}$$

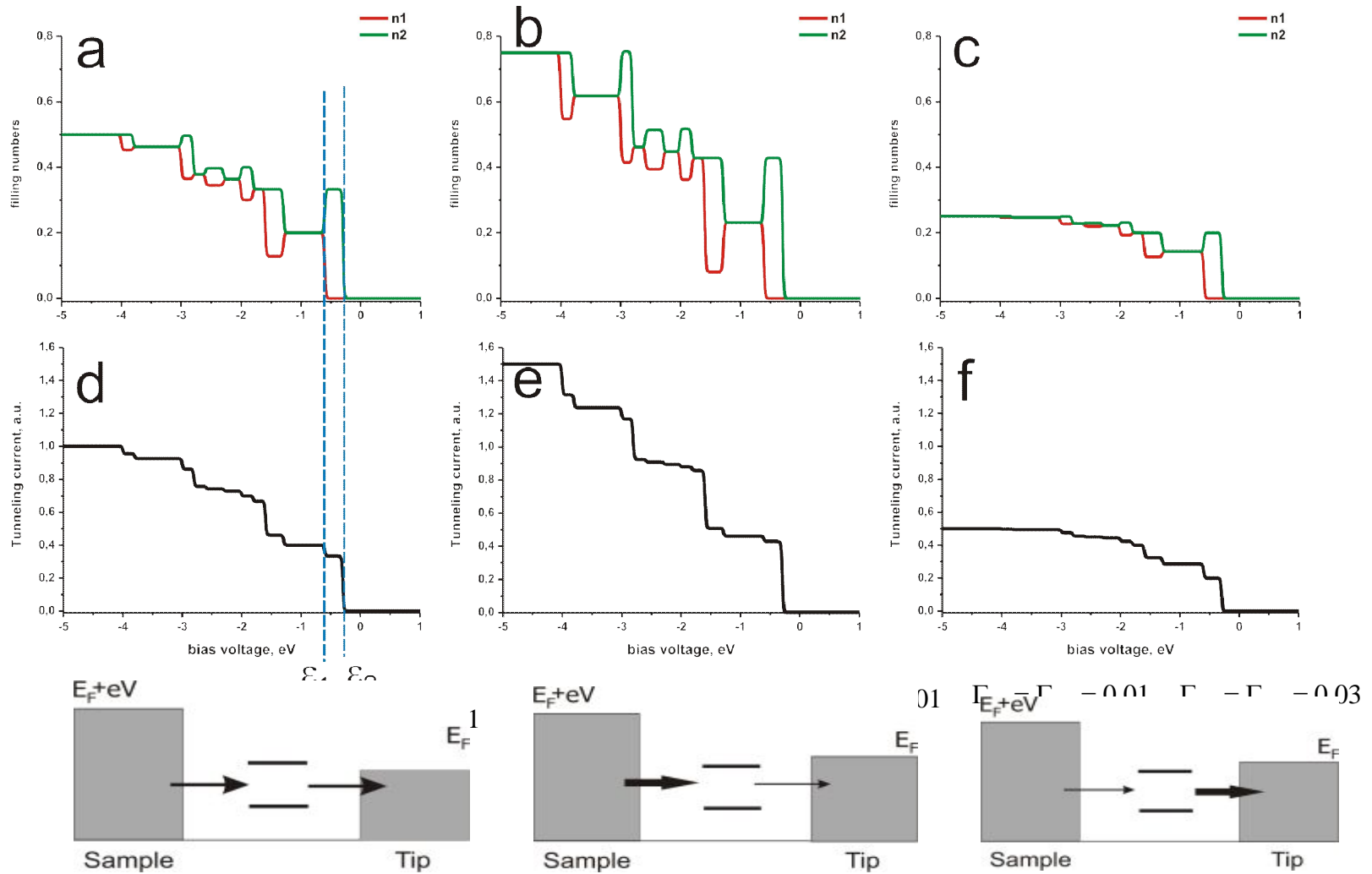
$$n_{2\sigma} = \frac{n_2^T(\varepsilon_2)(1 - n_1^T(\varepsilon_1))}{(1 + n_1^T(\varepsilon_1))(1 + n_2^T(\varepsilon_2)) - 4n_1^T(\varepsilon_1)n_2^T(\varepsilon_2)}$$

$$1) \quad n_2^T = 1/2 \quad n_1^T = 0 \\ n_1 = 0 \quad n_2 = 1/3$$

$$2) \quad n_2^T = 1/2 \quad n_1^T = 1/2 \\ n_2 = n_1 = 1/5$$

$$I_k = \frac{4\Gamma_k \Gamma_p}{\Gamma_k + \Gamma_p} \frac{(f_p(\varepsilon_1) - f_k(\varepsilon_1))(1 - n_2^T(\varepsilon_2)) + (f_p(\varepsilon_2) - f_k(\varepsilon_2))(1 - n_1^T(\varepsilon_1))}{(1 + n_1^T(\varepsilon_1))(1 + n_2^T(\varepsilon_2)) - 4n_1^T(\varepsilon_1)n_2^T(\varepsilon_2)}$$

# Tunneling characteristics and charge distribution



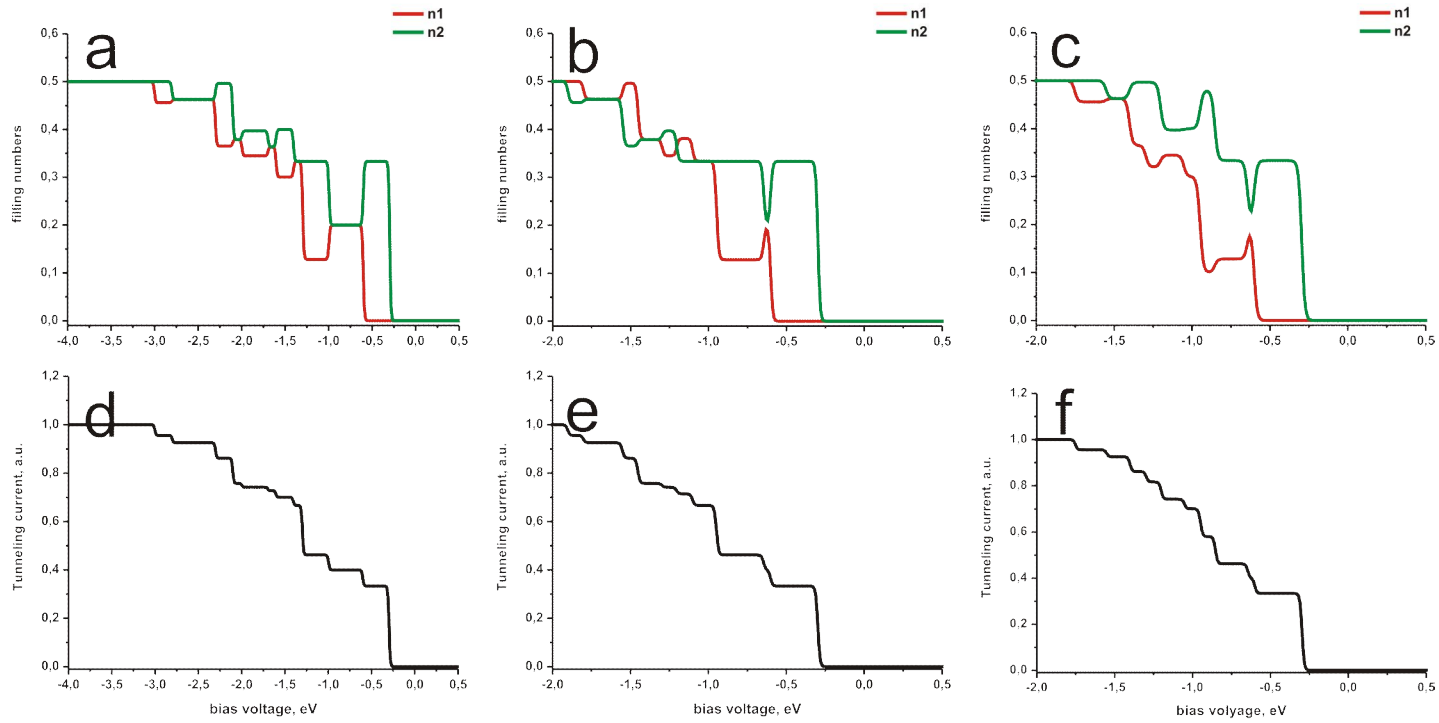
12 steps for  $V =$

$$\epsilon_1 \quad \epsilon_1 + U_{12} \quad \epsilon_1 + U_{11}$$

$$\epsilon_1 + U_{11} + U_{12} \quad \epsilon_1 + 2U_{12} \quad \epsilon_1 + U_{11} + 2U_{12}$$



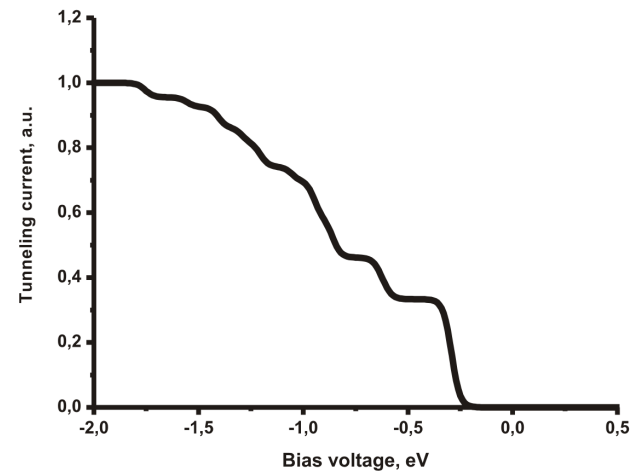
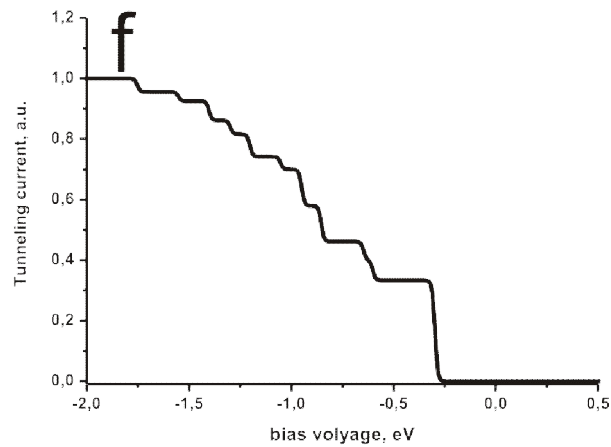
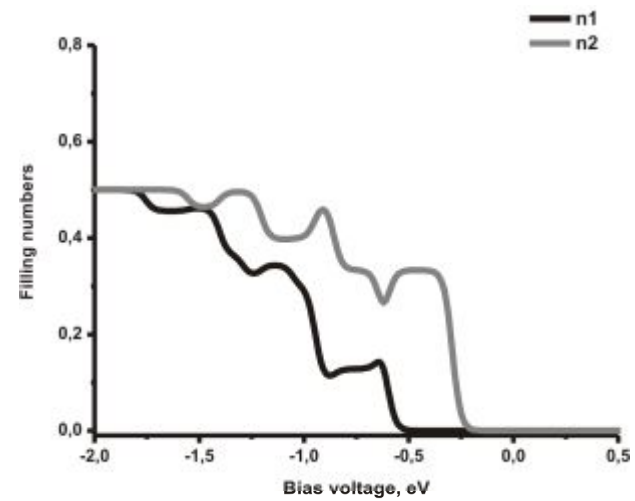
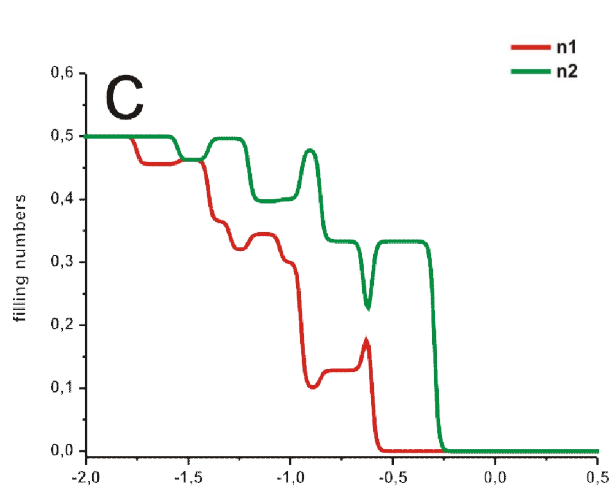
# U dependence



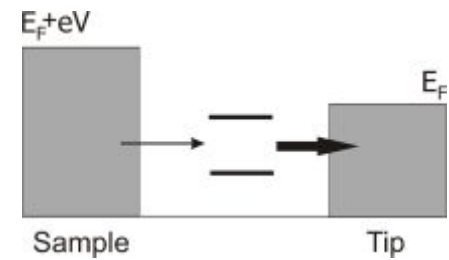
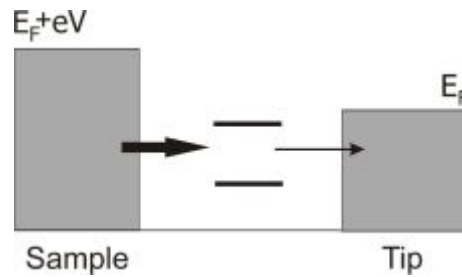
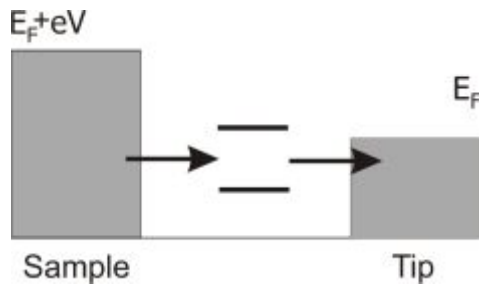
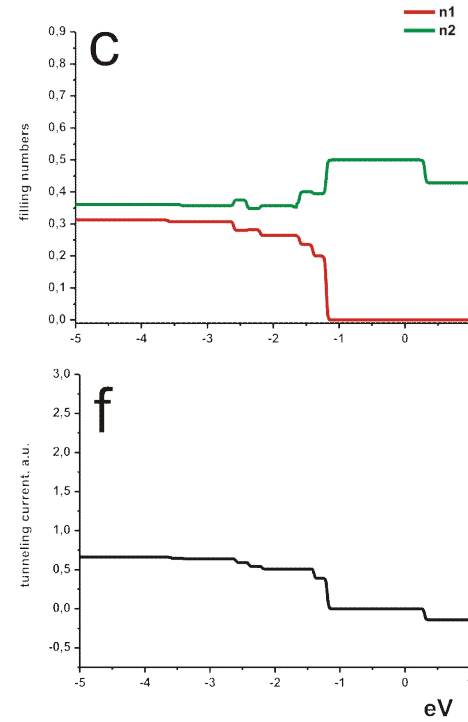
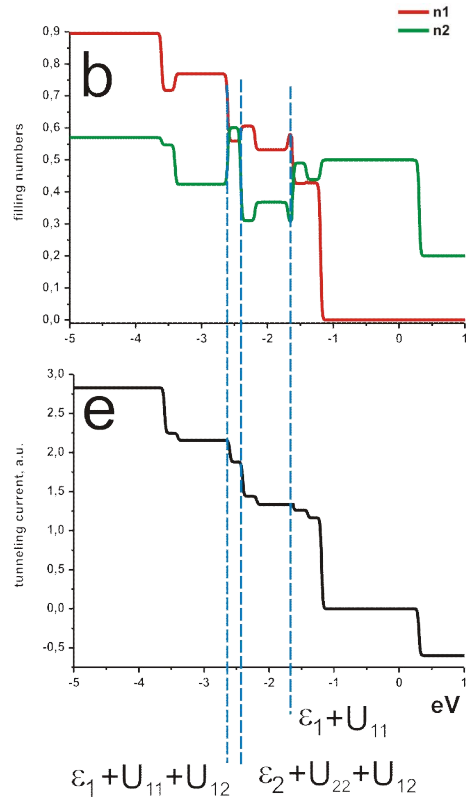
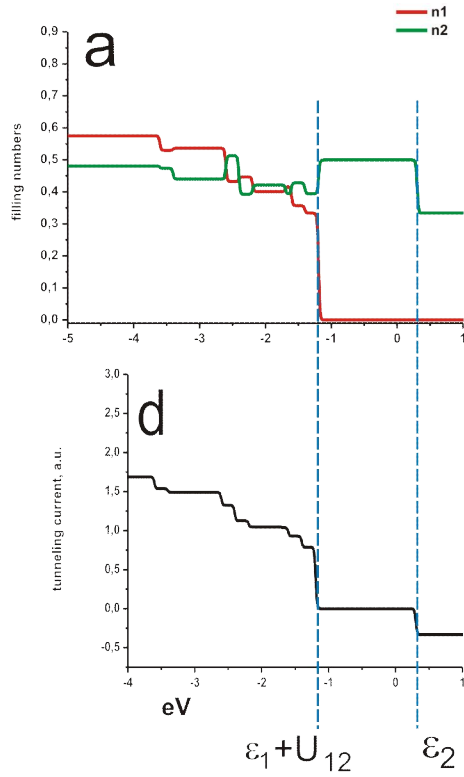
$$U_{12} = 1.0 \quad U_{11} = 1.5 \quad U_{22} = 1.6 \quad U_{12} = 0.4 \quad U_{11} = 0.5 \quad U_{22} = 0.65 \quad U_{12} = 0.15 \quad U_{11} = 0.25 \quad U_{22} = 0.4$$

$$\tau_1 = -0.1 \quad \tau_2 = -0.3$$

# Temperature smoothing

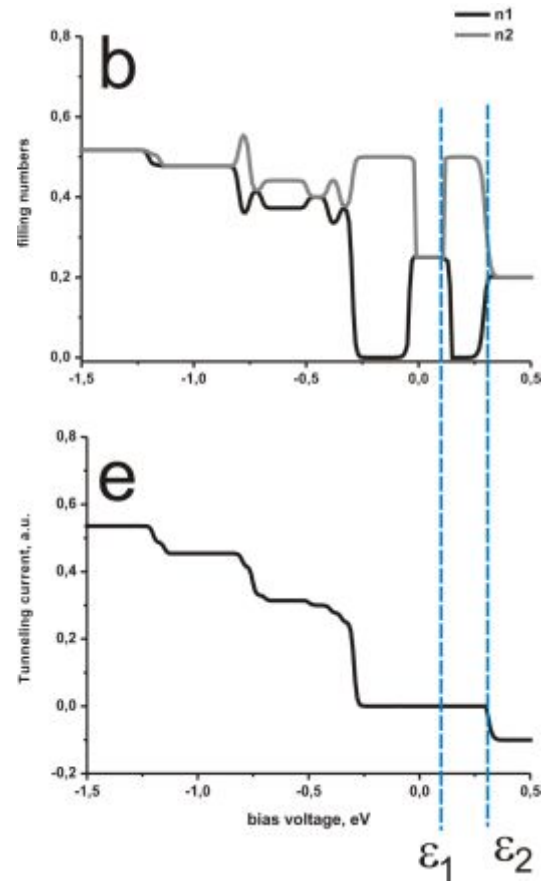


# Inverse occupation



$$T_1 = 0.2 \quad T_2 = -0.3 \quad U_{12} = 1.0 \quad U_{11} = 1.4 \quad U_{22} = 1.7$$

## Charge redistribution inside Coulomb blockade step



$$T_1 = -0.1 \quad T_2 = -0.3 \quad U_{11} = 0.5 \quad U_{22} = 0.65 \quad U_{12} = 0.4$$

# Negative differential conductivity

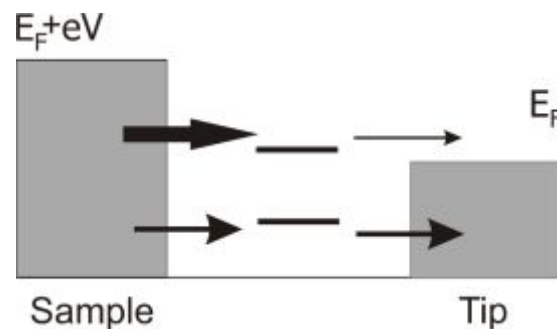
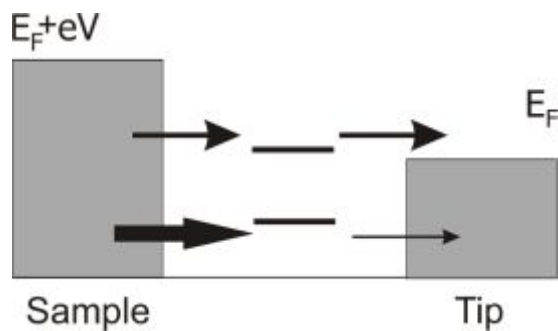
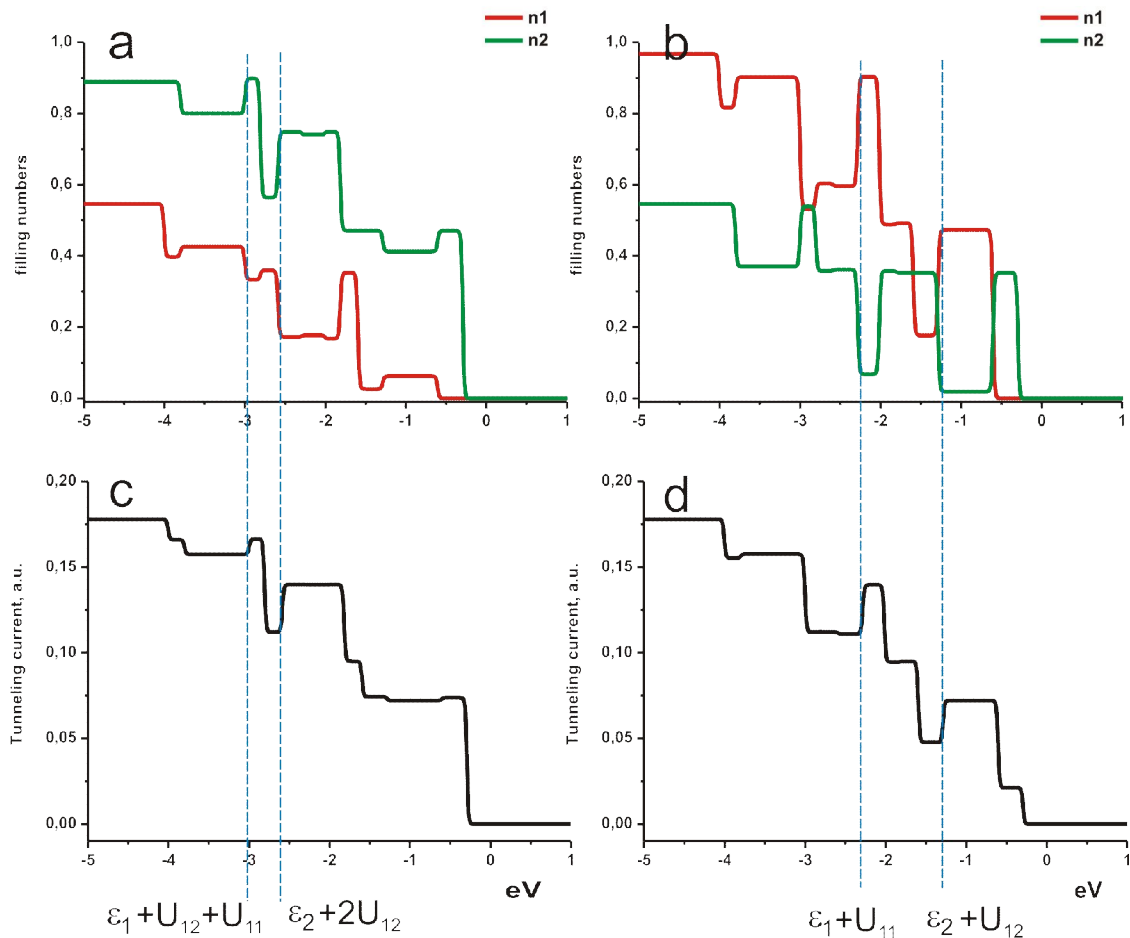
$$T_1 = 0.6$$

$$T_2 = 0.3$$

$$U_{12} = 1.0$$

$$U_{11} = 1.5$$

$$U_{22} = 1.6$$



## Some conclusions

Systems with several states - Coulomb blockade systems with “internal gate” controlled by the tunneling current

Possibility to control charge distribution by tunneling current

Negative differential conductivity